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Science Meeting, University of Geneva

Dark matter indirect detection limits including complete annihilation patterns

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Based on [2210.01220](#) [hep-ph]



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Département d'astronomie



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DARK MATTER

85% of the total matter of our Universe

Relic density observed experimentally by Planck:

$$\Omega_{\chi} h^2 \simeq 0.1200 \pm 0.0012$$

Ref: Ade et al. 2016, Astrophys. 594, A13

Its identification would **reveal new Physics**

Proving its existence and nature would **improve our understanding** of the Universe

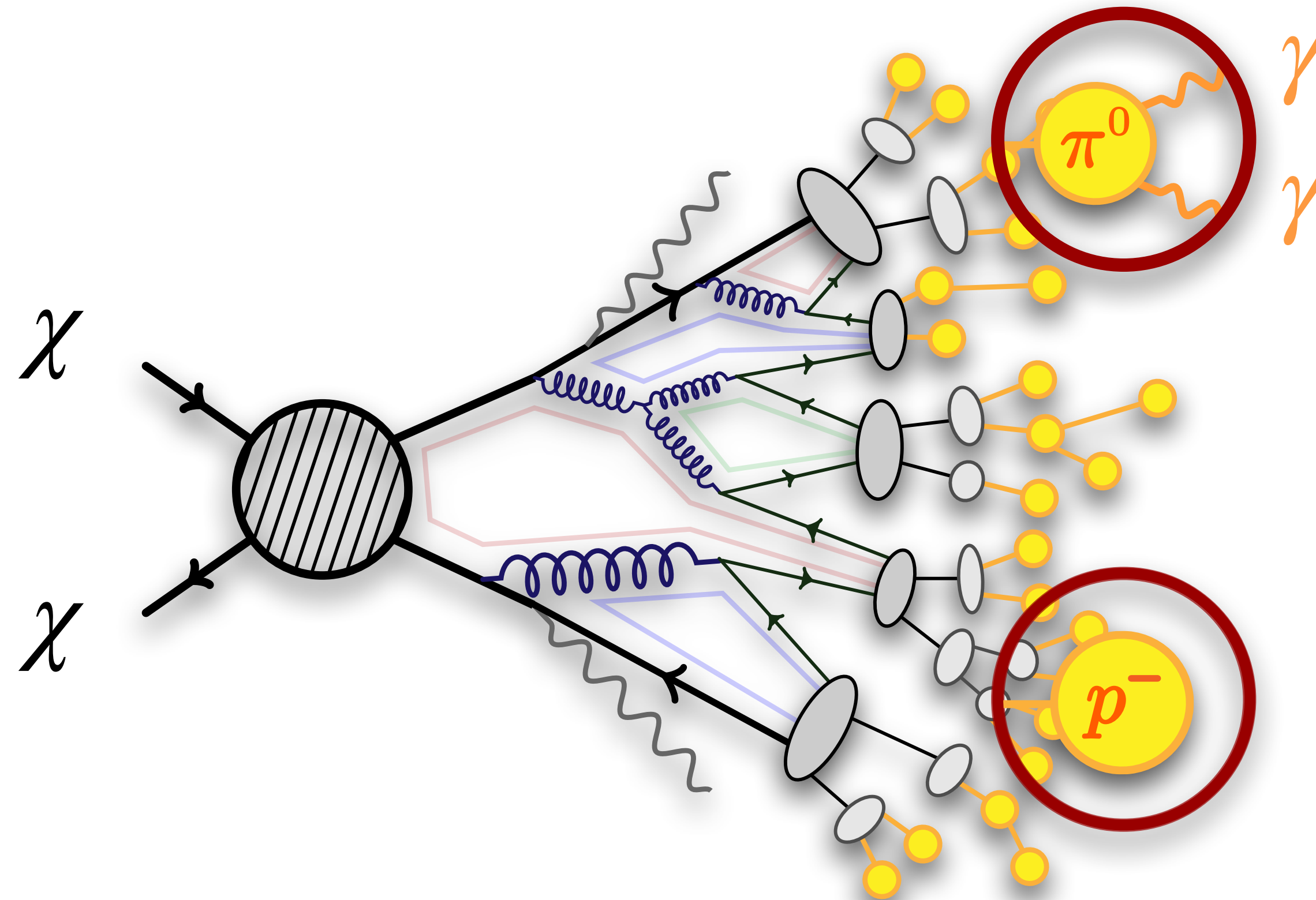
GOALS

Study of the impact of a more complete particle model

New prediction of DM upper limits with CTA mockdata of Sculptor

- **Previously:** use of individual annihilation channels
- **This work:** Combination of expertise (astro and particle physics) to include a more complex and more complete model

INDIRECT SEARCHES



Dark Matter (DM)
annihilation



Standard Model particles
(bosons, quarks, leptons)



Final state products
such as γ rays

INDIRECT SEARCHES

Expected γ -ray flux from DM annihilation

Astrophysical
J factor

$$\frac{d\Phi(\langle\sigma v\rangle, J)}{dE} = \underbrace{\frac{1}{4\pi} \frac{\langle\sigma v\rangle}{2m_\chi^2}}_{\text{Particle Physics factor}} \sum_f \text{BR}_f \frac{dN_f}{dE} \times \underbrace{\int_{\Delta\Omega} \int_{\text{los}} \rho_{\text{DM}}^2 ds d\Omega}_{\text{Astrophysical J factor}}$$

Particle Physics
factor

where

$\langle\sigma v\rangle$ = annihilation cross-section

m_χ = DM particle mass

BR_f = branching ratio

dN_f/dE = differential spectrum

ρ_{DM} = DM density

STATISTICAL ANALYSIS

LOG-LIKELIHOOD RATIO TEST STATISTICS

$$\Lambda = -2 \ln \frac{\mathcal{L}_{H_0}}{\mathcal{L}_{H_1}} = -2 \ln \frac{\mathcal{L}(\langle \sigma v \rangle_0 | \hat{N}_B, \hat{J})}{\mathcal{L}(\langle \hat{\sigma} v \rangle, \hat{N}_B, \hat{J})}$$

Constrained
minimization

Global
minimization

Ref: Cowan et al, 2010
Eur.Phys.J.C71:1554,2011

$\langle \sigma v \rangle$

Parameter of interest

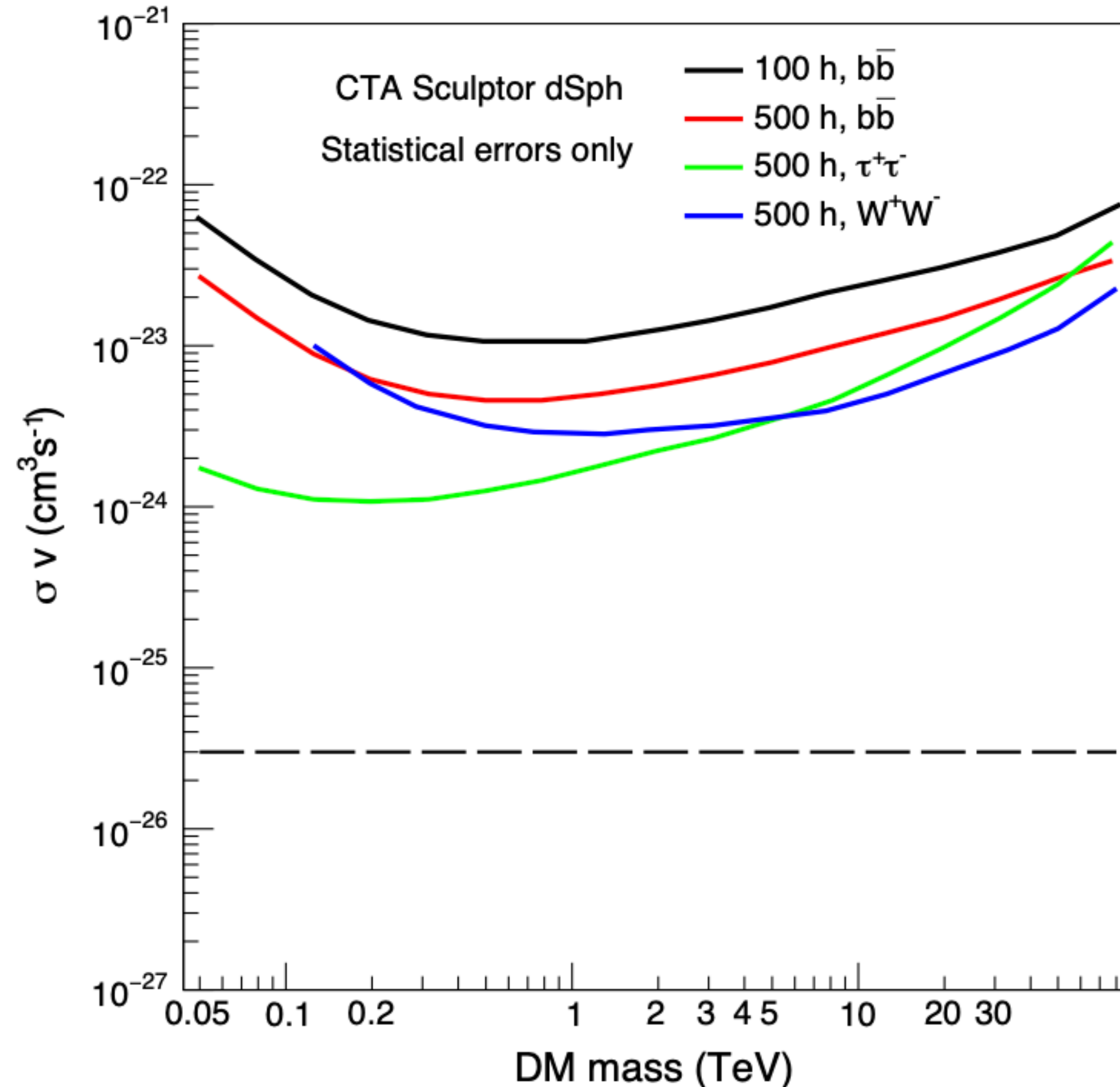
N_B, J

Nuisance parameters

Λ

2.71 at 95% Confidence Level

UPPER LIMITS

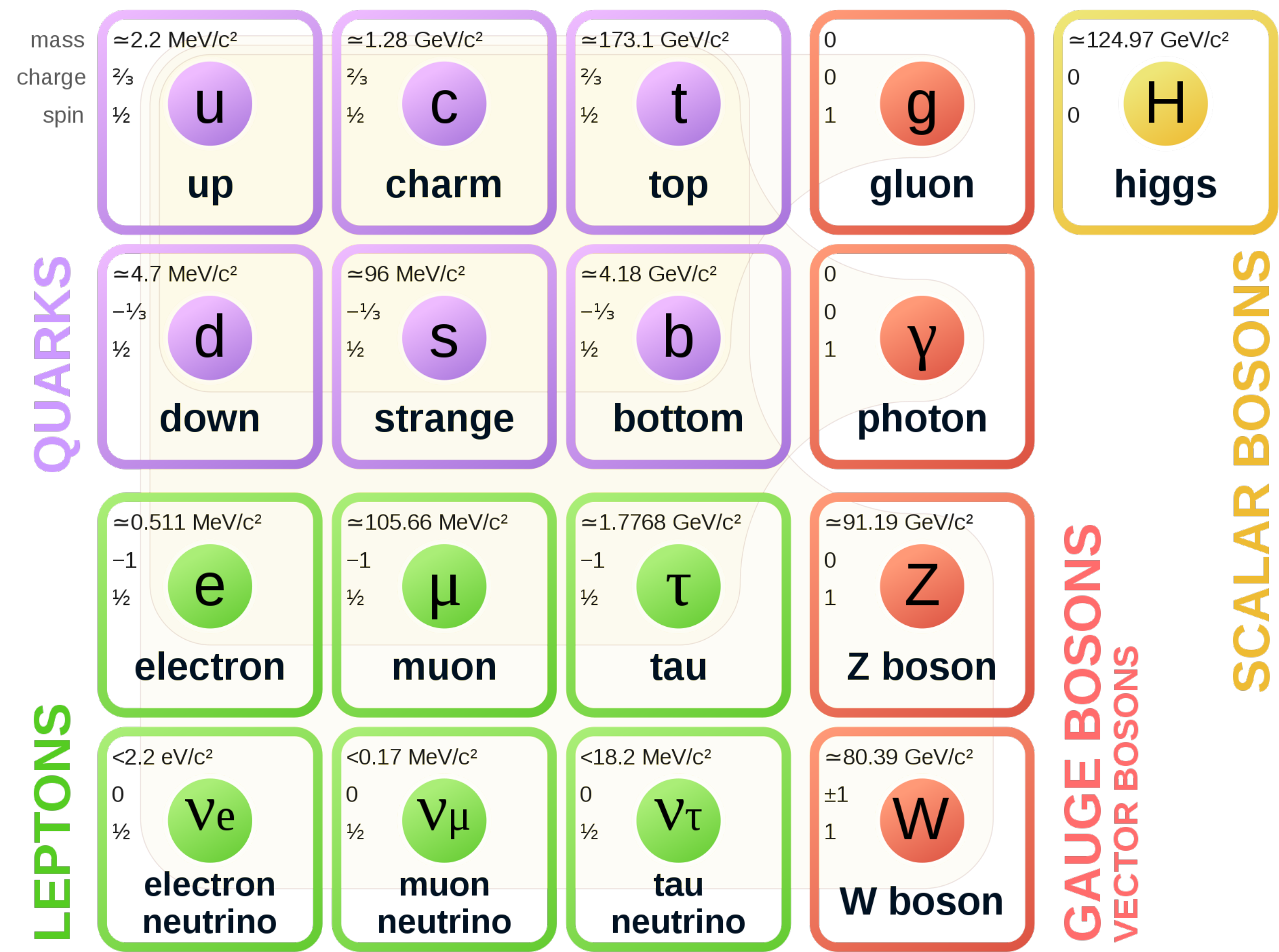


- Each annihilation channel **treated independently**
- Corresponding to a **branching ratio of 100%**
- **Simplest** model possible where all DM particles annihilate through the same channel

WHAT IF

We change the particle physics model?

STANDARD MODEL...



en.wikipedia.org/wiki/Standard_Model

STANDARD MODEL...

QUARKS	<div> <div>mass</div> <div>charge</div> <div>spin</div> </div> <div> $\approx 2.2 \text{ MeV}/c^2$ $\frac{2}{3}$ $\frac{1}{2}$ </div> <div> u up </div>	<div> <div>mass</div> <div>charge</div> <div>spin</div> </div> <div> $\approx 1.28 \text{ GeV}/c^2$ $\frac{2}{3}$ $\frac{1}{2}$ </div> <div> c charm </div>	<div> <div>mass</div> <div>charge</div> <div>spin</div> </div> <div> $\approx 173.1 \text{ GeV}/c^2$ $\frac{2}{3}$ $\frac{1}{2}$ </div> <div> t top </div>	<div> <div>mass</div> <div>charge</div> <div>spin</div> </div> <div> 0 0 1 </div> <div> g gluon </div>	<div> <div>mass</div> <div>charge</div> <div>spin</div> </div> <div> $\approx 124.97 \text{ GeV}/c^2$ 0 0 </div> <div> H higgs </div>
	<div> <div>mass</div> <div>charge</div> <div>spin</div> </div> <div> $\approx 4.7 \text{ MeV}/c^2$ $-\frac{1}{3}$ $\frac{1}{2}$ </div> <div> d down </div>	<div> <div>mass</div> <div>charge</div> <div>spin</div> </div> <div> $\approx 96 \text{ MeV}/c^2$ $-\frac{1}{3}$ $\frac{1}{2}$ </div> <div> s strange </div>	<div> <div>mass</div> <div>charge</div> <div>spin</div> </div> <div> $\approx 4.18 \text{ GeV}/c^2$ $-\frac{1}{3}$ $\frac{1}{2}$ </div> <div> b bottom </div>	<div> <div>mass</div> <div>charge</div> <div>spin</div> </div> <div> 0 0 1 </div> <div> γ photon </div>	
	<div> <div>mass</div> <div>charge</div> <div>spin</div> </div> <div> $\approx 0.511 \text{ MeV}/c^2$ -1 $\frac{1}{2}$ </div> <div> e electron </div>	<div> <div>mass</div> <div>charge</div> <div>spin</div> </div> <div> $\approx 105.66 \text{ MeV}/c^2$ -1 $\frac{1}{2}$ </div> <div> μ muon </div>	<div> <div>mass</div> <div>charge</div> <div>spin</div> </div> <div> $\approx 1.7768 \text{ GeV}/c^2$ -1 $\frac{1}{2}$ </div> <div> τ tau </div>	<div> <div>mass</div> <div>charge</div> <div>spin</div> </div> <div> $\approx 91.19 \text{ GeV}/c^2$ 0 1 </div> <div> Z Z boson </div>	
LEPTONS	<div> <div>mass</div> <div>charge</div> <div>spin</div> </div> <div> $< 2.2 \text{ eV}/c^2$ 0 $\frac{1}{2}$ </div> <div> ν_e electron neutrino </div>	<div> <div>mass</div> <div>charge</div> <div>spin</div> </div> <div> $< 0.17 \text{ MeV}/c^2$ 0 $\frac{1}{2}$ </div> <div> ν_μ muon neutrino </div>	<div> <div>mass</div> <div>charge</div> <div>spin</div> </div> <div> $< 18.2 \text{ MeV}/c^2$ 0 $\frac{1}{2}$ </div> <div> ν_τ tau neutrino </div>	<div> <div>mass</div> <div>charge</div> <div>spin</div> </div> <div> $\approx 80.39 \text{ GeV}/c^2$ ±1 1 </div> <div> W W boson </div>	

en.wikipedia.org/wiki/Standard_Model

Dark matter in the Universe...?

