Reorientational Hydrogen Dynamics in Complex Hydrides with Enhanced Li⁺ Conduction

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Supporting Information

ABSTRACT: Lithium amide–borohydrides Li[BH₄]ₓ[NH₂]ₓ possess liquid-like Li superionic conductivity at nearly ambient temperature. The fast Li⁺ diffusion facilitated by the localized motions of the anions is proposed to occur through a network of vacant tetrahedral sites, acting as conduction channels. To study the reorientational dynamics of the anions, we have performed quasielastic neutron scattering experiments on samples with different compositions (x = 2/3, 0.722, 0.737, 3/4) over a broad temperature and time range. To unambiguously disentangle the contributions of the two species, [BH₄]⁻ and [NH₂]⁻, we took advantage of deuterium labeling and could clearly demonstrate that the quasielastic broadening is mainly determined by the [BH₄]⁻ reorientations. With the help of a newly developed model, supported by ab initio molecular dynamics calculations, we have identified three relaxation components, which account for generally anisotropic Cᵣ-rotations of the [BH₄]⁻ tetrahedra including jumps by a small angle from the equilibrium position.

INTRODUCTION

Lithium complex hydrides with [BH₄]⁻ and [NH₂]⁻ anions have been mainly associated with hydrogen storage technologies due to their characteristically high volumetric and gravimetric hydrogen capacity.¹⁻⁴ Apart from this, recent research efforts have focused on another energy-storage related function of lithium amide-borohydrides, namely fast Li⁺ ionic conduction.⁵,⁶ Conductivities of 10⁻¹⁻¹⁰⁻³ S/cm at room temperature classify these materials as promising solid state electrolytes (SSE) for all-solid-state rechargeable batteries.⁷ The best achieved conductivity of 6.4 × 10⁻³ S/cm (at 313 K) in an [BH₄]⁻-rich lithium amide-borohydride⁸ is comparable to typical values of liquid organic electrolytes used in lithium-ion batteries nowadays and, hence, these materials are competitive with the best SSE known to date.⁹⁻¹² The high conductivity in the understoichiometric Li[BH₄]ₓ[NH₂]ₓ, (2/3 < x < 3/4) has been attributed to the presence of a [BH₄]⁻-rich side phase, coexisting with the stoichiometric x = 3/4 phase, commonly referred to as the α-phase in the LiBH₄–LiNH₃ pseudobinary phase diagram.⁸ Lithium amide-borohydrides are characterized by lightweight, negligible electronic conduction, low grain boundary resistance, high thermal stability. Finally, the natural abundance of the constituent elements of these compounds is also considered advantageous in the development of new SSE.⁷ Composition dependent structures of Li[BH₄]ₓ[NH₂]ₓ have been extensively studied by X-ray and neutron diffraction.⁵,¹³⁻¹⁶ The [BH₄]⁻ and [NH₂]⁻ anions with nearly ideal geometry¹⁵ form {Li[BH₄]ₓ[NH₂]ₓ} tetrahedra with a Li⁺-ion in the center. To ensure charge neutrality, there is another set of tetrahedra that remain empty and facilitate Li⁻-migration.⁵ The conductivities of the lithium amide-borohydrides are four or 5 orders of magnitude higher than that of the constituent materials, LiBH₄ and LiNH₃, at room temperature.⁵,⁶ A comparable value of Li⁺-conductivity in LiBH₄ can only be obtained above the temperature of the first-order phase transition from the low-temperature (LT) orthorhombic phase to the high-temperature (HT) hexagonal phase at 381 K.¹⁷,¹⁸ These structural changes are accompanied not only by improved Li⁻ translational mobility, but also by significantly more rapid reorientational motion of [BH₄]⁻ anions.¹⁹⁻²⁰ High anion jump rates have likewise been observed in the related systems, where the disordered HT-like phase is...
stabilized by addition of lithium halides\textsuperscript{21–23} or nanoconfine-
ment\textsuperscript{24,25} to improve the performance of the materials as SSE or
for hydrogen-storage applications. In the case of larger anions, such as sulfates or phosphates, anion assisted ionic conduction has been discussed within the so-called "paddle-wheel" mechanism.\textsuperscript{26,27} The model implies that rotational motion of polyatomic anions enhances the mobility of cations. Although the universal applicability of this idea is under discussion, the model points out that the mechanism of cation diffusion is more complicated than just conventional hopping and that the contribution from reorientations and center-of-mass fluctuations of the anions may be not negligible. Thus, acquiring sufficient knowledge about the relation between the crystal structure, anion reorientational dynamics and cation mobility holds the key for further improvement of ion-conducting and hydrogen-
storage characteristics of these materials.