Neutrino masses...?

Hierarchy problem...?

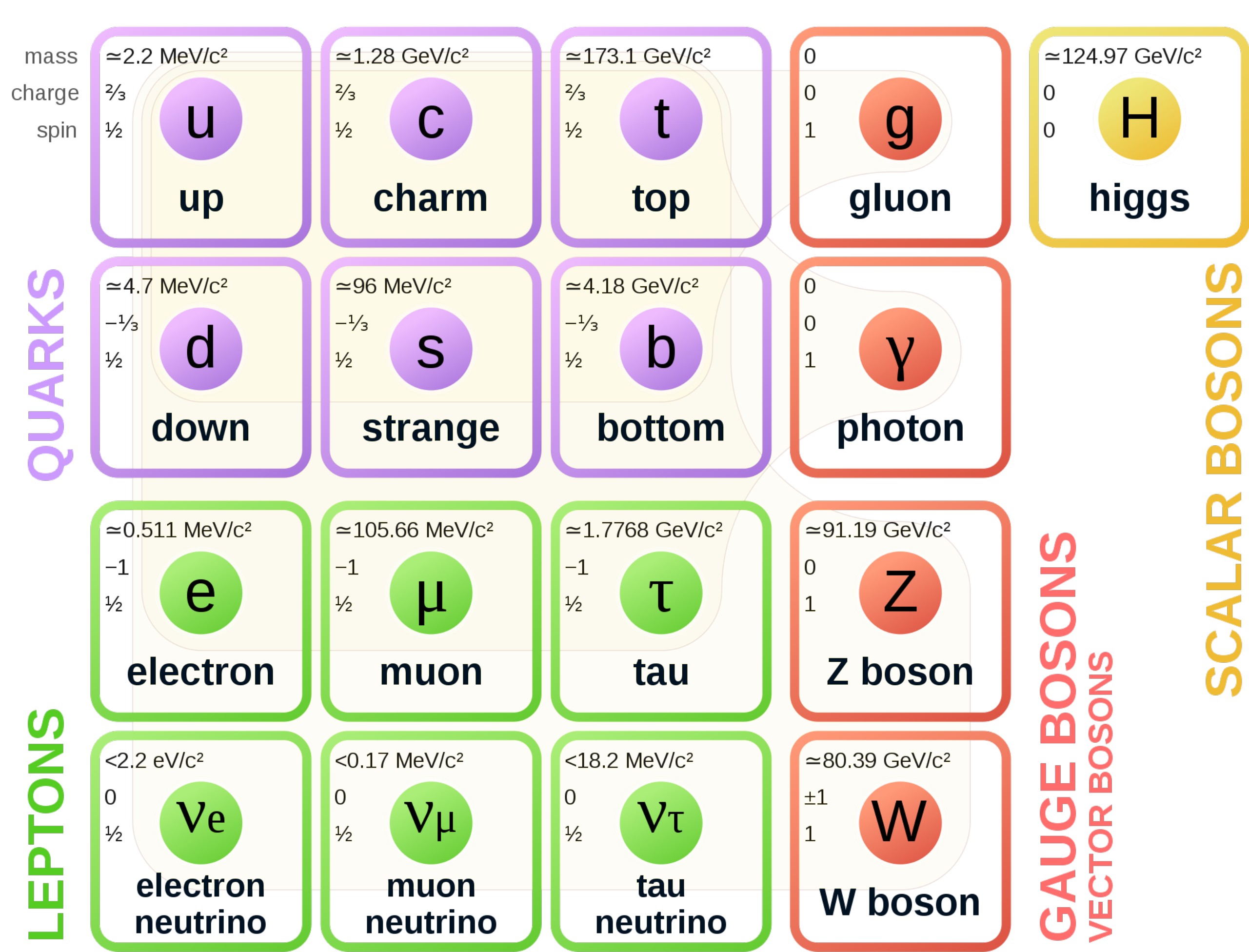
Gauge coupling unification...?

Gravity...?

Lepton-flavour non-universality...?

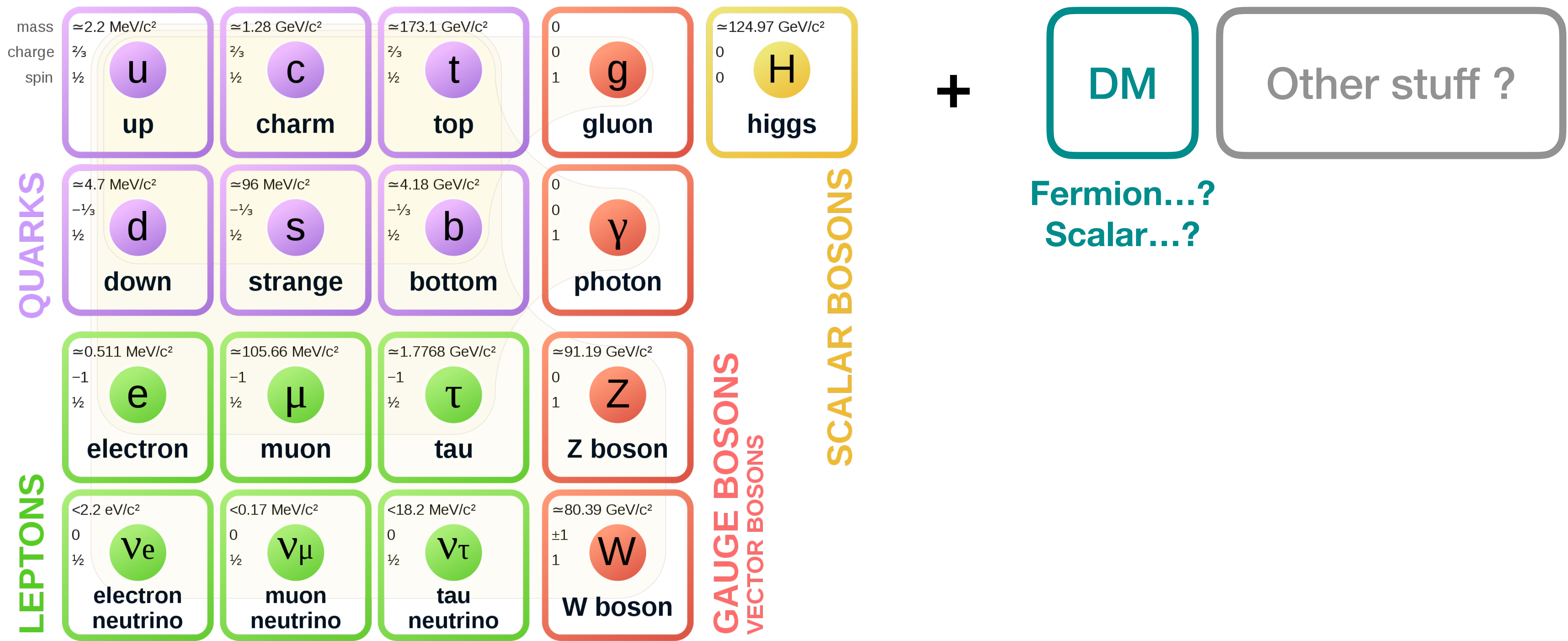
Flavour problem...?

STANDARD MODEL... AND BEYOND



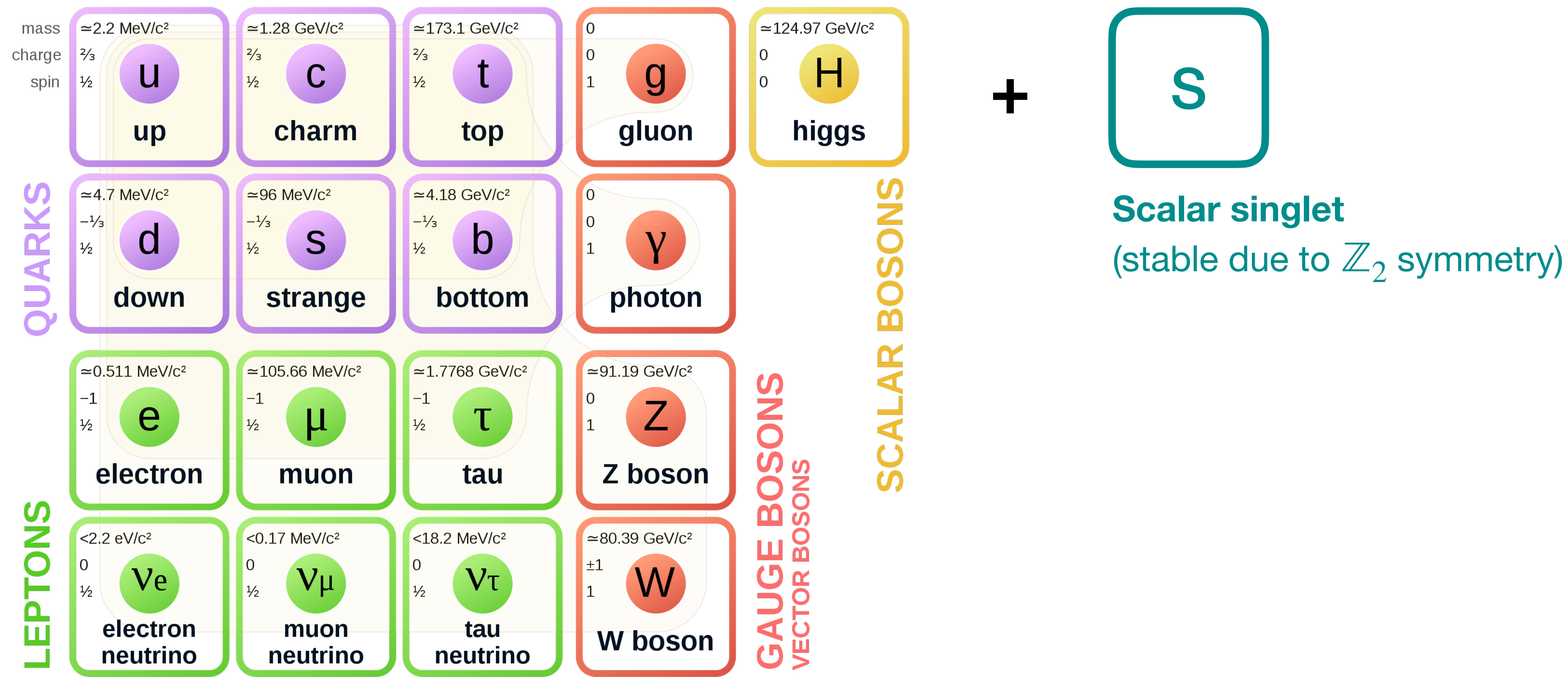
Dark matter in the Universe...?

STANDARD MODEL... AND BEYOND



en.wikipedia.org/wiki/Standard_Model

SINGLET SCALAR DARK MATTER



en.wikipedia.org/wiki/Standard_Model

SINGLET SCALAR DARK MATTER

Standard model extended by an additional scalar field (DM)

$$V_{\text{scalar}} \supset 2\lambda_H v^2 h^2 + \underbrace{\frac{1}{2}\mu_S^2 S^2}_{\text{DM mass}} + \underbrace{\frac{1}{4}\lambda_{SH} v^2 S^2 + \frac{1}{4}\lambda_{SH} v S^2 h + \lambda_{SH} S^2 h^2}_{\text{DM – Higgs interaction ("Higgs portal")}}$$

$$m_S^2 = \mu_S^2 + \frac{1}{2}\lambda_{SH} v^2$$

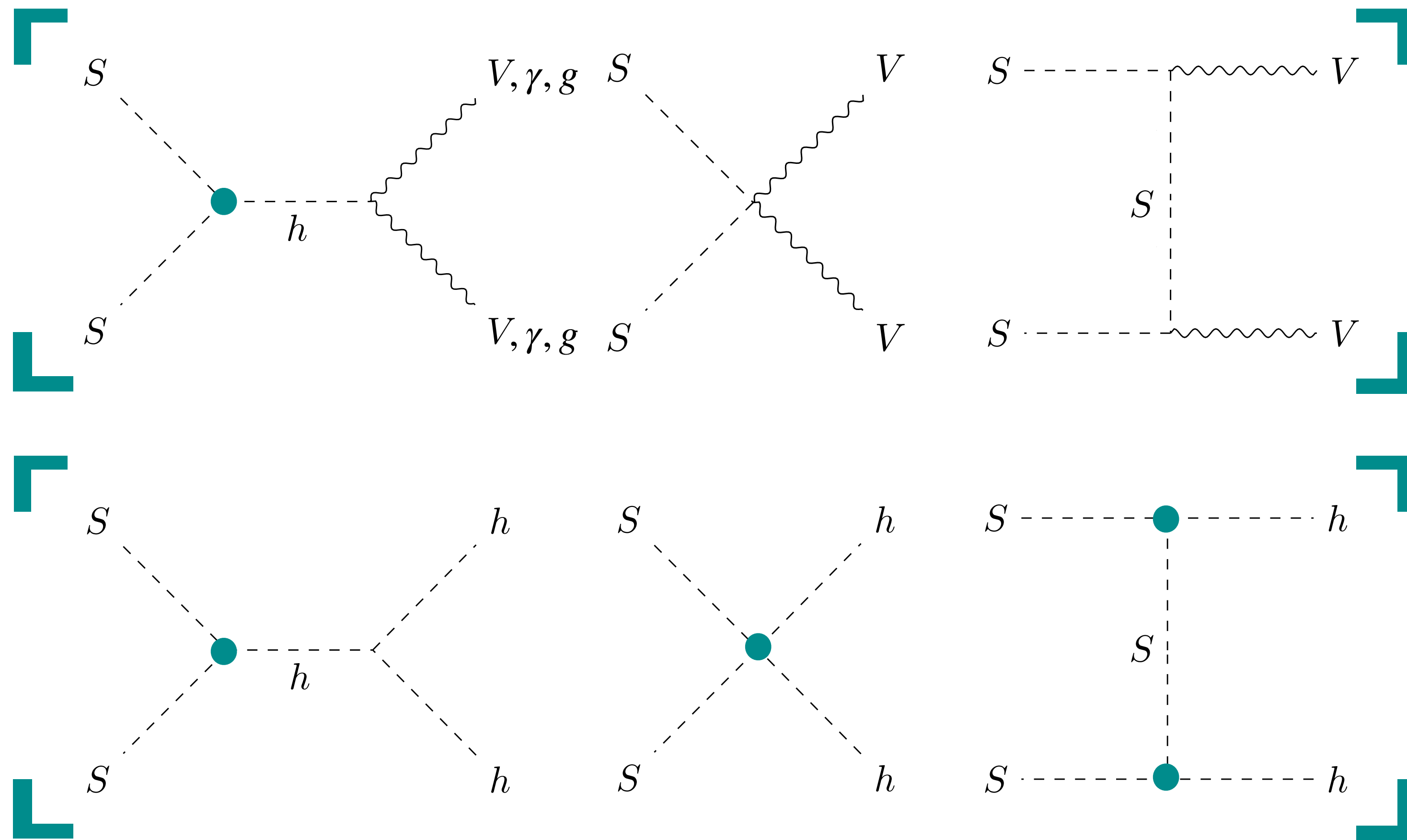
Phenomenology governed by

m_S (DM mass)

λ_{SH} (DM coupling)