Since the microscopic dynamical description in mixed amide-
borohydrides is scarce,\textsuperscript{28} the goal of the present work was to
investigate the reorientational motion of [BH\textsubscript{4}]\textsuperscript{−} and [NH\textsubscript{2}]\textsuperscript{−} units in Li[BH\textsubscript{4}]\textsubscript{x−1}([NH\textsubscript{2}]\textsubscript{y})\textsubscript{x} by means of quasielastic neutron scattering (QENS).\textsuperscript{29} This technique has been successfully used to study dynamical properties of metal borohydrides and related compounds in the past decade.\textsuperscript{19–21,30–33} Being sensitive to hydrogen, QENS also probes the relaxation time scale suited to resolve anion jump reorientations. Moreover, QENS delivers information on both spatial and time characteristics of studied processes. This is an advantage of the method compared with other valuable techniques such as solid-state nuclear magnetic resonance spectroscopy (NMR).\textsuperscript{34,35} As both species, [BH\textsubscript{4}]\textsuperscript{−} and [NH\textsubscript{2}]\textsuperscript{−}, contain hydrogen, the main challenge in the interpretation of QENS spectra would be to disentangle the two contributions. Nevertheless, the method provides a tool, namely deuterium labeling, to perform a sophisticated analysis. Thus, employing partially deuterated samples, we aimed to distinguish the [BH\textsubscript{4}]\textsuperscript{−} and [NH\textsubscript{2}]\textsuperscript{−} components, determine the geometry and evaluate the jump rates of anion motions. This detailed information about the microscopic dynamics is a requisite for understanding why mixed amide-borohydrides Li-
[BH\textsubscript{4}]\textsubscript{x−1}([NH\textsubscript{2}]\textsubscript{y})\textsubscript{x} have much better ion-conducting properties than the constituent materials.

\section*{Experimental Section}

\textbf{Samples.} The lithium amide–borohydrides Li-
[BH\textsubscript{4}]\textsubscript{x−1}([NH\textsubscript{2}]\textsubscript{y})\textsubscript{x} (x = 2/3, 0.722, 0.737, 3/4) were synthesized and characterized as described previously.\textsuperscript{9} To avoid the strong neutron absorption by the \textsuperscript{10}B isotope in natural boron, \textsuperscript{11}B-enriched LiBH\textsubscript{4} purchased from Katchem was used in the synthesis. LiNH\textsubscript{2} from Sigma-Aldrich and LiND\textsubscript{2} from Deutero were the precursors for the protiated and partially deuterated samples, respectively. The samples were handled in an Ar-filled glovebox to avoid air exposure.

IR characterization of the samples was performed on a temperature controlled Specac ATR setup mounted on a Biorad Excalibur FT-IR instrument in the frequency range between 600 and 4000 cm\textsuperscript{−1} with a resolution of 1 cm\textsuperscript{−1}.

\textbf{Calculations.} The experiments were complemented with sets of \textit{ab initio} molecular dynamics (MD) calculations. The constant volume MD studies were performed with the Nose–
Hoover thermostat,\textsuperscript{36} and the time step 0.6 fs was chosen for integration of the equations of motions. For calculations of forces we used the Born–Oppenheimer approximation and the density functional theory (DFT). The core/valence electron interaction was described by the projector augmented wave method as implemented in the VASP package.\textsuperscript{37,38} Atoms were represented by pseudopotentials with the valence electronic configurations 1s\textsuperscript{2}2s\textsuperscript{2} for Li, 2s\textsuperscript{2}2p\textsuperscript{1} for B, 2s\textsuperscript{2}2p\textsuperscript{3} for N, and 1s\textsuperscript{1} for H. The exchange correlation functional was approximated by the Perdew–Burke–Ernzerhof generalized gradient approach,\textsuperscript{39} and the wave functions were expanded in the plane wave basis set with the kinetic energy cutoff of 450 eV.

A single k-point was used for the MD calculations. All MD calculations were performed in a cubic unit cell with the experimental lattice constant 10.664 Å.\textsuperscript{40} To approach dynamics of the system we used an enhanced temperature method and two independent sets of calculations were performed at 400 and 800 K. At each temperature the system was equilibrated for 5 ps followed by 15 ps of data collection. The stoichiometry of the system was changed by replacement of [NH\textsubscript{2}]\textsuperscript{−} by [BH\textsubscript{4}]\textsuperscript{−}, keeping the volume of the unit cell constant.

To illustrate rotational mechanisms of different species, we calculated the projection of the vectors linking the central B or N atom with the hydrogen atoms of the corresponding anion \(\vec{r}(t) = \vec{r}(t) - \vec{r}(0)\), where the time lag \(t\) ranged from 1.2 fs to 5 ps, \(\vec{r}(0)\) and \(\vec{r}(t)\) are the unit vectors (BH/IBH or NH/INH) at the initial time point and at the time lag \(t\), respectively. For each [BH\textsubscript{4}]\textsuperscript{−} there are four such autocorrelation functions, while two are necessary to describe rotational dynamics of [NH\textsubscript{2}]\textsuperscript{−}.

\textbf{Neutron Experiment.} QENS measurements were performed on the cold neutron time-of-flight spectrometers FOCUS at Paul Scherrer Institute in Villigen, Switzerland\textsuperscript{41,42} and IN16B at the Institut Laue–Langévin in Grenoble, France.\textsuperscript{43} The instruments operate on significantly different time scales and, hence, we could follow the quasielastic signal in a broad temperature range from 150 to 425 K.