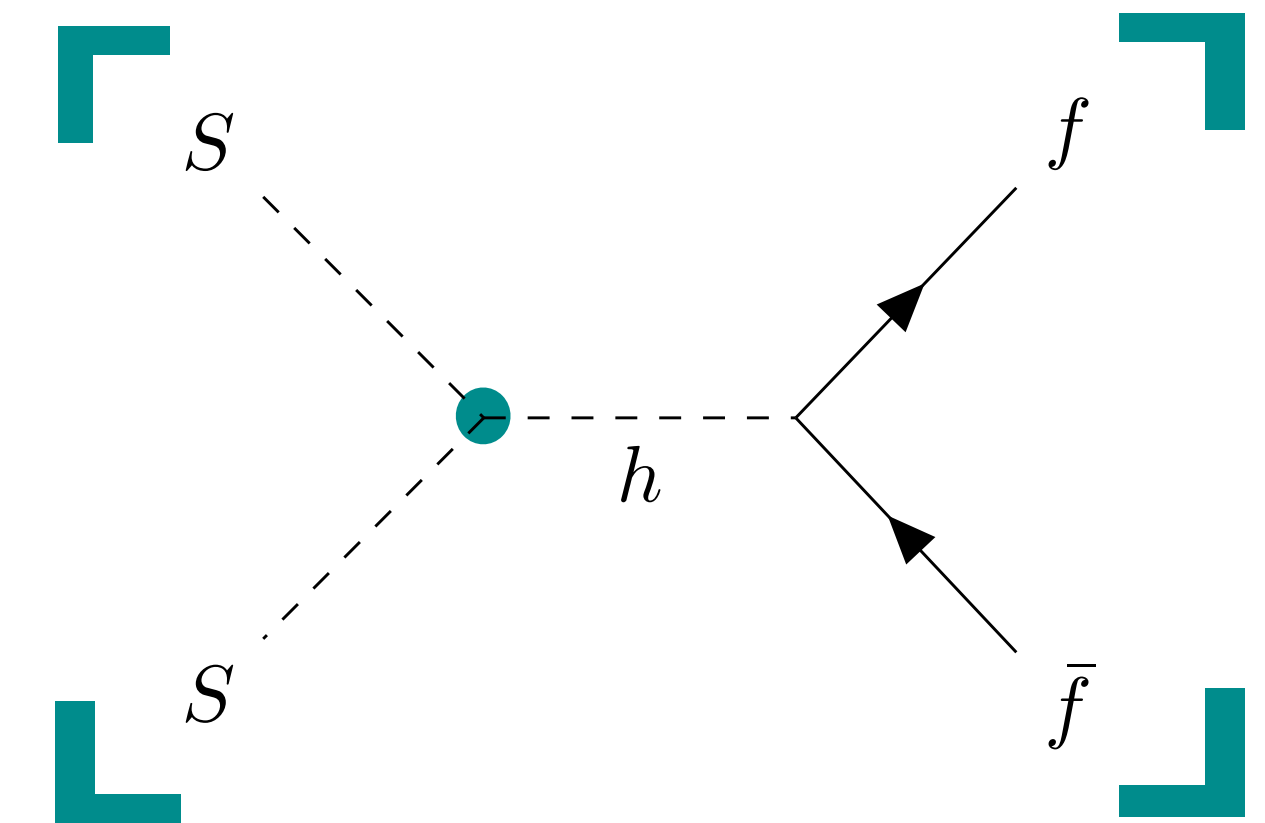
SINGLET SCALAR DARK MATTER

Possible dark matter annihilation channels (DM relic density + indirect detection)



Gauge boson final states

$$V = Z^0, W^\pm$$



Quark or lepton final states

$$f = u, d, c, s, b, t, e, \mu, \tau$$

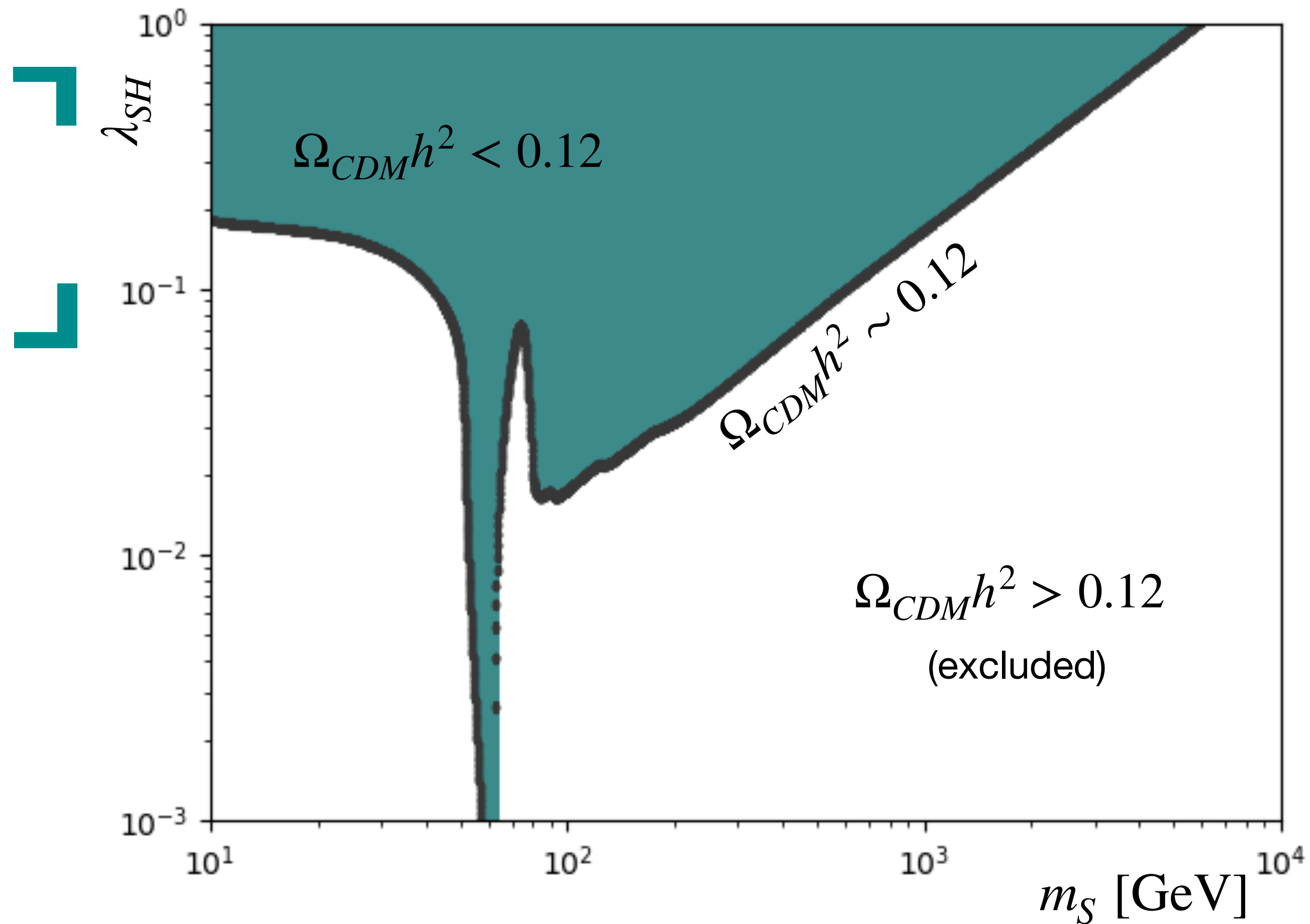
Higgs boson final states

SINGLET SCALAR DARK MATTER

DM coupling vs DM mass

Relic density and branching ratio grid
computed using micrOMEGAs

Ref: Bélanger, Pukhov et al. 2003 - 2022



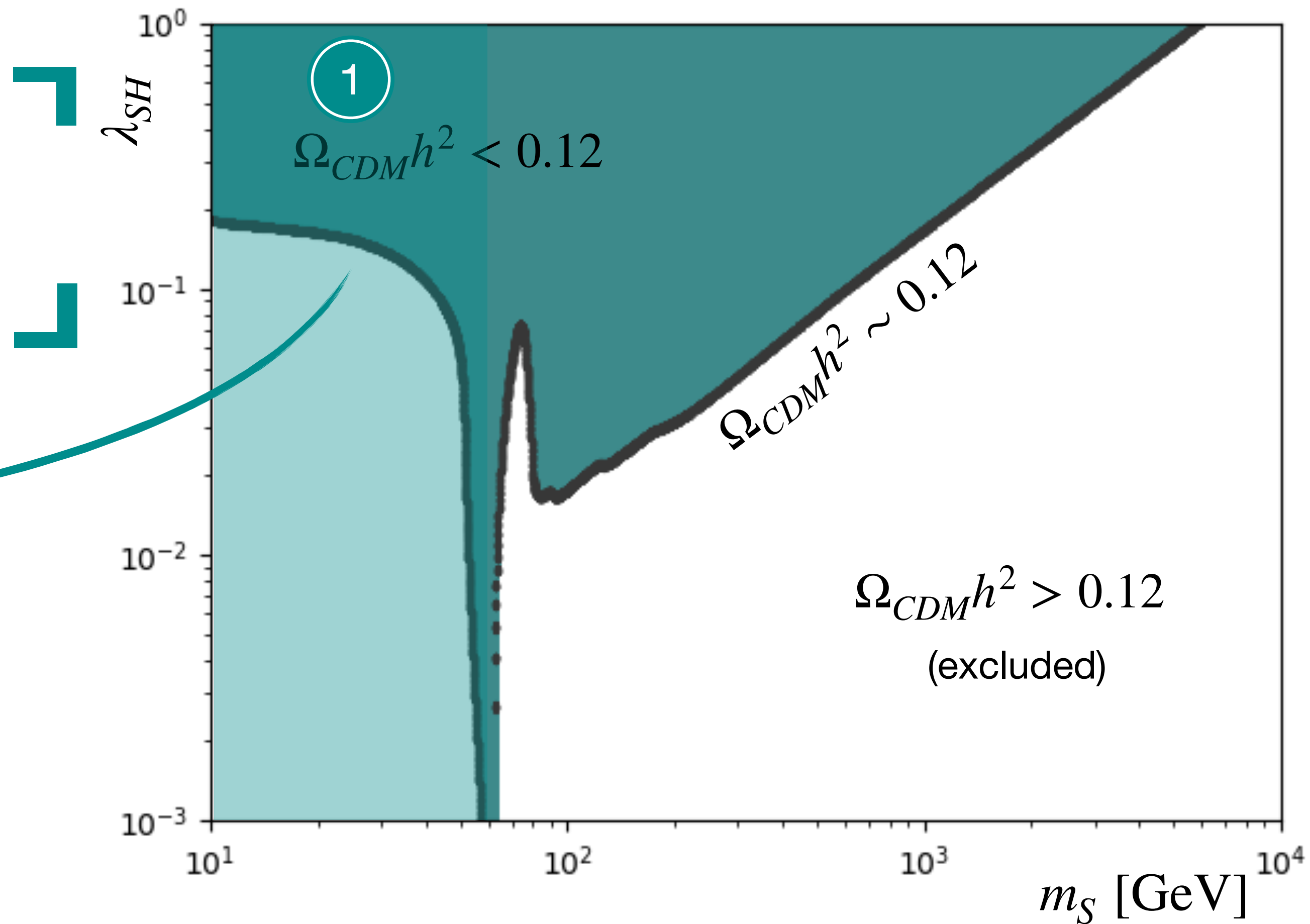
SINGLET SCALAR DARK MATTER

DM coupling vs DM mass

Relic density and branching ratio grid
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Ref: Bélanger, Pukhov et al. 2002 - 2022

$SS \rightarrow b\bar{b} \quad \sim 75 - 85 \%$
 $SS \rightarrow \tau^+\tau^- \quad \sim 7 - 10 \%$
 $SS \rightarrow c\bar{c} \quad \sim 3 - 4 \%$
 $SS \rightarrow gg \quad \sim 3 - 15 \%$



SINGLET SCALAR DARK MATTER

DM coupling vs DM mass

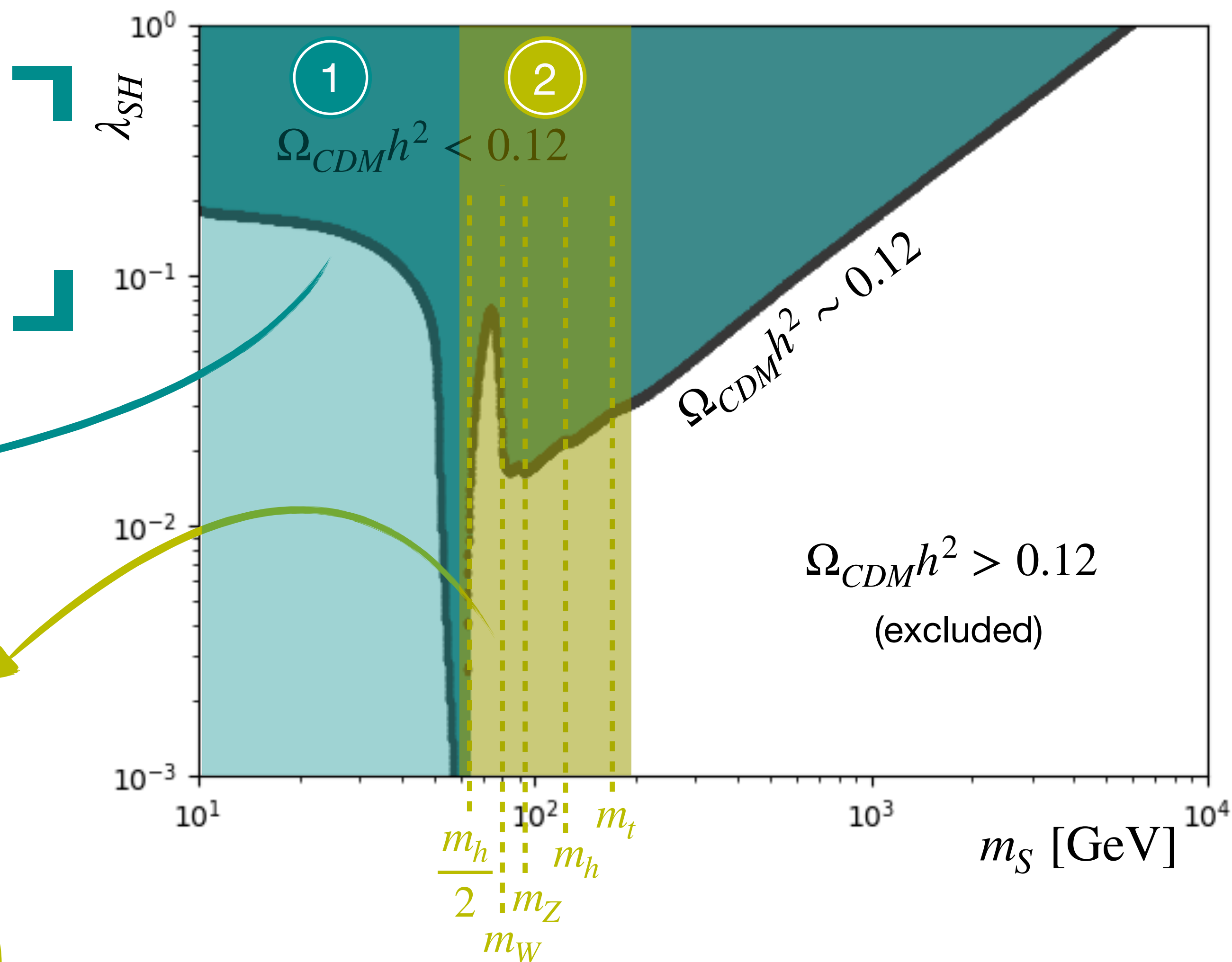
Relic density and branching ratio grid
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$$\begin{aligned} SS &\rightarrow b\bar{b} && \sim 75 - 85 \% \\ SS &\rightarrow \tau^+\tau^- && \sim 7 - 10 \% \\ SS &\rightarrow c\bar{c} && \sim 3 - 4 \% \\ SS &\rightarrow gg && \sim 3 - 15 \% \end{aligned}$$

Region of frequent change
of the dominant annihilation channel

New annihilation channels open,
Higgs resonance at $m_h/2$



SINGLET SCALAR DARK MATTER

DM coupling vs DM mass

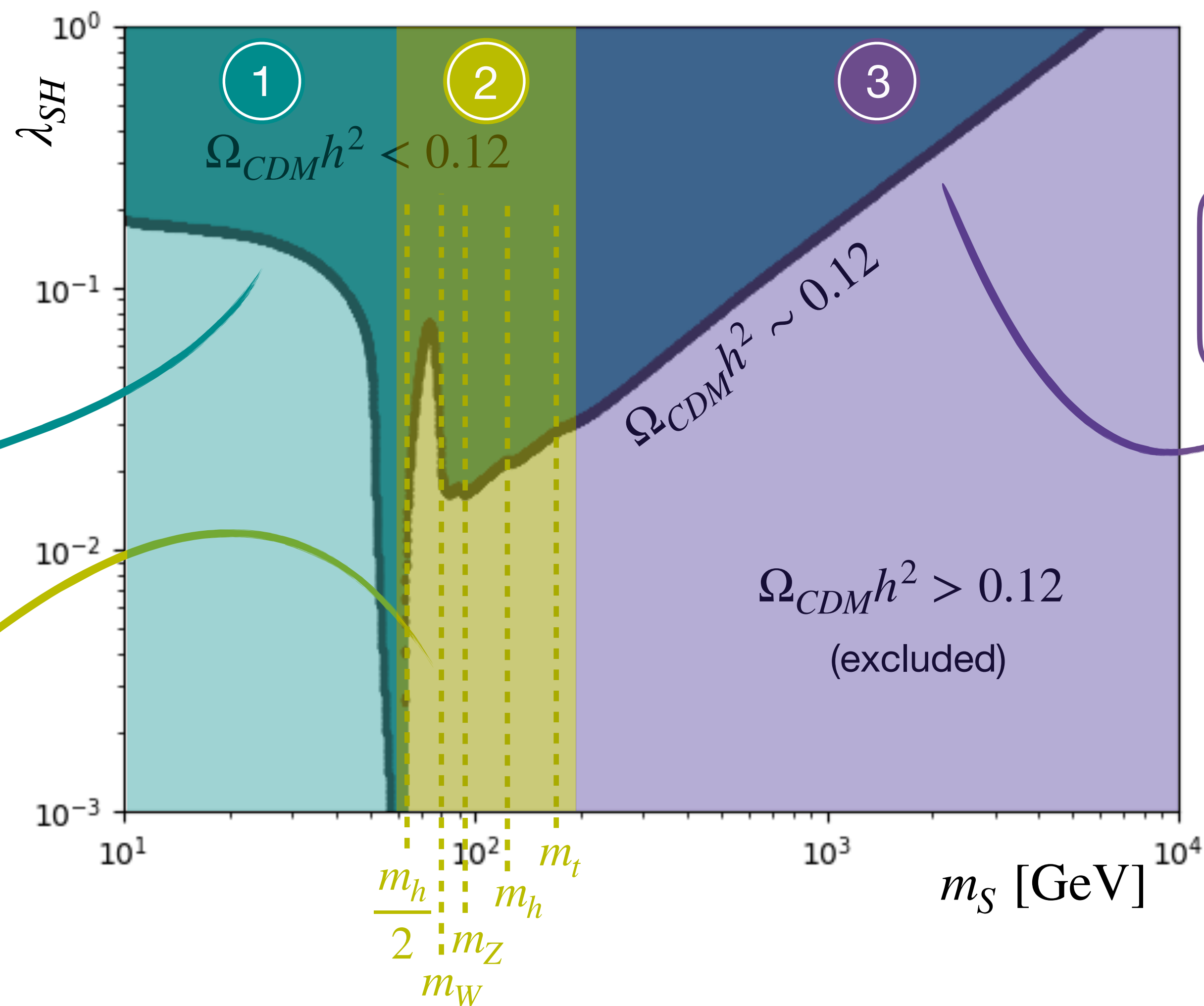
Relic density and branching ratio grid
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Region of frequent change
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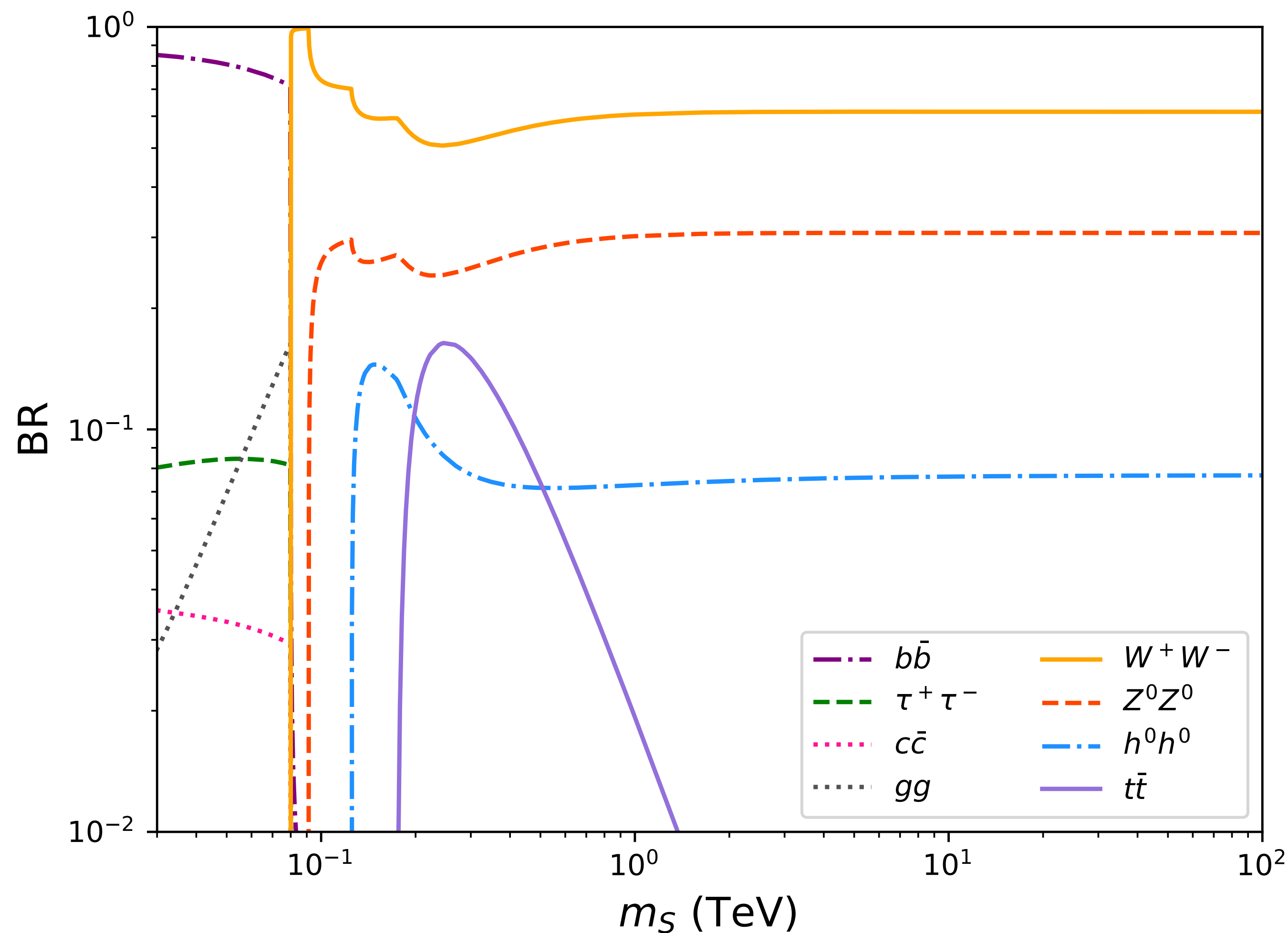


$$\begin{aligned} SS &\rightarrow W^+W^- && \sim 62 \% \\ SS &\rightarrow Z^0Z^0 && \sim 30 \% \\ SS &\rightarrow h^0h^0 && \sim 8 \% \end{aligned}$$

→ All annihilation channels **treated all together** whose **branching ratio varies** with respect to the DM mass

SINGLET SCALAR DARK MATTER

Branching Ratio according to the relic density constraint



None of the annihilation channels are at 100% branching ratio over the full mass range

For the remaining part, we focus on the case where the relic density constraint is satisfied (black line in previous figure):

$$\Omega_\chi h^2 \simeq 0.1200 \pm 0.0012$$

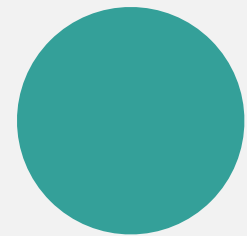
Even in such a simple setup, the
“100% hypothesis” is not justified...

More complex models invoke an even
richer phenomenology...

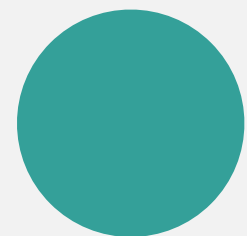
TARGET SOURCE



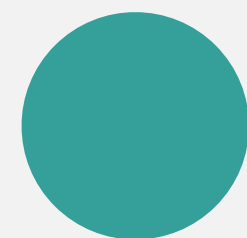
Dwarf galaxy selected for the
CTA dark matter program



South Hemisphere
 $l = 287.62^\circ, b = -83.16^\circ$



J factor
 $\text{Log}_{10} J_{0.1} = 18.3 \pm 0.3$



Ref: Bonnivard et al, 2015 ApJ 808 L3

Sculptor

Mock data prepared
with Gammapy 0.18.2



Simulated events for 500h of
observation at 20° zenith angle




Background only



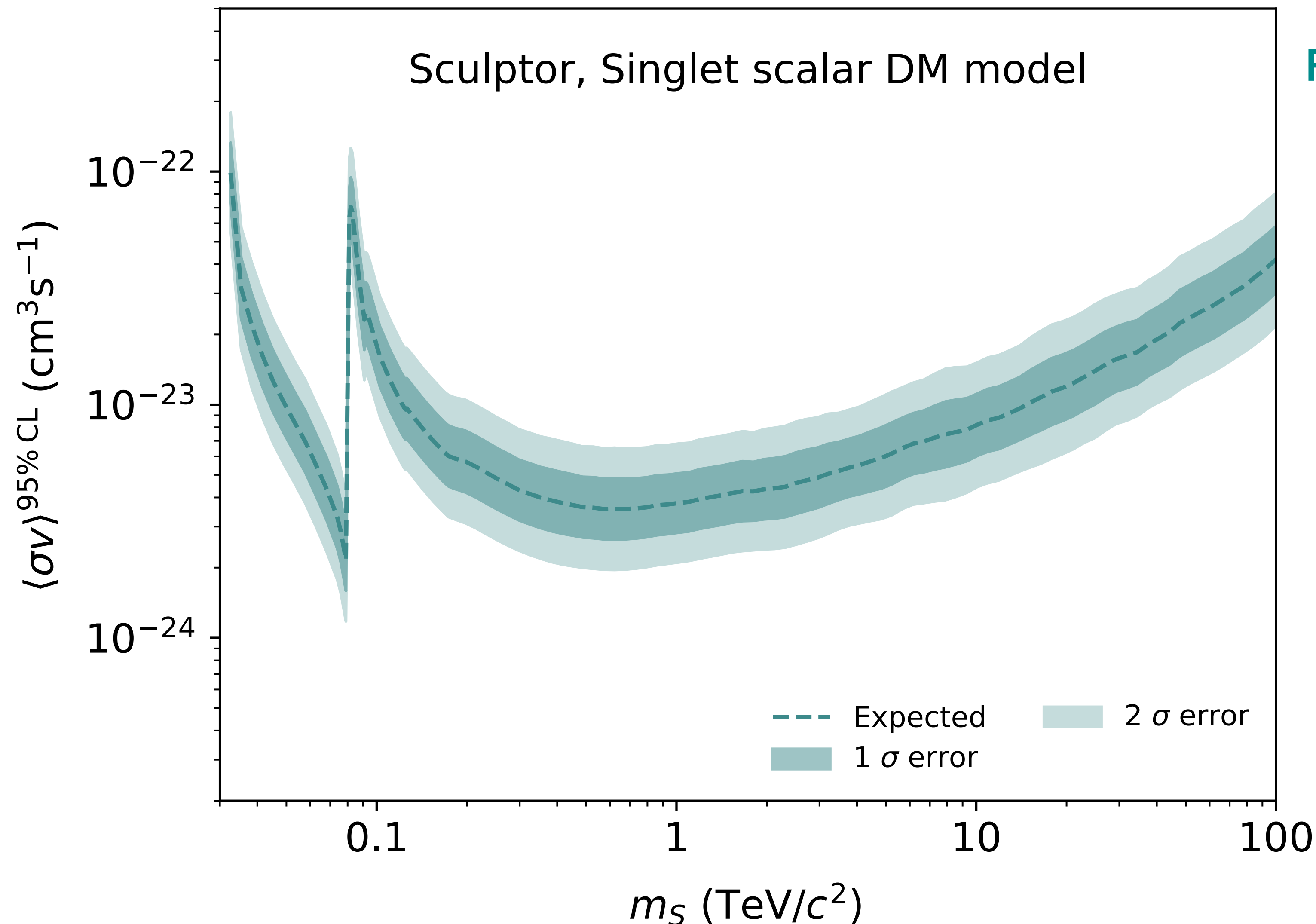
NEW UPPER LIMITS

Computation of the predicted DM cross section
VS
DM particle mass

- ① **Expected** limits - Sample of **500 Poisson realizations** of the simulated background events
 - ② **Mean expected limits**
Mean of the derived $\langle\sigma v\rangle$ distribution
 - Statistical uncertainty bands**
Standard deviation at 1 and 2σ
- 
- ```
graph TD; A[1 Expected limits - Sample of 500 Poisson realizations of the simulated background events] --> B[2 Mean expected limits
Mean of the derived $\langle\sigma v\rangle$ distribution]; A --> C[Statistical uncertainty bands
Standard deviation at 1 and 2σ];
```



# RESULTS



## Predicted upper limit and uncertainties

Assuming a singlet scalar DM model  
 $\gamma$ -ray spectra taken from Cirelli et al.  
*JCAP* 03 (2011) 051