At IN16B\textsuperscript{44} a neutron wavelength of \(\lambda = 6.271\ \text{Å}\) was selected, which corresponded to the resolution of 0.8 \(\mu\text{eV}\) (full width at half-maximum, fwhm). The wavevector transfer available with this setting ranged from 0.2 to 1.9 Å\textsuperscript{−1}. Two types of measurements were performed on IN16B. First, both elastic and inelastic fixed window scans (EFWS and IFWS)\textsuperscript{35} were recorded at a rate of 1.0–2.0 K/min. Second, we used the QENS mode with a Doppler drive changing the wavelength of incident neutrons to obtain spectra at several selected temperatures in the dynamical range of \pm 30 \(\mu\text{eV}\). The samples with the thickness of 1 mm were measured in an aluminum flat sample holder positioned in transmission geometry at 135° to the incident beam. The necessity to use relatively "thick" samples is explained by the presence of natural Li, which also absorbs neutrons, although to a less extent than natural B.

The experiments on FOCUS were performed with a wavelength of incident neutrons of \(\lambda = 4.0\ \text{Å}\). The resolution of 0.220 meV (fwhm) and a much broader energy transfer window (~2–3 meV) were needed to study anion reorientational dynamics at temperatures above 300 K. The spectra were binned in a range of scattering vectors of \(Q = 0.5–2.5\ \text{Å}\textsuperscript{−1}. The sample containers used on FOCUS had a hollow cylindrical geometry with the gap width of 1 mm between the inner and outer cylinder and the outer diameter of 12 mm.

Additional runs with vanadium standards and empty sample containers were carried out on both spectrometers to perform typical corrections for experimental distortions. The procedure included vanadium normalization, detector efficiency correction and background subtraction. The sample attenuation and self-shielding factors were calculated with respect to the geometry of the experiment. The standard data reduction of the IN16B data
was performed using the LAMP\textsuperscript{46} software package. The DAVE\textsuperscript{1} package was used for both the data reduction of the FOCUS spectra and further examination of all the data sets at individual $\mathbf{Q}$-groups.

The sample thickness of 1 mm unavoidably led to pronounced effects of multiple scattering, which could not be neglected in this case. To eliminate its influence, multiple scattering corrections were performed with the help of the McStas software (http://mcstas.org) in an iterative way. The input files with the scattering function were generated using the model function described in the following section on the doubled momentum-range as compared to the experimentally accessible one.

For both instruments, the QENS spectra were analyzed in a program module,\textsuperscript{48} which performs two-dimensional surface fits. This approach enables obtaining more stable and consistent results, as simultaneous fits with both $E$ and $\mathbf{Q}$ being independent variables reduce the total number of free parameters to be adjusted.

## RESULTS AND DISCUSSION

### Data Analysis

The analysis of stochastic motions in Li[\[BH_4\]]\textsubscript{1}...[NH_2]... is significantly simplified owing to the large incoherent cross section of hydrogen. Even for the partially deuterated samples the measured intensity, $I_{\text{meas}}$ is dominated by incoherently scattered neutrons. In this case, only single-particle dynamics have to be considered. Hence, the QENS analysis is based on the fitting of experimental data to a model incoherent dynamic structure factor, $S(Q,E)$, convoluted with the resolution function of the instrument, $R(Q,E)$:

$$I_{\text{meas}} \sim \exp(-2W) S(Q,E) \otimes R(Q,E) + bk(Q)$$

where $\exp(-2W)$ is the Debye–Waller factor and $bk(Q)$ is a flat background accounting for faster motions, which cannot be resolved on the available experimental time scale.

The reorientational motions of the [NH\textsubscript{2}]\textsuperscript{−} anions have been studied less extensively than those of the [BH\textsubscript{4}]\textsuperscript{−} anions.\textsuperscript{19,20,50,51} A low symmetry environment of the amide group would allow only 180°-flips along 2-fold axes, whereas other jump rotations (90°-tumbling in the cubic phase, C\textsubscript{t} uniaxial rotation in the tetragonal phase) are possible around additional axes provided by the site symmetry.\textsuperscript{49} The geometry of [BH\textsubscript{4}]\textsuperscript{−} reorientations is also defined by the distances within the crystal and its symmetry. In the LT orthorhombic phase of bulk LiBH\textsubscript{4}, the dominating motion is a 3-fold jump rotation around the C\textsubscript{3} axis.\textsuperscript{19,25,52} For the HT hexagonal phase the trigonal disorder model was proposed,\textsuperscript{20,25} where the [BH\textsubscript{4}]\textsuperscript{−} unit undergoes rapid reorientational jumps, accompanied by quasi-free jumps of the three trigonal hydrogen atoms about the C\textsubscript{3} axis of the anion (parallel to the crystallographic $c$ axis). However, none of these models were appropriate to consistently describe the reorientational dynamics of the [BH\textsubscript{4}]\textsuperscript{−} groups in Li-[BH\textsubscript{4}]...[NH\textsubscript{2}]... in a broad temperature range. Therefore, we propose a modification of the 120°-tumbling model with a certain degree of anisotropy in the jump rates. The idea is illustrated in Figure 1. The C\textsubscript{3} axes are not equivalent and the jump rate around one of them, $1/\tau_C$, is different (faster) than around the other three, $1/\tau_0$. There are additional sites ($\alpha$ and $\beta$) at an angle $\theta$ from the equilibrium positions 1, 2, and 3. The radius of the circle, on which the H atoms are located, can be calculated from the B–H bond length, $r_{\text{BH}}$ as $r_0^2 = \frac{2\sqrt{2}}{3}r_{\text{BH}}$. Fast jumps with the residence time $\tau_1$ can be performed in the following directions: $n \to n_{\alpha}$ or $n_{\beta} \to n$ and $n_{\beta} \to n$, $n \in \{1, 2, 3\}$. Thus, the sites are not equivalent, and the occupational probability of any $n$-th site is 1/8 and any $n_{\alpha}$ or $n_{\beta}$-th site is 1/16. This simplified picture served to mimic disorder around the equilibrium positions, which can be significant in mixed amide-borohydrides as has been shown in simulations.\textsuperscript{54,55}