## Inflection point

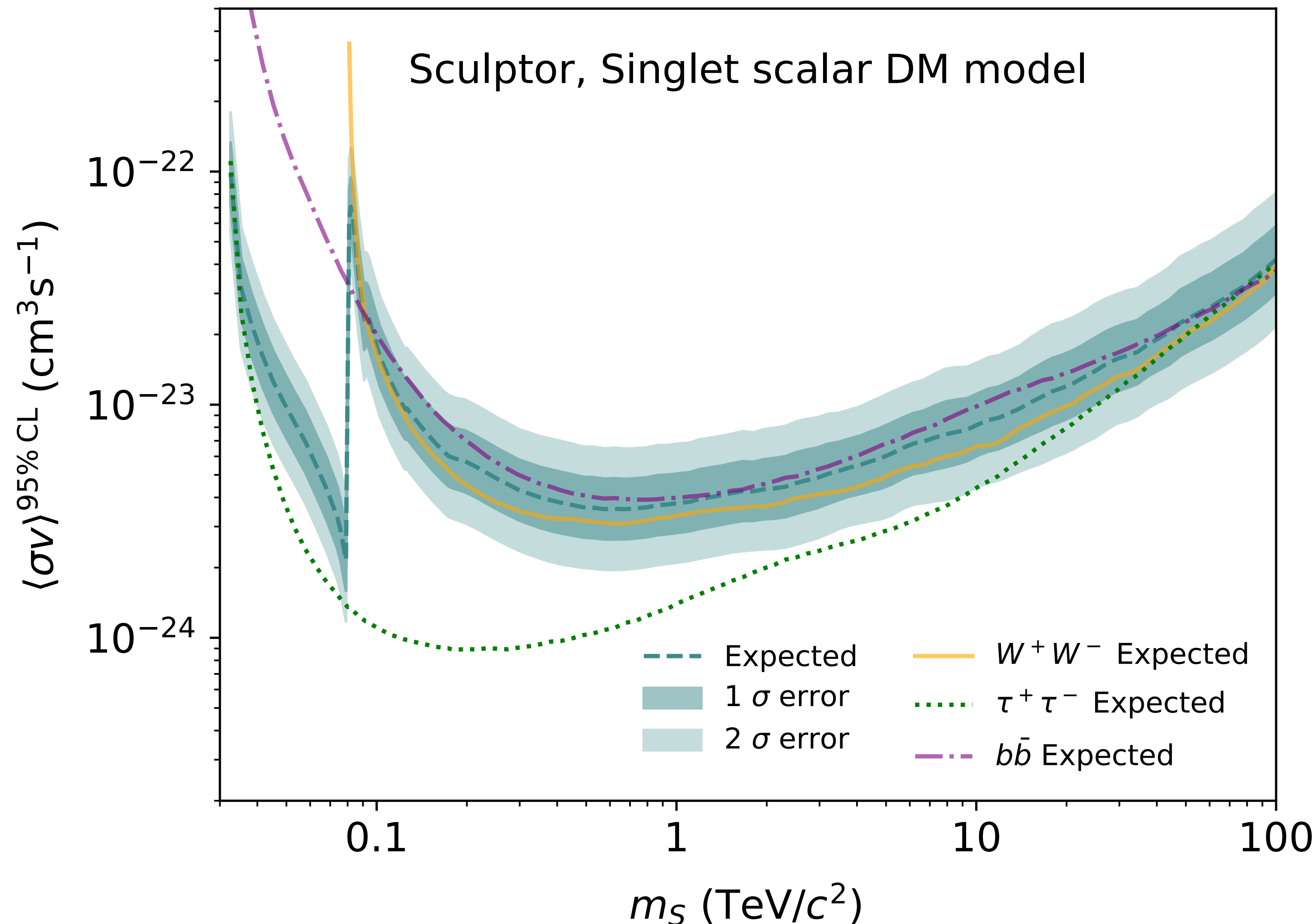
Due to the Higgs resonance

## Sudden increase

Due to the opening of the WW channel

# COMPARISONS

## SINGLET SCALAR MODEL VS 100% $W^+W^-$



### Below the $W$ mass

No upper limit for 100%  $WW$  since the  $WW$  channel **does not exist**

### Above the $W$ mass

**Additional contributions:**  $ZZ$ ,  $hh$ ,  $tt$  which produce less  $\gamma$  than the  $WW$  channel

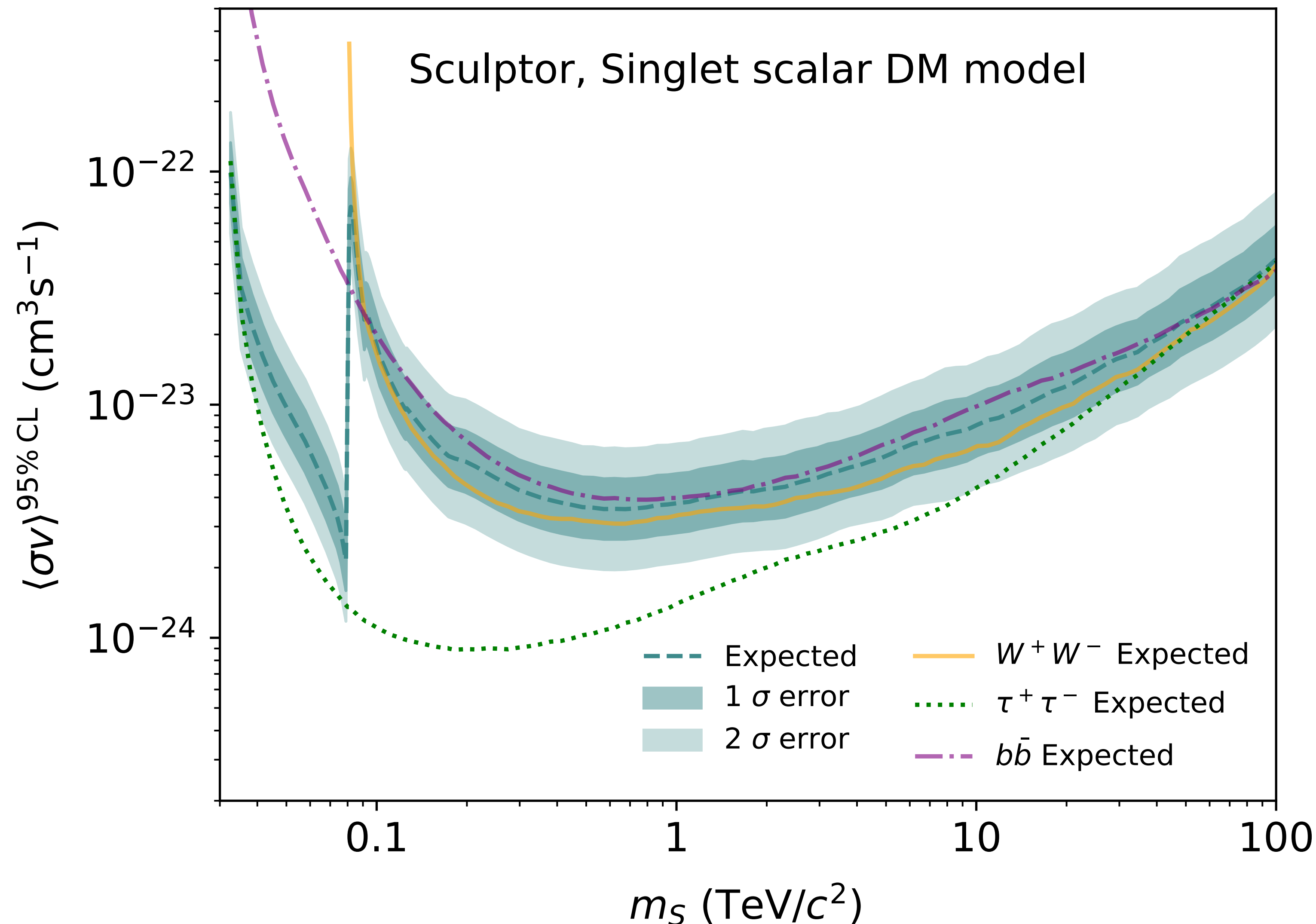
### Above 1 TeV

**Stability** with  $\sim 62\%$   $WW$  -  $30\%$   $ZZ$  -  $8\%$   $hh$

**More conservative limit** with the singlet scalar DM model

# COMPARISONS

SINGLET SCALAR MODEL  
VS  
100%  $\tau^+\tau^-$



100%  $\tau^+\tau^-$  produces more  $\gamma$  rays  
Leads to **more constraining** upper limits

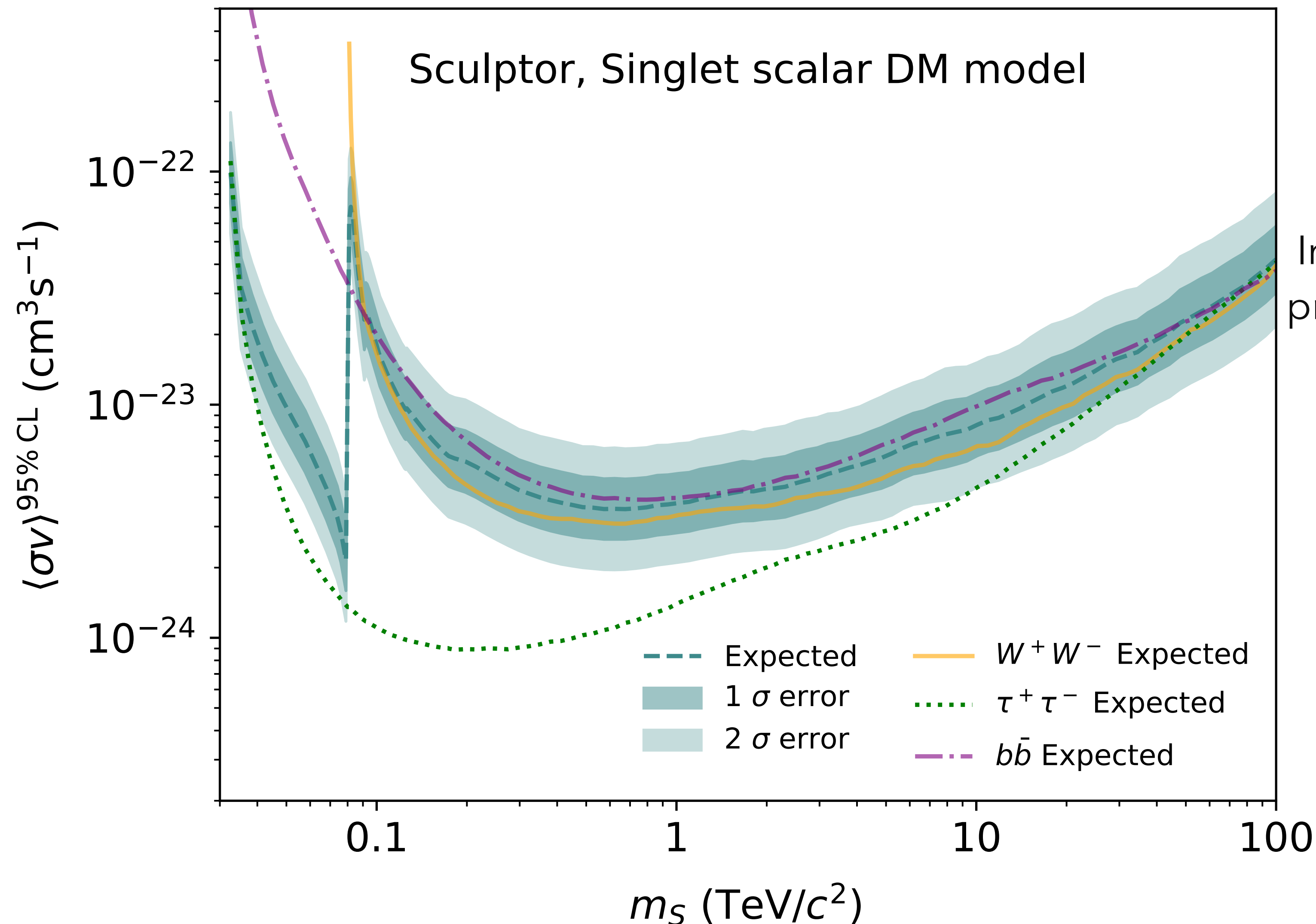
However, in the singlet scalar model,  
**this  $\tau^+\tau^-$  channel is never dominant**

**100%  $\tau^+\tau^-$**  = over estimation of the  
contribution



# COMPARISONS

## SINGLET SCALAR MODEL VS 100% $b\bar{b}$



### Below the W mass

Singlet scalar **much more constraining**

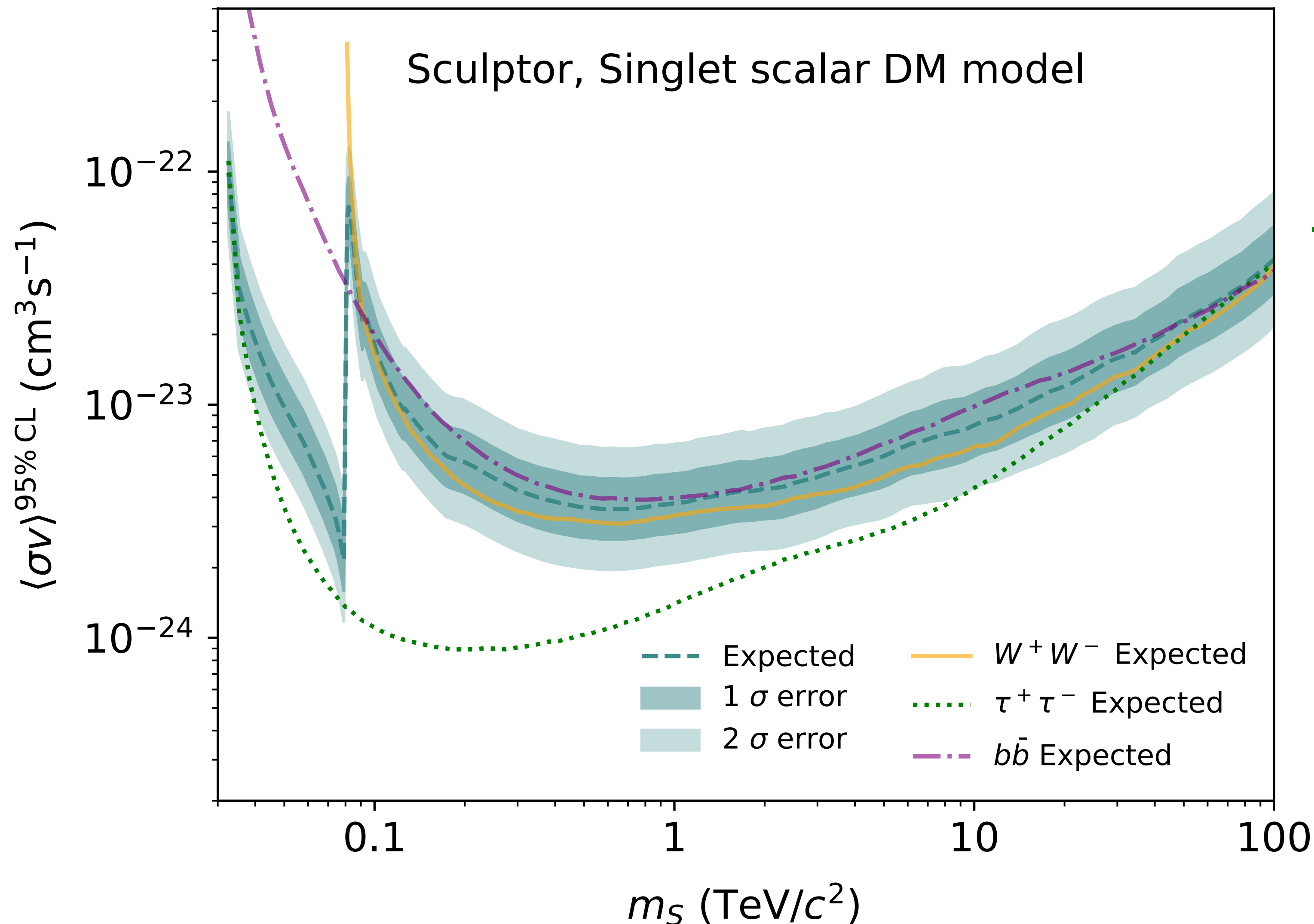
Important difference with 100%  $b\bar{b}$  due to the presence of the subdominant channels  $\tau^+\tau^-$ ,  $c\bar{c}$ , and  $g\bar{g}$

### Above the W mass

**$b\bar{b}$  suppressed** in the singlet scalar  
 **$b\bar{b}$  produces less  $\gamma$**  than the 4 contributing channels  $WW$ ,  $ZZ$ ,  $hh$ , and  $t\bar{t}$  (between the  $t$  mass and 1 TeV)

**More constraining limit** with the singlet scalar DM model

# RELATIVE ERRORS



## WW

- Ranges between **-22% and -6%**
- Reaches values **beyond 100%** for masses at the W mass threshold

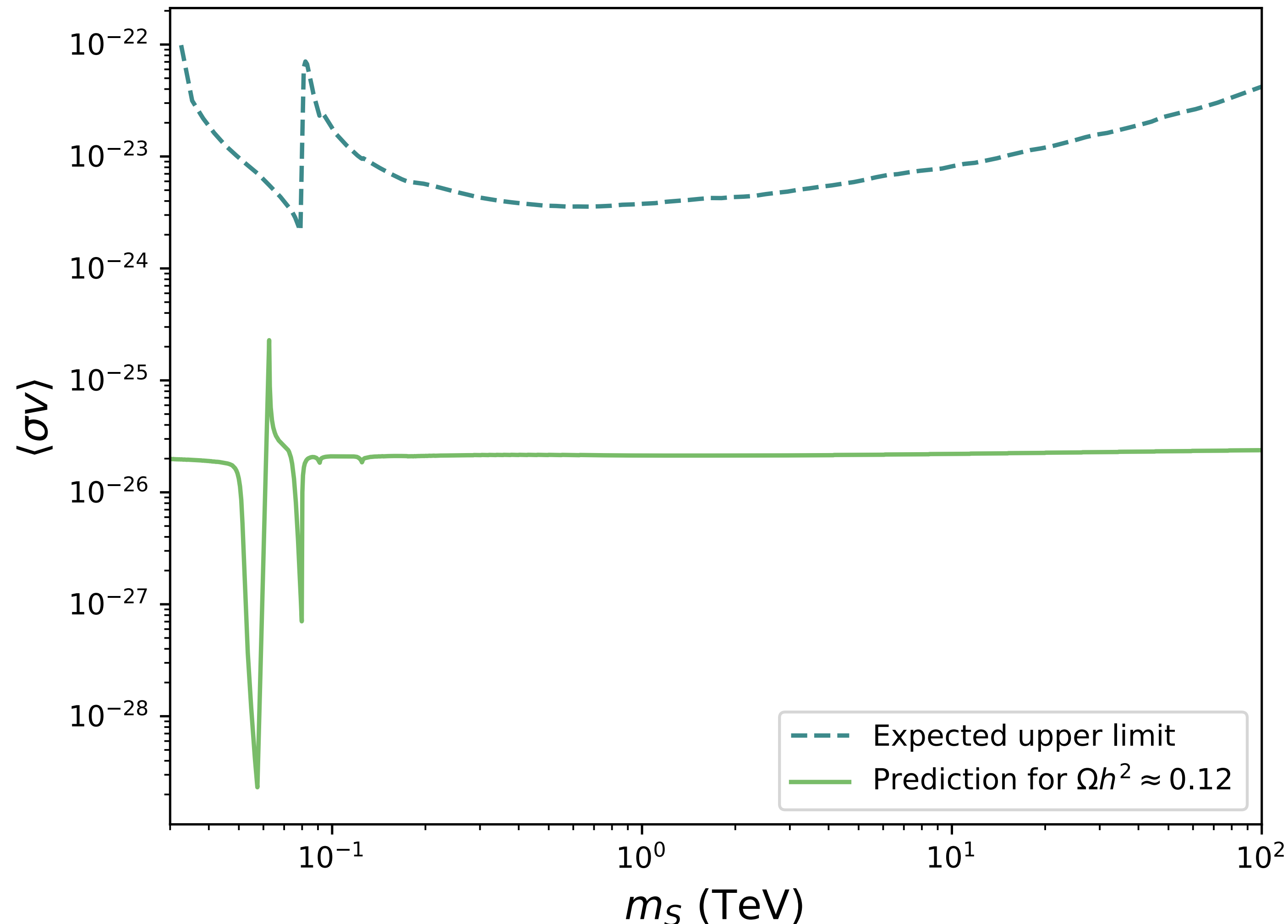
## $\tau^+\tau^-$

- Ranges between **-65% and +12%** below the W mass threshold
- Around the W mass threshold **reaches -98%**
- Then decreases **to -3% at 100 TeV**

## $b\bar{b}$

- **In the order of 1000%** below the W mass threshold
- Then **drops to -56%** at the W mass threshold
- Then remains in the range of **-10% to +38%** after the threshold

# EXCLUSION



Singlet scalar model **not excluded** by DM indirect detection

However, **resonance and kinematical thresholds** influence the exclusion curve together with the predicted annihilation cross-section

Generally, such fluctuations might lead to exclusion...

# CONCLUSION & PERSPECTIVES

- Use of a **more complex and more complete** particle physics model
- Takes into account the **full phenomenology** with all annihilation channels at once
- **Change of dominant annihilation channel(s)** along with the DM particle mass
- **Affects** the predicted upper limits
- Feature can be **expected in any particle physics model**
- Derivation of a **predicted upper limit and its  $1\sigma$  and  $2\sigma$  uncertainty bands**
- Particle physics model could be used as well **on the future data of CTA**
- Paper submitted to JCAP & available on **[2210.01220](#)** [hep-ph]





# Thanks for your attention



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# BACKUP



# STATISTICAL ANALYSIS

Total likelihood

$$\mathcal{L}(\langle\sigma v\rangle, N_B, J) = \prod_{i=1} \underbrace{\mathcal{L}_{P_i}(\langle\sigma v\rangle, N_{B_i}, J | N_{\text{ON}_i}, N_{\text{OFF}_i}, \alpha)}_{\text{Poisson likelihood}} \underbrace{\mathcal{L}^J(J | \bar{J}, \sigma_J)}_{\text{Log-normal likelihood}}$$

Poisson likelihood

Log-normal  
likelihood

Poisson likelihood for each energy bin

$$\mathcal{L}_i^P = \underbrace{\frac{(N_{S_i} + N_{B_i})^{N_{\text{ON}_i}}}{N_{\text{ON}_i}!} e^{-(N_{S_i} + N_{B_i})}}_{\text{ON REGION}} \cdot \underbrace{\frac{(\alpha N_{B_i})^{N_{\text{OFF}_i}}}{N_{\text{OFF}_i}!} e^{-\alpha N_{B_i}}}_{\text{OFF REGION}}$$

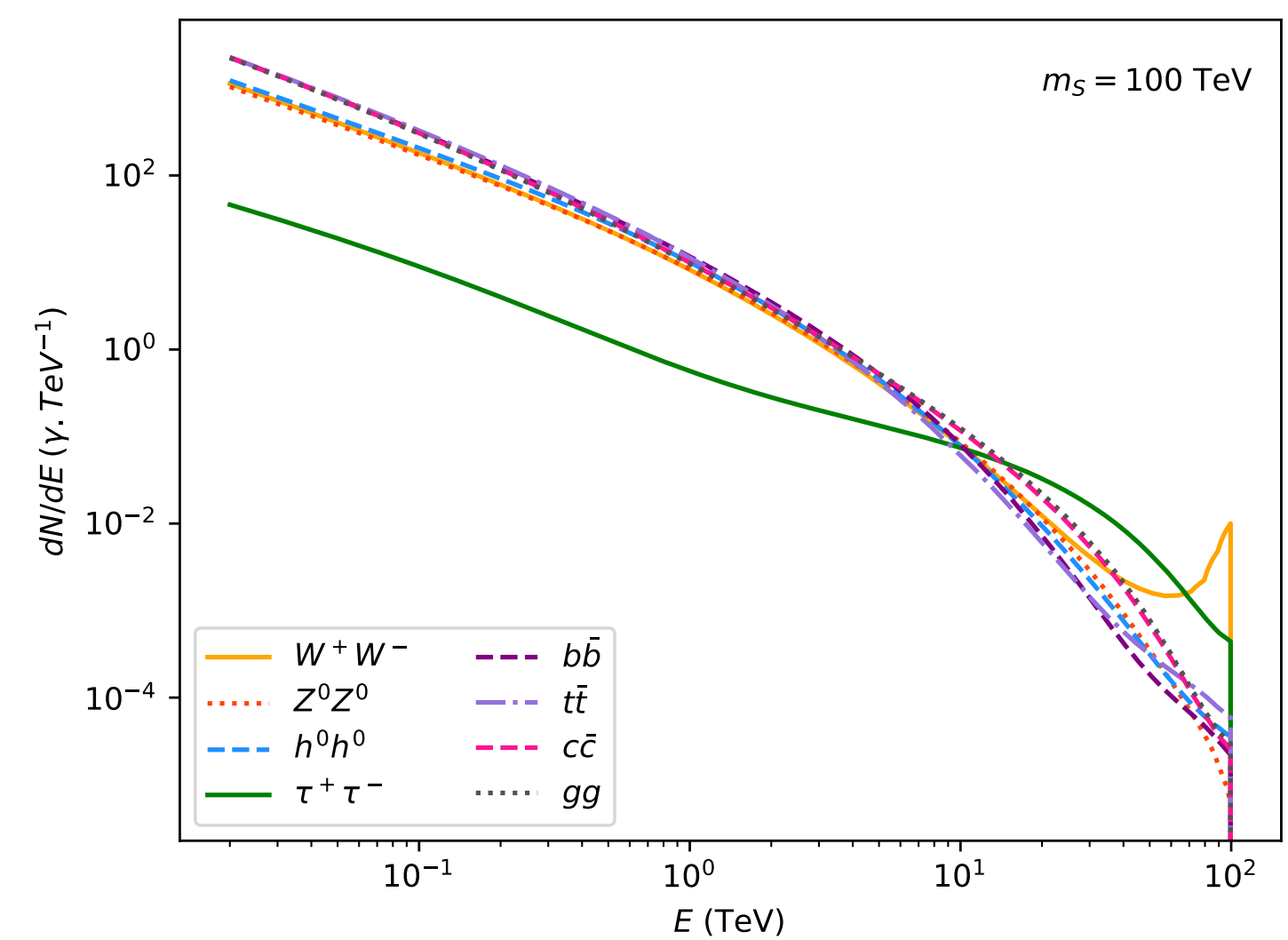
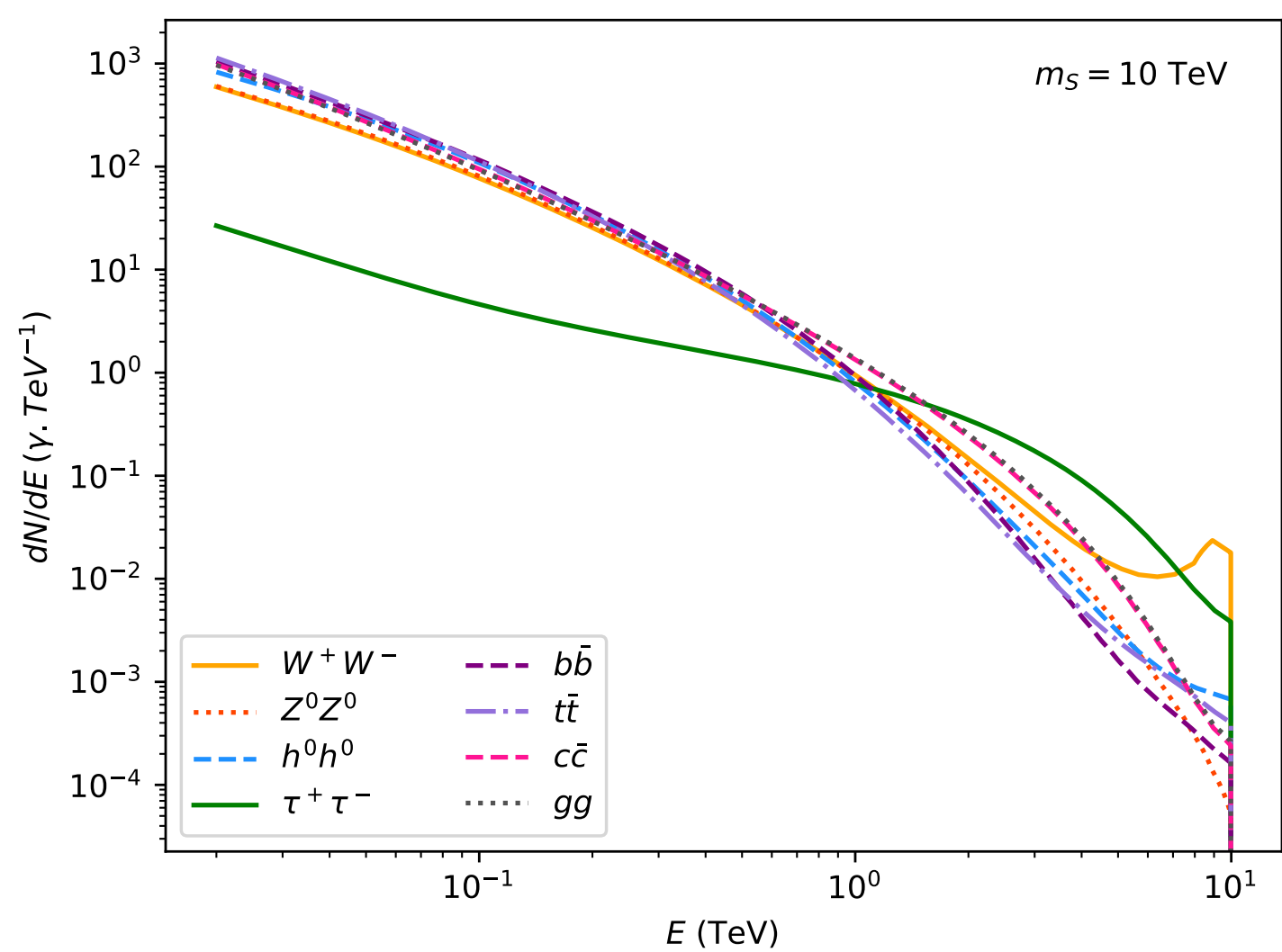
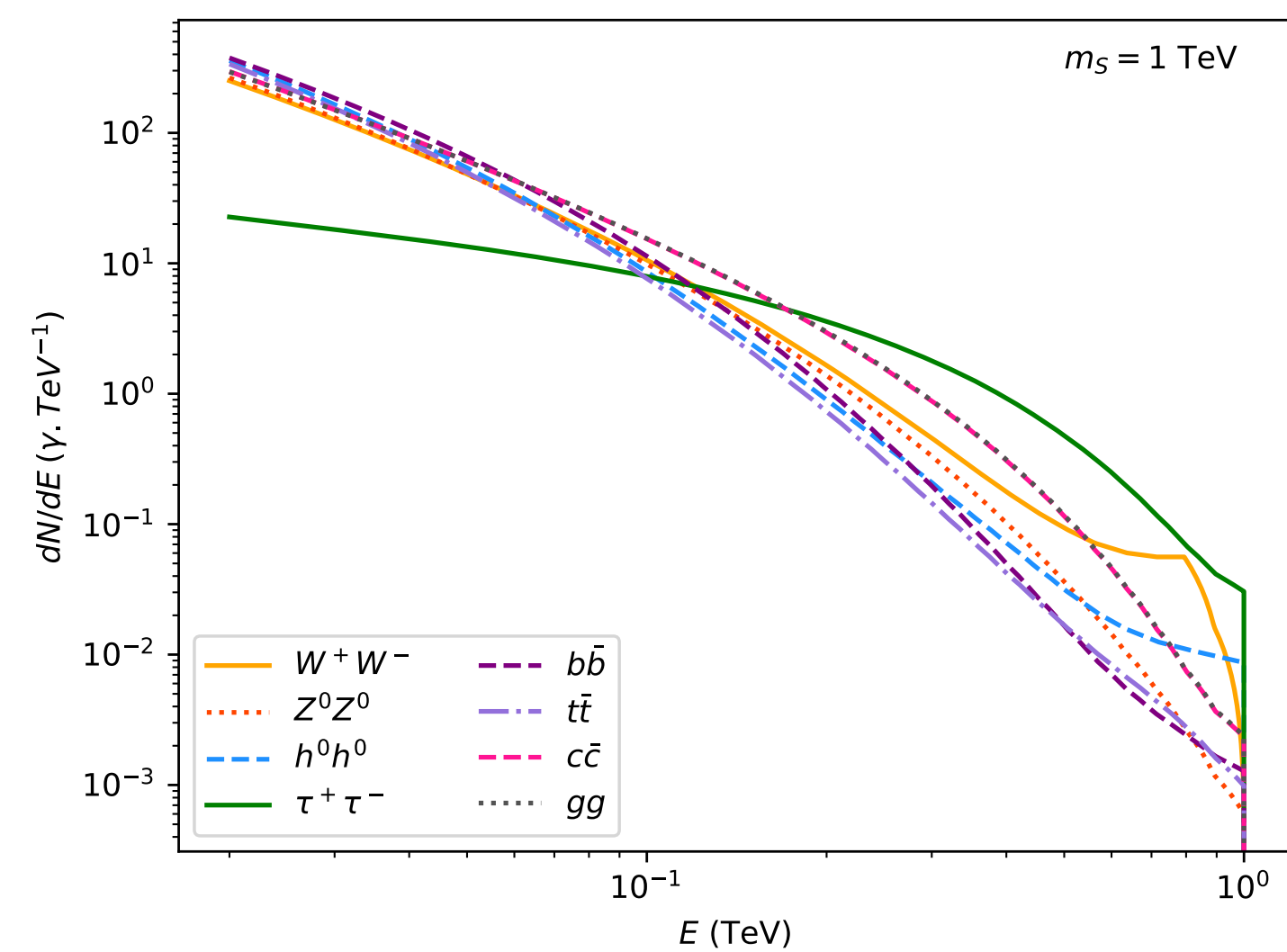
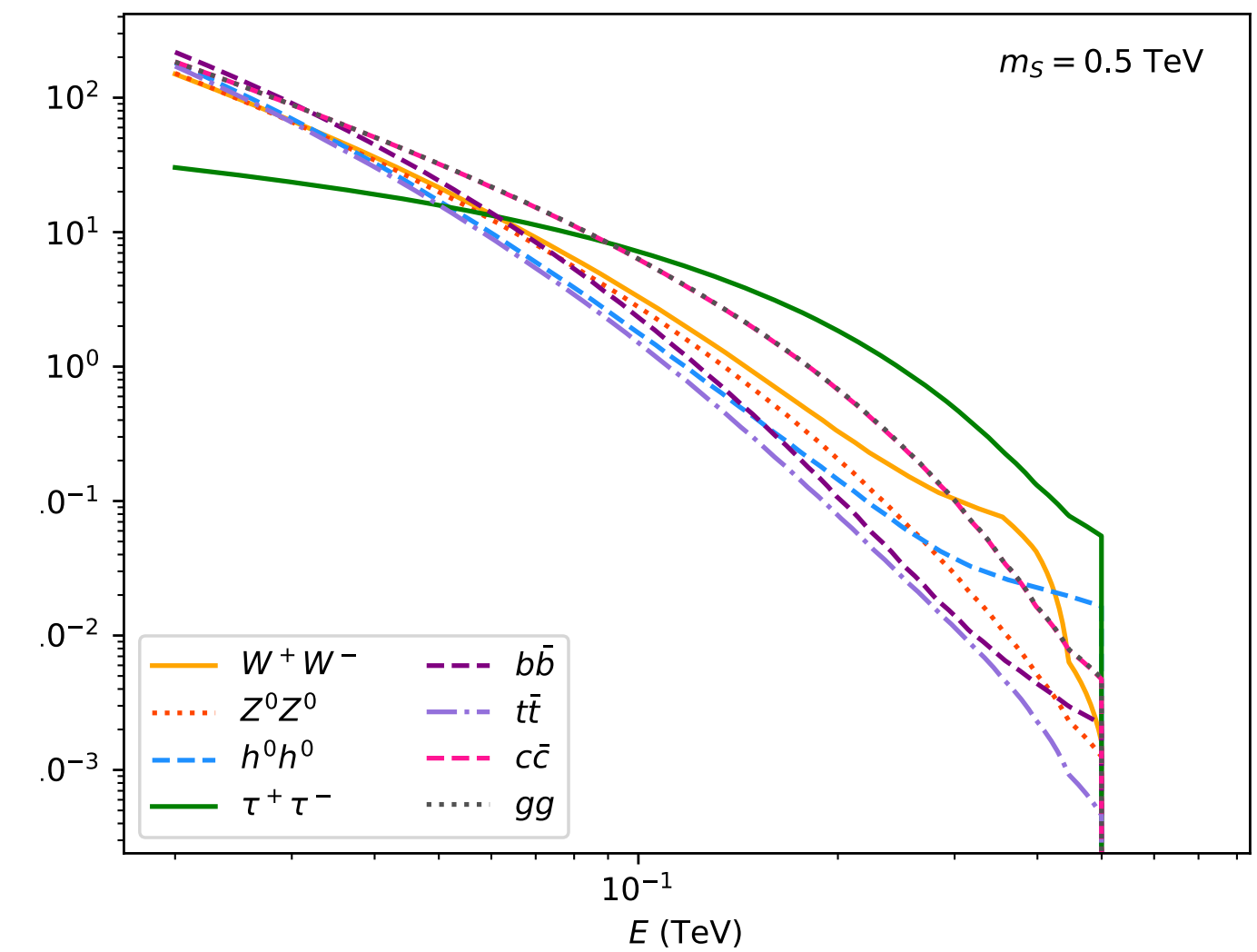
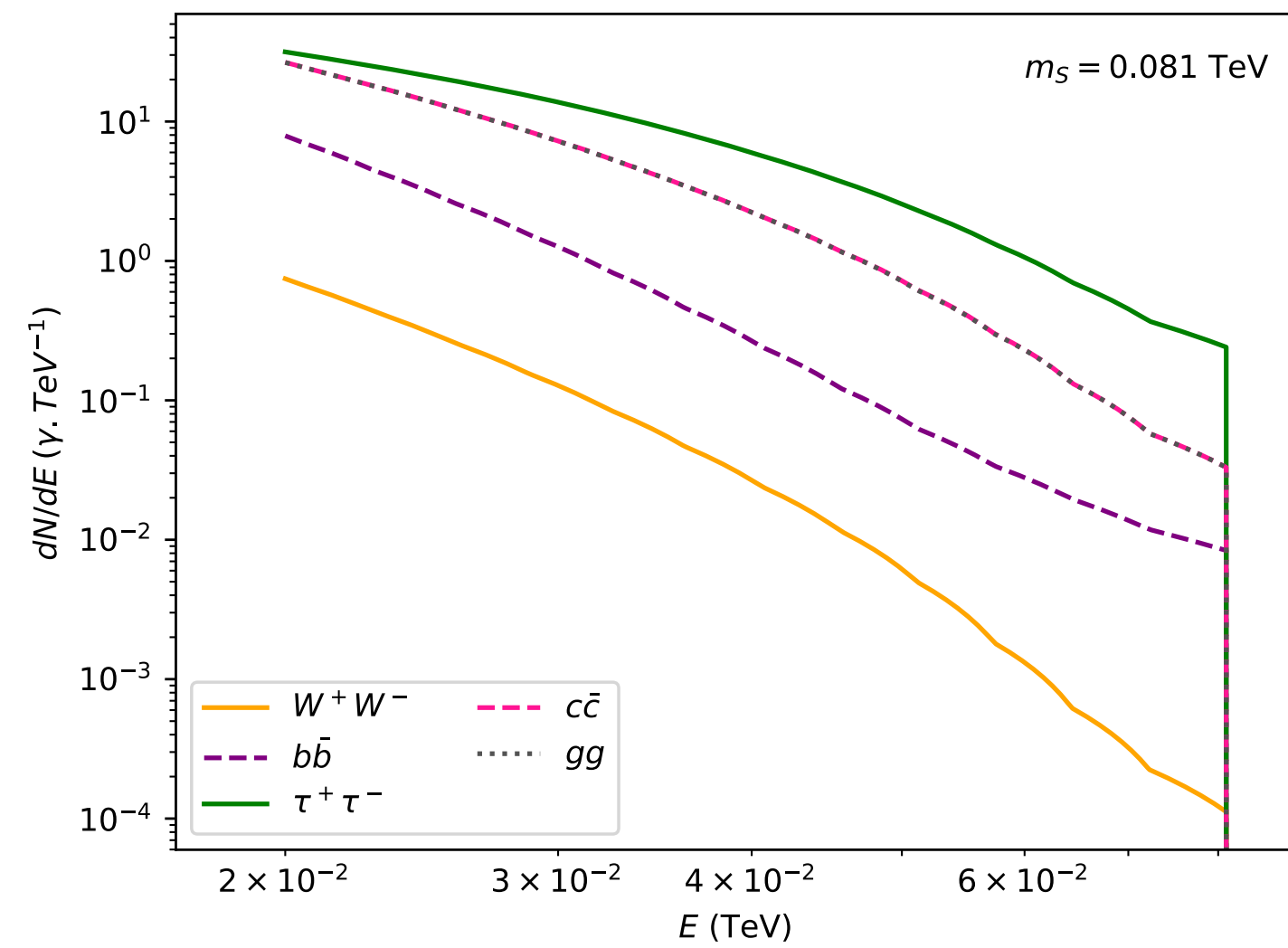
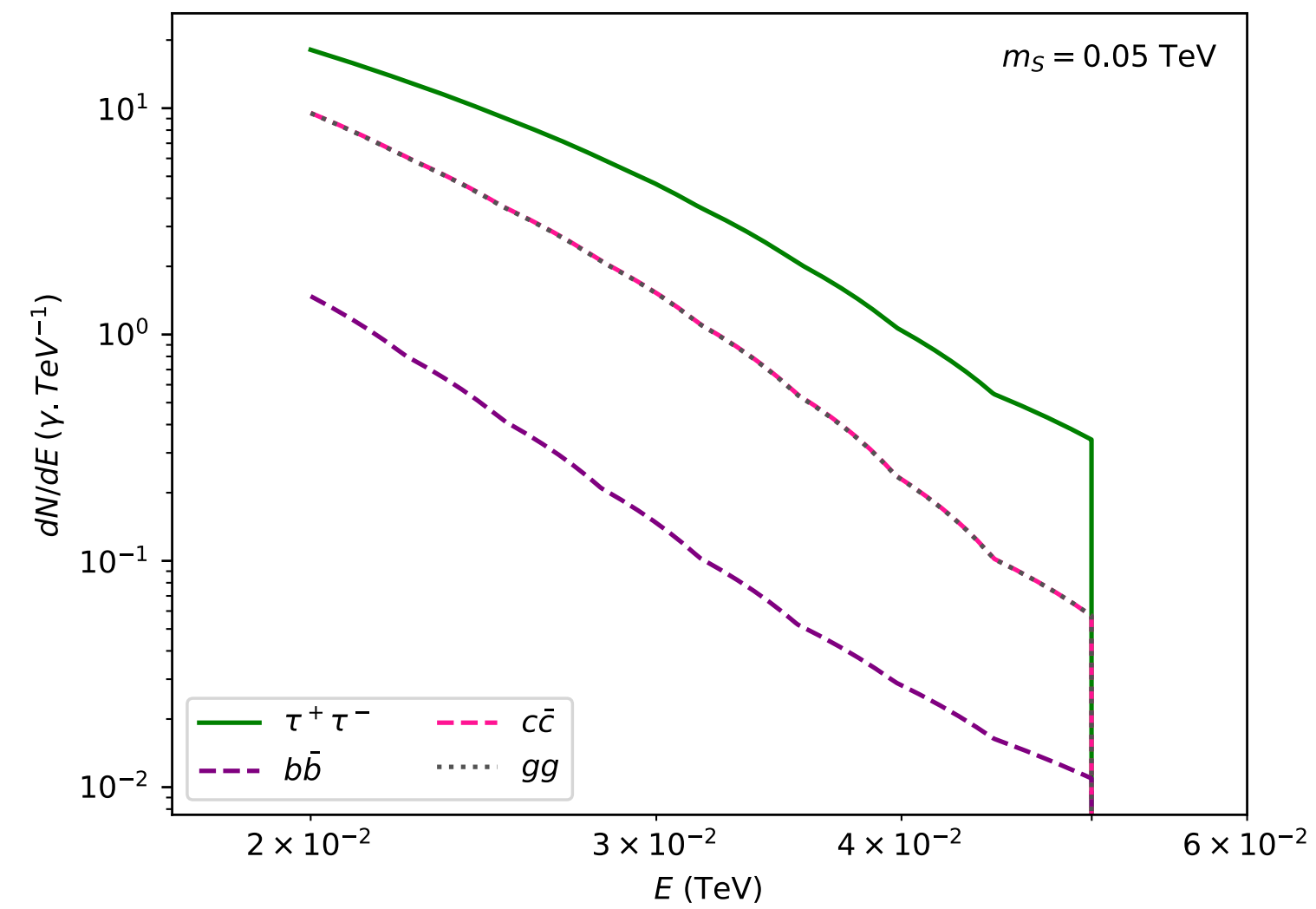
Log-normal likelihood to model the  
uncertainties of the J factor