The presented scheme of jump reorientations has common features with the models proposed by Verdal et al.\textsuperscript{20} The advantage of our approach is that it is applicable for a broad temperature range, in which the character of reorientational dynamics gradually changes. Moreover, the focus of the earlier study\textsuperscript{20} was mainly the fraction of elastically scattered neutrons, or elastic incoherent structure factor (EISF), whereas the complete analytical expression of the dynamic structure factor is required to profit from the simultaneous surface fits in the $(Q,E)$-domain employed in our analysis.

Following the classical methodology,\textsuperscript{53,56,57} we solved the rate equations given in the Supporting Information (eq S1) and derived the dynamic structure factor $S_{\text{rot}120\_0}(Q,E)$ for the proposed model:

$$S_{\text{rot}120\_0}(Q,E) = \mathbf{L}(E)\mathbf{S}\mathbf{B}(Q)$$

where $\mathbf{L}(E)$ is the row-vector of Lorentzian functions $\mathbf{L}(1, E)$ with the following line widths:

$$\Gamma = \begin{pmatrix} 0, \frac{\alpha}{\tau_0}, \left(\frac{\alpha + 1}{\tau_0}, \frac{\alpha + 1}{\tau_0}, \frac{1}{\tau_0}\right), \\ \frac{1}{\tau_0}, \frac{3}{\tau_0} + \frac{4}{\tau_1}\end{pmatrix}$$

$$S = \begin{pmatrix} 17 & 66 & 12 & 12 & 12 & 3 & 3 & 3 \\ 27 & -42 & 4 & 4 & 1 & 1 & 1 & 1 \\ 3 & 6 & -4 & -4 & -4 & 1 & 1 & 1 \\ 2 & 4 & 0 & 0 & 0 & -2 & -2 & -2 \\ 24 & -24 & 32 & -16 & -16 & 8 & -4 & -4 \\ 24 & -24 & -32 & 16 & 16 & 8 & -4 & -4 \\ 16 & -16 & 0 & 0 & 0 & -16 & 8 & 8 \\ 9 & 18 & -12 & -12 & -12 & 3 & 3 & 3 \\ 6 & 12 & 0 & 0 & 0 & -6 & -6 & -6 \end{pmatrix}$$

$$\mathbf{B}(Q) = \begin{pmatrix} 1, 0, 0, 0, 0, 0, 0, 0 \end{pmatrix}$$

$\mathbf{B}(Q)$ is the column-vector of spherical Bessel functions of the zeroth order.

![Figure 1](https://example.com/figure1.png)
Article

In the limit \( \theta \to 0 \) at very low temperatures or if \( \tau \) becomes too fast to be resolved on the time scale of the experiment, eqs 2–5 can be simplified, and the dynamic structure factor reads:

\[
S_{\text{rot,120}}(Q, E) = \frac{1}{4}(1 + 3j_0(Q_0\sqrt{3}))\delta(E) + \frac{1}{2}(1 - j_0(Q_0\sqrt{3}))\mathcal{L}(\Gamma_1, E) + \frac{1}{2}(1 - j_0(Q_0\sqrt{3}))\mathcal{L}(\Gamma_2, E)
\]

The last point to mention is that the QENS analysis does not permit to distinguish between the uniaxial \( C_2 \)-reorientations with all four hydrogen atoms performing jumps and the uniaxial \( C_2 \)-reorientations with one immobile atom on the axis of rotation discussed above. The same remains valid for the models taking into account jump motions with different rates. The dynamic structure factor for the prevailing \( C_2 \)-mechanism has the same expression (eq S9 of the Supporting Information) from a formal mathematical point of view as eq 6. However, jump motions around the \( C_3 \) axis correspond better to the symmetry of the local environment of the \( \text{[BH}_4\text{]}^– \) units in the cubic \( \alpha \)-phase of \( \text{Li[BH}_4\text{]}_{1/4}[\text{NH}_2]_{3/4} \). This is further evidenced by IR spectra in the frequency range of the \( \text{[BH}_4\text{]}^– \) bending modes (Figure S3 of the Supporting Information), which display characteristic changes upon a symmetry reduction from \( T_d \) for ideal \( \text{[BH}_4\text{]}^– \) tetrahedra to \( C_3 \) because of a trigonal deformation.55,59

Our MD simulations also support the idea of the predominant \( C_2 \)-reorientation mechanism for borohydride tetrahedra, which is illustrated with the angular autocorrelation functions in Figure 2.

Figure 2. Autocorrelation functions of \( \text{[BH}_4\text{]}^– \) determined from the MD simulations at \( T = 400 \) K (solid lines) and \( T = 800 \) K (dotted lines) for the \( x = 0.656 \) composition. The \( C_2 \) axes of rotation \((a_0, a_1, a_2, a_3)\) in Figure 1) are assumed to be collinear to the B–H bonds at time 0.