$$\mathcal{L}^J = \frac{1}{\ln(10)\sqrt{2\pi}\sigma_J J} \exp - \frac{(\log_{10} J - \log_{10} \bar{J})^2}{2\sigma_J^2}$$

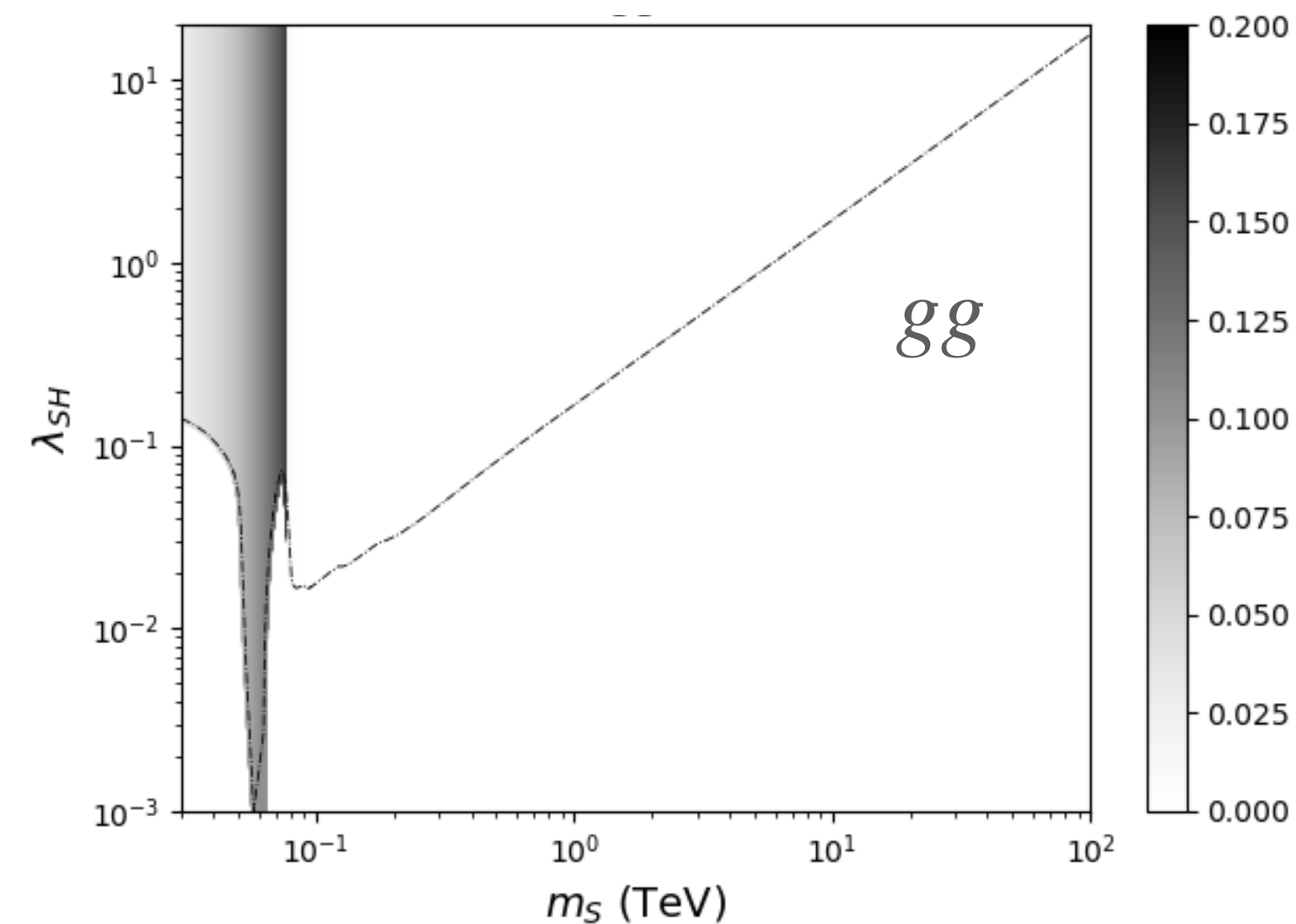
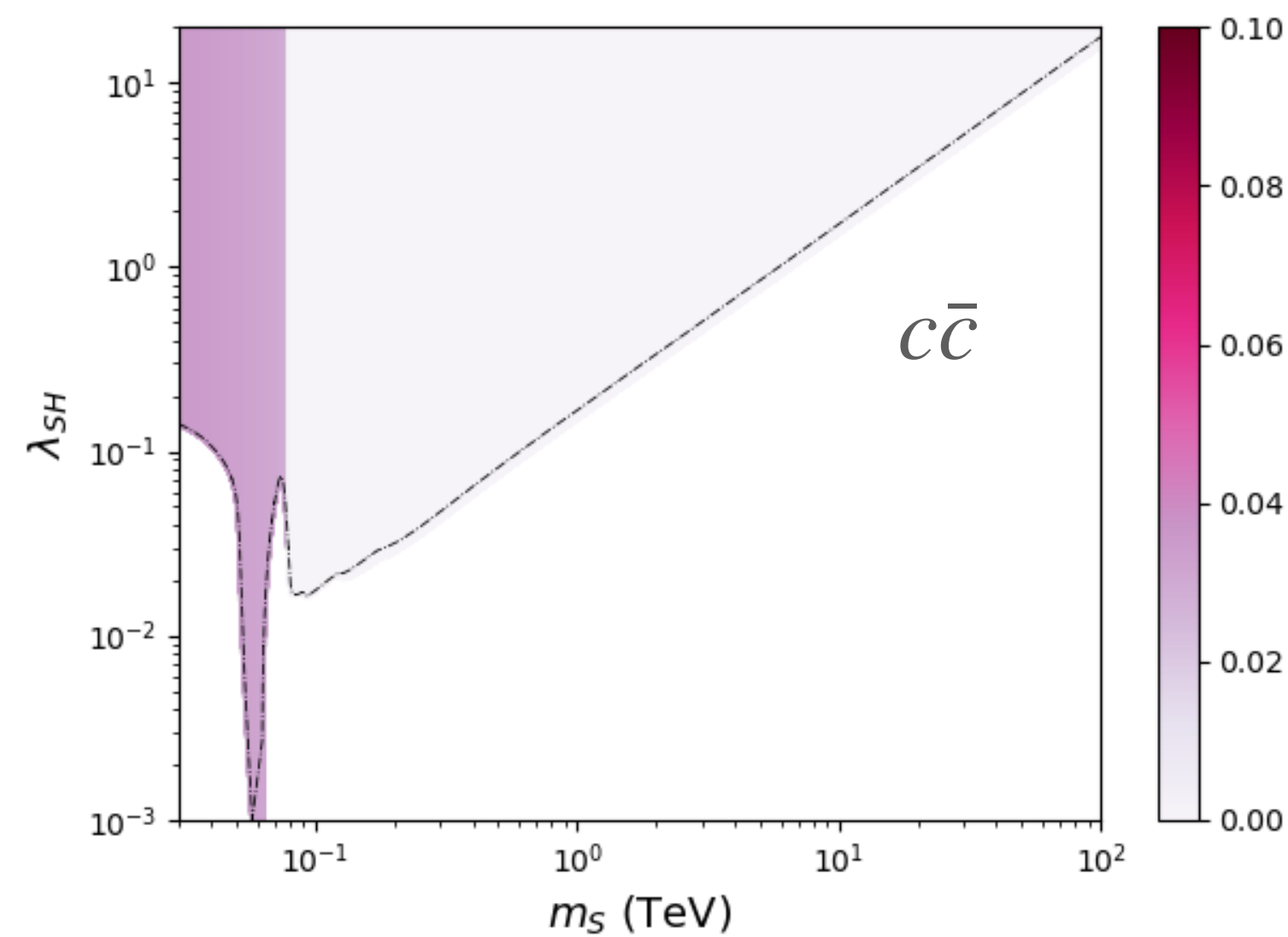
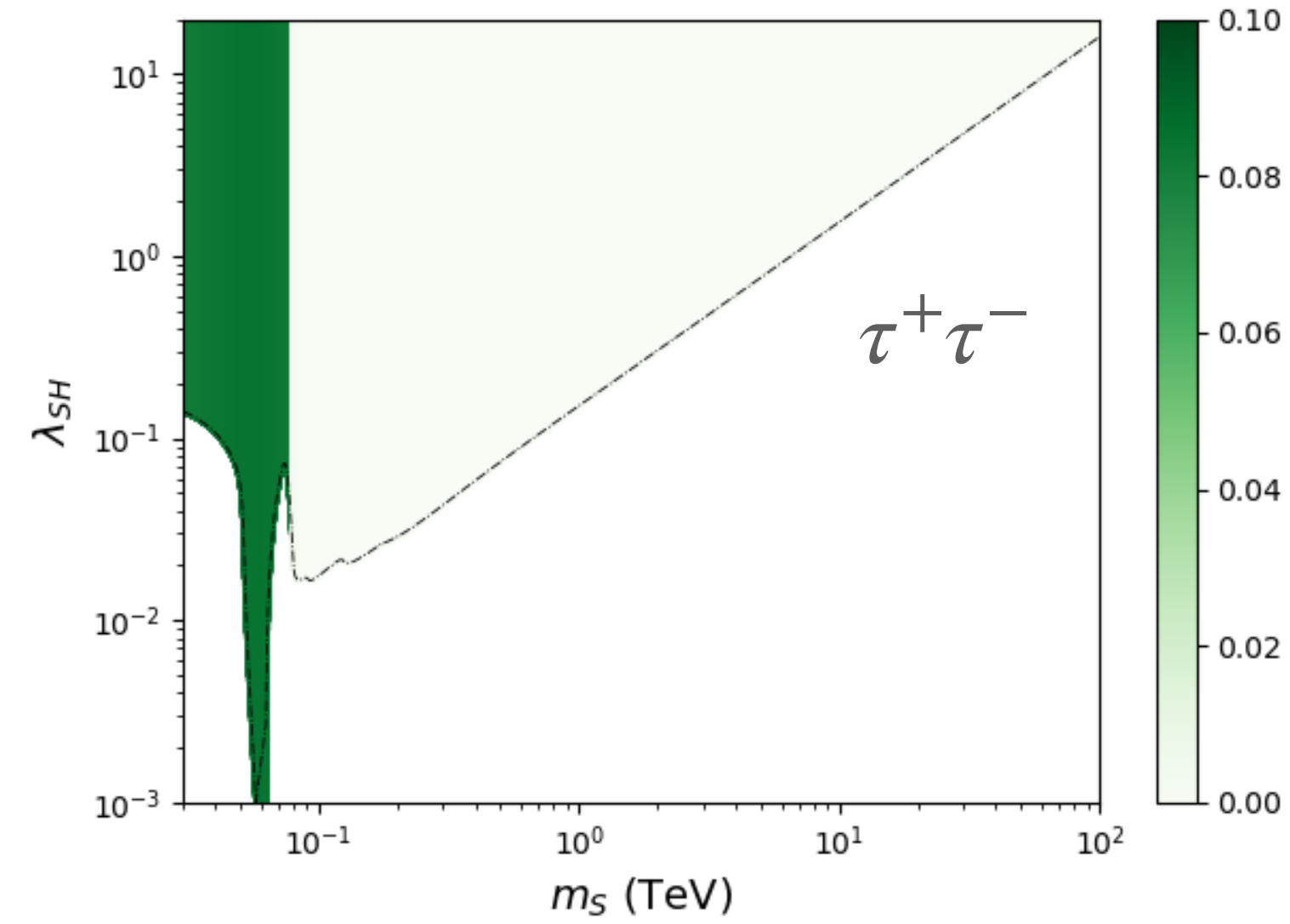
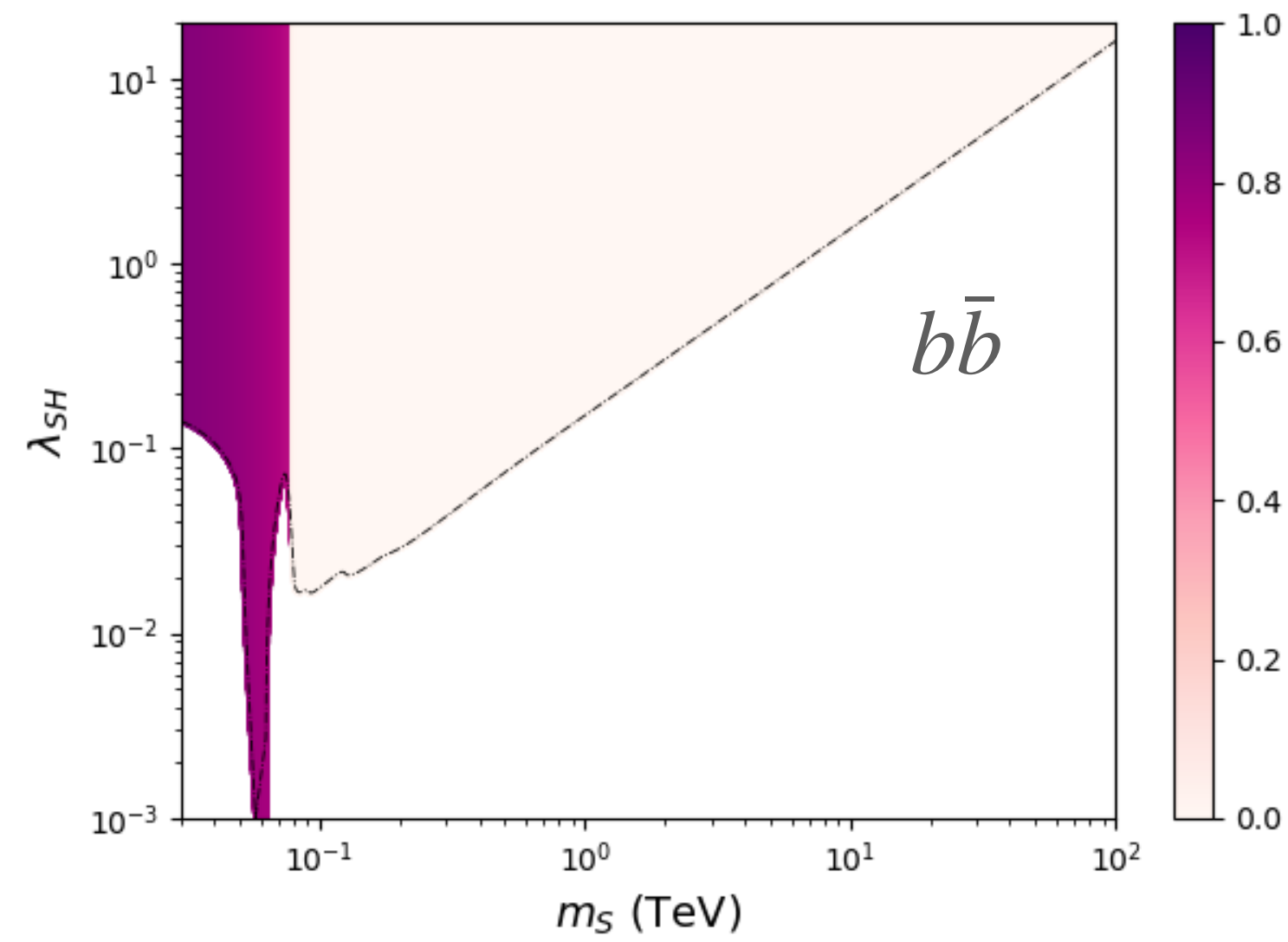


# SPECTRA

Ref: Cirelli et al. *JCAP* 03 (2011) 051

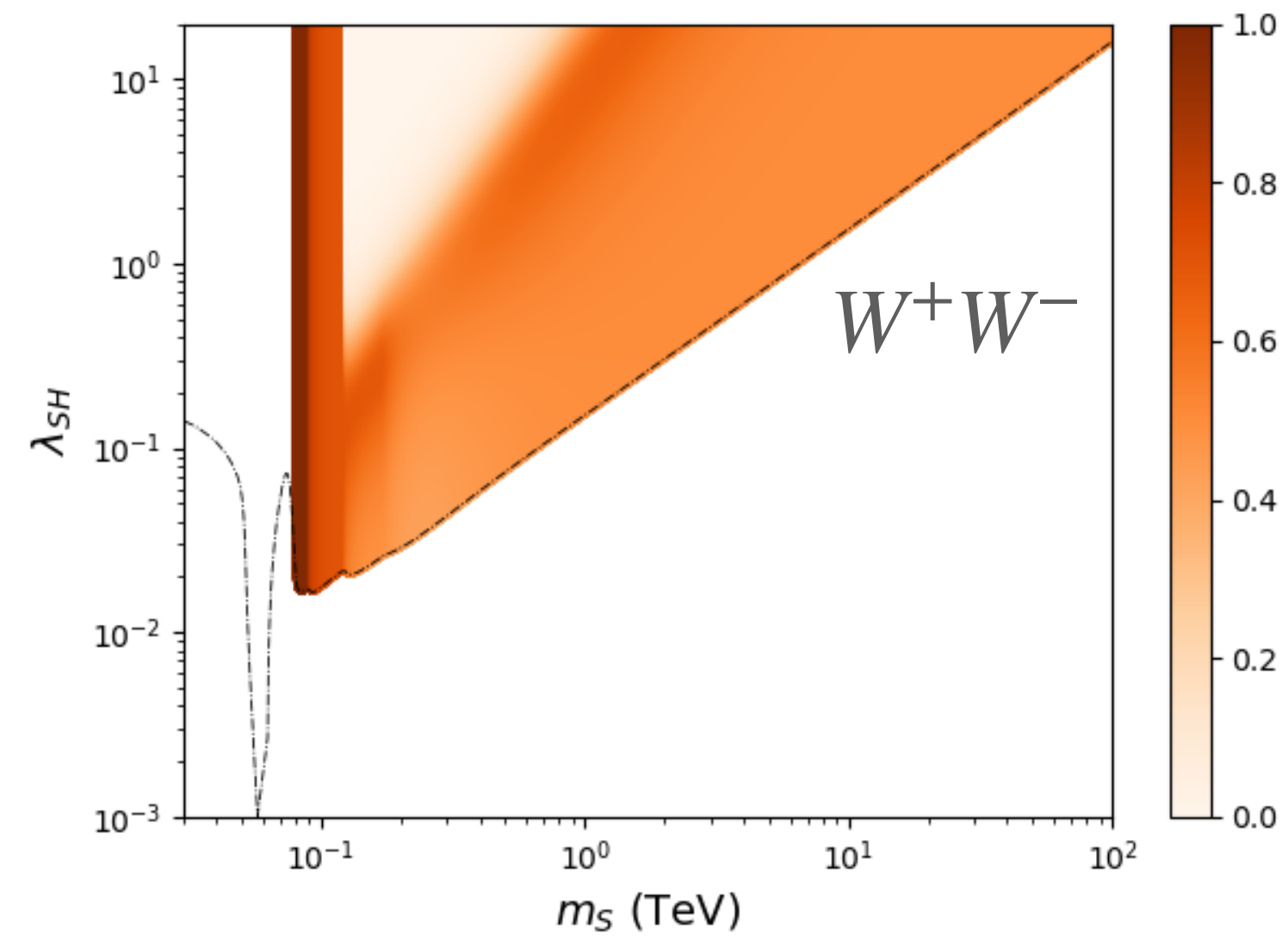
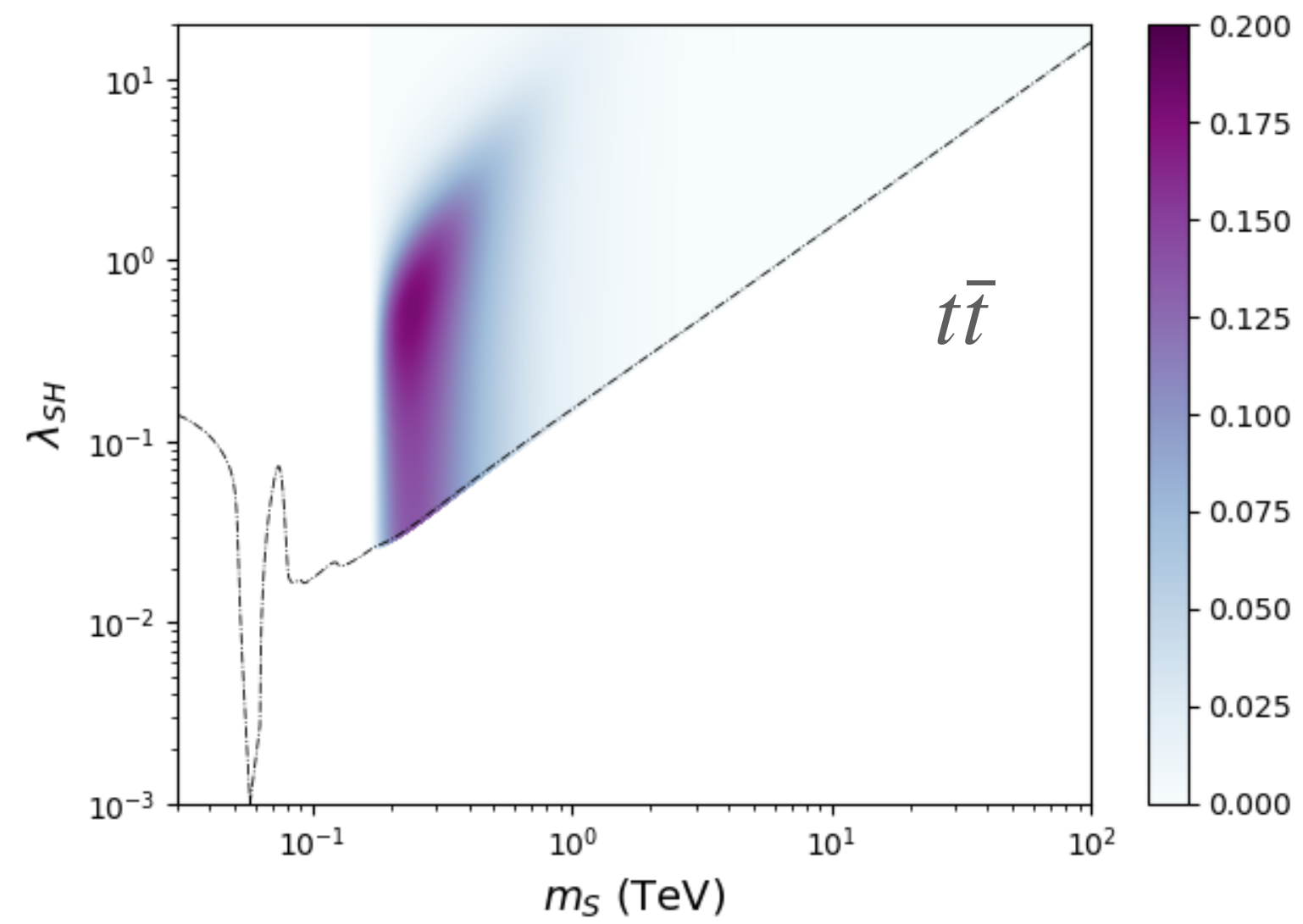


# BRANCHING RATIOS



$$m_S \lesssim m_W$$

# BRANCHING RATIOS



$$m_S \gtrsim m_W$$