If jump rotations occurred only around axis \( a_0 \) (Figure 1), one component \( r(t) \) would not change with time, which is valid in the low temperature regime within 15 ps of the simulation time. If reorientations around \( a_1, a_2, a_3 \) are also possible, but on a slower time scale, this component starts to decay. Indeed, as the temperature increases, jumps around various \( C_3 \) axes become more frequent. Owing to the difference in the relaxation times, it is still easy to distinguish \( r(t) \) from the other three ones at \( T = 400 \) K. Any type of the \( C_2 \) model would not leave just one atom immobile or less mobile, and thus, can be ruled out. At higher temperatures the gap between the curves is smeared away, because rotations around all axes become equally probable. In contrast to the \( \text{[BH}_4\text{]}^– \) tetrahedra, the \( \text{[NH}_2\text{]}^– \) groups do not perform any reorientational motion at low temperatures (Figure S2 of the Supporting Information) within 15 ps of the simulation time, although this does not exclude a slower relaxation process. The amplitude of the \( \text{[NH}_2\text{]}^– \) wiggling or librational dynamics is, nevertheless, large. Flips of the \( \text{[NH}_2\text{]}^– \) units related to Li\(^+\) translational motion start in the high temperature regime, where
the reorientational jump processes for both anions occur on the time scale of ~0.1 ps.

**Anion Dynamics on Nanosecond and Picosecond Time Scale.** The temperature dependence of the elastic intensity of LiNH₂ and Li[BH₄]₁₋ₓ[NH₂]ₓ obtained on different time scales is displayed in Figure 3 and 4. In the picosecond time range accessible on FOCUS the mixed samples show the onset of a quasielastic contribution above 300 K, whereas the gradual decrease of the elastic intensity in LiNH₂ is due to the temperature dependence of the Debye–Waller factor alone. From this observation we conjectured that the [NH₂]⁻ groups probably do not contribute to the quasielastic broadening in the mixed compounds detected in the FOCUS experimental time window. The experiment on IN16B with protiated and partially deuterated samples provided an additional and convincing evidence of this idea (Figure 4).

Assuming that the samples scatter mainly incoherently and that [BH₄]⁻ and [NH₂]⁻ motions are not correlated, the dynamic structure factor of the protiated and deuterated sample can be expressed in the following way:

\[
S_{prot}(Q, E) = \frac{4\sigma_H S_{BH4}(Q, E) + 2\left(\frac{x}{1-x}\right)\sigma_D S_{NH2}(Q, E)}{4\sigma_H + 2\left(\frac{x}{1-x}\right)\sigma_D}
\]

(9a)

\[
S_{deut}(Q, E) = \frac{4\sigma_H S_{BH4}(Q, E) + 2\left(\frac{x}{1-x}\right)\sigma_D S_{NH2}(Q, E)}{4\sigma_H + 2\left(\frac{x}{1-x}\right)\sigma_D}
\]

(9b)

where \(S_{BH4}(Q, E)\) and \(S_{NH2}(Q, E)\) stand for the [BH₄]⁻ and [NH₂]⁻ contributions and \(\sigma_H\) and \(\sigma_D\) are the neutron incoherent scattering cross sections of hydrogen and deuterium, respectively. Equation 9 is basically a system of two linear equations, which can be solved in the whole scanned temperature range (Figure 4, upper panel). Apparently, all main characteristic step-like features on the nanosecond time scale in the mixed compounds originate from the [BH₄]⁻ units. The decrease of the [NH₂]⁻ elastic intensity is mostly due to vibrational and librational motions. These observations agree with the results of the DFT calculations, which show that the [NH₂]⁻ groups only wiggle when the rotation of the [BH₄]⁻ units sets in (Figure S2 of the Supporting Information).

The EFWS and IFWS of the samples with \(x = 2/3\) and \(x = 3/4\) are similar in the temperature range of 10–340 K (Figure 4, lower panel). The onset of the dynamics seen on FOCUS with a coarser resolution above 300 K is shifted to lower temperatures on IN16B, since intensity drop of EFWS or intensity increase of IFWS typical for thermally activated processes occur in the temperature range, where relaxation times, \(\tau\), fulfill the condition: \(\hbar/\tau \approx \sigma_{rel}\). These dynamics correspond to the rotational motion of the [BH₄]⁻ groups and are similar to what was observed in the bulk LiBH₄. The second characteristic decrease of the elastic intensity and the corresponding increase of the inelastic intensity can be seen only in the highly conducting sample with \(x = 2/3\) above ~355 K, which can be related to a pronounced endothermic event at 313 K on heating. The stoichiometric composition (\(x = 3/4\)) demonstrated a significantly smaller value of the latent heat at 313 K and this fact can account for the absence of the corresponding features in the EFWS and IFWS. The transition at 313 K is presumably associated with a side phase coexisting with the cubic \(\alpha\)-phase for \(x = 2/3–3/4\) and reported in literature, the fraction of the side phase being larger in BH₄-rich samples. The presence of the side phase could also explain the temperature behavior of the IR spectra (Figure S3 of the Supporting Information), which demonstrate additional [BH₄]⁻-bending modes that disappear upon heating. The structure of the dominating \(\alpha\)-phase does not change above 313

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**Figure 3.** Elastic intensity of LiNH₂ and mixed lithium amide-borohydrides Li[BH₄]₁₋ₓ[NH₂]ₓ measured on FOCUS and averaged over the analyzed Q-range as a function of temperature.

**Figure 4.** Upper panel: EFWS of the protiated and partially deuterated samples (\(x = 2/3\)) recorded on IN16B. The [BH₄]⁻ and [NH₂]⁻ contributions are the solutions of eq 9 and scaled to 0.5 at low temperature for clarity. Lower panel: EFWS (circles) and IFWS (triangles) of the partially deuterated samples Li[BH₄]₁₋ₓ[ND₂]ₓ with \(x = 3/4\) (red) and \(x = 2/3\) (blue) averaged over the studied Q-range.
K exhibiting only a slight thermal expansion. The trace of this transition can also be seen in the elastic intensity measured on FOCUS (Figure 3) for the \( x = 2/3 \) composition in the temperature range 300—350 K, where the steepness of the temperature dependence is larger than for the other samples.

Taking into account that only \([\text{BH}_4]^-\) rotational motions are resolved on the time scale of FOCUS and IN16B, the fraction of the hydrogen atoms in the borohydride anions, \( p_{\text{BH4}} = 4/(4 + 2x/(1 - x)) \), has to be added to the final expression of the dynamic structure factor:

\[
S(Q, E) = (1 - p_{\text{BH4}})\delta(E) + p_{\text{BH4}}S_{\text{model}}(Q, E)
\]

(10)

The FOCUS spectra at the highest available temperatures could be satisfactorily fitted with the simpler model describing \( C_3 \) jump reorientations (eqs 6 and 10). However, after having applied it for a broader temperature range, we found it inconsistent. It was clear that the underlying rotational mechanism was more complex. First, the relaxation times, \( \tau_0 \) and \( \tau_r \), started decreasing for \( T < 350 \) K, which is unphysical. Second, it was necessary to accept that \( p_{\text{BH4}} \) might decrease with temperature as well. Third, we obtained an overestimated \( B-H \) bond length (>1.36 Å) in comparison to the literature values.15,54

The model independent analysis (eq 7) showed that the \( Q \)-dependence of the elastic incoherent structure factor (EISF, \( A_0 \) in eq 8) at low temperatures corresponds to a characteristic jump distance \( \leq 1.0 \) Å, which is significantly less than the \( H-H \) distance in the \([\text{BH}_4]^-\) or \([\text{NH}_2]^-\) groups. Therefore, the model with additional jump sites was applied (Figure 1, eqs 3–5). In comparison with its predecessor, this function has two additional adjustable parameters, \( \tau_r \) and \( \theta \), which is not generally favorable for the stability of fitting. Hence, we had to introduce some constraints. First, the \( B-H \) bond length was fixed to 1.225 Å as obtained from the analysis of the bulk LiBH₄ data with eq 6. This value is also in a good agreement with the previously published results and the average bond length 1.228 Å from our MD calculations. Second, the fraction of rotating \([\text{BH}_4]^-\) units also remained restricted to the value determined from the nominal composition of a mixed compound. Finally, the parameters related to the fastest contribution were evaluated only for \( T < 323 \) K. Their values in the high-temperature range were estimated by extrapolation and fixed as well.

The proposed model (Figure 1, eq 3–5) contains a sum of several Lorentzians, which can be grouped into the narrow (\( \Gamma[2] \) = 4\( h/\tau_0 \), due to the \( 120^\circ \)-reorientations around a1, a2, a3), medium (\( \Gamma[5] = h/2 \times (5/\tau_0 + 3/\tau) \), which contains the faster reorientational motion around a0) and broad quasielastic (all the other line widths) components. Their relative contributions to the total line broadening change with temperature, because all the three relaxation times are characterized by different activation energies. This statement is illustrated by Figure 5. At elevated temperatures the broadest component is almost identical to a flat contribution. This explains why the fits with the simpler model (eqs 6 and 10), in principle, work nicely. At low temperatures, the narrowest contribution becomes unresolved and is basically proportional to the resolution function; the broadest Lorentzian, on the contrary, appears to be distinguishable under these experimental conditions. The usage of eqs 6 and 10 in this temperature range leads to the erroneous temperature dependence of \( p_{\text{BH4}} \) and the relaxation times.

The relaxation time of fast oscillations, \( \tau_f \), is about 1 ps at \( T = 250-323 \) K and does not depend on the composition of the mixed amide-borohydrides within the margin of error. The \( \theta \) value is about 15–17° at 250 K and increases with temperature, but as soon as the slowest component can be reliably resolved, \( \theta \) has to be fixed together with \( \tau_r \). The estimate of the activation energy for the fastest component gives \( E_A = 3.6 \pm 0.5 \) kJ/mol. For the sake of mathematical simplicity, we considered deviations only around positions 1, 2, 3 (Figure 1). This definitely does not rule out a more complicated scheme of jump sites. Moreover, we still cannot completely exclude the possibility that this relaxation process partially originates from the \([\text{NH}_2]^-\) anions, which can oscillate with an amplitude of about 45° according to the MD simulations (Figure S2 of the Supporting Information). Since the quasielastic incoherent structure factors (QISF, \( A_x \) in eq 7) of the fastest contribution are much less than those of the other two components, it could appear in the IFWS (Figure 4, lower panel) only as a weak shoulder before the main bump. However, if it existed, the statistical quality of the data in this temperature range does not allow us to see any difference between the partially deuterated and protiated samples and, hence, to prove or disprove the \([\text{NH}_2]^-\) contribution. Broad quasielastic features were also described in several works on disordered systems and attributed to overdamped anion vibrations characterized by mean-squared displacement distances \( \sqrt{\langle u_x^2 \rangle} \). If the latter interpretation is accepted in the analysis of our data, then the intensity dependence of the fast component on \( Q \) yields, for example, \( \sqrt{\langle u_x^2 \rangle} = 0.33 \) Å at \( T = 300 \) K. At the same time, the jump distance between sites \( n_x \) and \( n_y \) equals 0.40 Å. This illustrates...
that our model description with librational motions by an angle $\theta$ may be closely related to the concept of the overdamped vibrational modes.

Figure 6 displays the temperature dependencies of the $[\text{BH}_4^-]$-reorientational relaxation times in Li$[\text{BH}_4]_{1-x}[\text{NH}_2]_x$ calculated from the QENS spectra recorded on both instruments. For comparison, we also performed a reanalysis of the LiBH$_4$ data from the QENS spectra recorded on both instruments. The two regions with a larger ($T < 320$ K) and smaller ($T > 340$ K) activation energies are even more pronounced. This temperature behavior correlates with that established for the Li-conductivity and is a new example of coupling between Li-mobility and enhanced anion dynamics.

At first sight, the difference between the relaxation times measured on FOCUS and IN16B is significant (Figure 6) even allowing for resolution effects, because the analysis of the LiBH$_4$ data demonstrated that both instruments delivered consistent results. The answer can be found, if a broader temperature range available in the IWFS is analyzed. To fit the data to eq 8, we need to know the functional dependence of $\tau_0$ and $\tau$ on temperature. Assuming that both relaxation times follow the Arrhenius law

$$\tau = \tau_0 \exp\left(\frac{E_A}{RT}\right)$$

we were not able to obtain physically reasonable values of the fit parameters. Indeed, the fits of the individual QENS spectra at $T = 220$, 250, and 300 K measured on IN16B showed that the origin of the quasielastic broadening at lower temperatures is mainly the uniaxial $C_3$-reorientation, the slowest component being too narrow even at $T = 300$ K. It affects the high-temperature wing of the IFWS curve, but does not have any influence at $T < 300$ K and, hence, cannot determine the broad shape of the IFWS curves. A single component with a smaller value of the activation energy, $E_A$, could extend the IFWS signal over a broader temperature range, however, the resulting line is highly asymmetrical. Therefore, we included a Gaussian distribution of activation energies into our analysis, which is quite common for solid solutions with mixed anions:

$$T_{\text{IFWS}}(T) = \int T_{\text{IFWS}}(E, T) g(E; E_A, \Delta E_A) \, dE$$

where $g(E; E_A, \Delta E_A)$ is the Gaussian function with the maximum at $E = E_A$ and the variance $\Delta E_A$. This approach leads to a much better agreement between the experimental data and the model IFWS curves (Figure 7).

The results of the fits with the Gaussian distribution function are summarized in Table 2. The sample with the $\text{BH}_4^-:\text{NH}_2$ ratio of 1:2 ($x = 2/3$) exhibits a broader range of the activation energies than the $x = 3/4$ composition. The corresponding relaxation times, $\tau$, are displayed in Figure 6, lower panel as a hatched area, which covers the values evaluated from the QENS spectra recorded both on FOCUS and IN16B. The distribution of the activation energies explains, why the final fit results strongly depend on the instrumental resolution, which was not the case for the bulk LiBH$_4$. Different local environments of the BH$_4$ groups in the mixed compounds, especially with the BH$_4$-rich side phase, as well as additional jump sites on the circumference of the circle can cause a change in the energy barrier for rotation. It is necessary to mention that the presence of multiple scattering effects can influence the estimates significantly. Unfortunately, because IFWS/EFWS encompass a broad temperature range, the correction procedure converges slowly and is very time-consuming and challenging as compared
to the analogous approach for QENS spectra measured at a single temperature point.

There remains an open question about the nature of the dynamics that set in above 350 K in the borohydride rich samples \((x = 2/3)\). The model-independent approach showed that the EISF of \(\text{Li}[\text{BH}_4]_{1/3}[\text{NH}_2]_{2/3}\) did not depend on \(Q\) within the error margins and stayed at the level of 0.88 at \(T = 360\) K and 0.82 at \(T = 375\) K. This behavior excludes localized processes with the EISF tending to 1.0 at small-\(Q\) values, the assumption of a diffusional process only for a certain fraction of particles in the system. This would corroborate the interpretation that the transition at 313 K is due to the melting of the side phase. To prove the conjecture, jump diffusion models have to be tested. The Chudley—Elliott model, which considers jump vectors of constant length, \(l\), and random direction, has the following \(Q\)-dependence of the quasielastic line width:

\[
\Gamma(Q) = \Gamma_0 \left(1 - \frac{\sin(\theta)}{Ql}\right)
\]

Here \(\tau_r\) is the residence time. \(\Gamma(Q)\) tends to 0 at small-Q values, however, the experimental line widths are severely distorted in this \(Q\)-range due to the multiple scattering (Figure 8). The iterative correction procedure involving eq 13 yields \(l = 4.4 \pm 0.6\) Å and \(\tau_r = 0.62 \pm 0.06\) ns at \(T = 360\) K for approximately 12% of the \([\text{BH}_4]^-\) units, but the agreement between the experimental data and the Chudley—Elliott model at \(T = 375\) K is significantly worse. This is an indication that eq 13 can serve only as a rough approximation and a more detailed study is required to clarify the motion mechanism in this temperature range.

### Table 2. Parameters of the Best Fit IFWS Curves Obtained for the Uniaxial C<sub>3</sub>-Rotation Model with a Gaussian Distribution of Activation Energies in the Temperature Range \(T = 150–350\) K on IN16B

<table>
<thead>
<tr>
<th>(x)</th>
<th>(\text{Y})</th>
<th>(\tau_r), fs</th>
<th>(E_a), kJ/mol</th>
<th>(\Delta E_a), kJ/mol</th>
</tr>
</thead>
<tbody>
<tr>
<td>2/3</td>
<td>(\text{NH}_2)</td>
<td>1.22(0.12)</td>
<td>25.2(0.2)</td>
<td>2.64(0.04)</td>
</tr>
<tr>
<td>2/3</td>
<td>(\text{ND}_2)</td>
<td>2.57(0.18)</td>
<td>23.3(0.2)</td>
<td>2.59(0.04)</td>
</tr>
<tr>
<td>3/4</td>
<td>(\text{NH}_2)</td>
<td>2.87(0.19)</td>
<td>24.3(0.2)</td>
<td>1.30(0.04)</td>
</tr>
<tr>
<td>3/4</td>
<td>(\text{ND}_2)</td>
<td>1.62(0.11)</td>
<td>25.5(0.2)</td>
<td>1.66(0.05)</td>
</tr>
</tbody>
</table>

### CONCLUSIONS

In this work we obtained a coherent picture of anion reorientational dynamics in the lithium amide-borohydrides \(\text{Li}[\text{BH}_4]_{1-x}[\text{NH}_2]_x\) \((2/3 \leq x \leq 3/4)\) by means of QENS. The experiments have been carried out on two different time scales (∼1 ns on IN16B and ∼1 ps on FOCUS) and in the temperature range of 5–425 K. Deuterium labeling has clearly demonstrated that the quasielastic signal in the studied time and temperature range originates mainly from the \([\text{BH}_4]^-\) units, whereas the \([\text{NH}_2]^-\) reorientational dynamics appeared to be too slow to be resolved. To describe motions of the \([\text{BH}_4]^-\) tetrahedra, we have developed a detailed model supported by the MD simulations and based on \(C_3\)-reorientations with different jump rates for an extended temperature range. The proposed model was validated by the results for the well studied bulk LiBH₄ and allowed us to identify three processes in the lithium amide-borohydrides, which can be resolved in successive order as the temperature increases.

The fastest process with the activation energy of 3.6 kJ/mol was detected on FOCUS in the temperature range of 250–300 K. The geometry of this motion is connected with small amplitude jumps close to the equilibrium positions. We tentatively assign this process to the \([\text{BH}_4]^-\) tetrahedra. The second process is associated with the uniaxial \(C_3\) reorientation of the borohydride units. It characterizes the shape of the IFWS/EFWS measured in the temperature range 130–350 K on IN16B and is one of the main contributions resolved at higher temperatures on FOCUS. Predominant \(C_3\) reorientations were proved by our MD simulations and IR spectra. Finally, as temperature increases, the third relaxation component sets in, when the \([\text{BH}_4]^-\) tetrahedra start rotating around all four \(C_3\) axes. The temperature dependence of both the second and the third component of the best conducting sample \((\text{Li}[\text{BH}_4]_{1-x}[\text{NH}_2]_x)_{3/4}\) exhibits a pronounced change in the activation energy above the phase transition at 313 K, consistent with the ionic conductivity measurement. The analysis of the IFWS in an extended temperature range has shown that the same sample also features a broader distribution of activation energies as compared to the reference sample with \(x = 3/4\). Moreover, there is a clear onset of presumably diffusional motion of \([\text{BH}_4]^-\) in the high-temperature range. Thus, enhanced anion dynamics and rotational disorder are closely related to the high Li-conductivity realized in BH₄-rich \(\text{Li}[\text{BH}_4]_{1-x}[\text{NH}_2]_x\) compounds.
Our analysis approach is not limited to lithium amide-borohydrides and can be extended to a family of related compounds with reorientational processes on different time scales. We have demonstrated that sophisticated information on the geometry, relaxation times, and origin of dynamics can be reliably extracted from QENS spectra of multicomponent systems.

**ASSOCIATED CONTENT**

Supporting Information

The Supporting Information is available free of charge on the ACS Publications website at DOI: 10.1021/acs.jpcc.7b05651.

Jump models for reorientational dynamics of borohydride tetrahedra, time evolution of the spherical coordinates of hydrogen atoms in \([BH_4]^-\) and \([NH_4]^+\) as obtained from the MD calculations, and IR spectra in the wavenumber range 1000–1400 cm\(^{-1}\) (PDF)

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Notes

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