



**UNIVERSITÉ  
DE GENÈVE**

**FACULTÉ DES SCIENCES**  
Département d'astronomie

# Constraining the nature of dark matter and modified gravity in galaxy clusters

Dominique Eckert

Department of Astronomy, University of Geneva

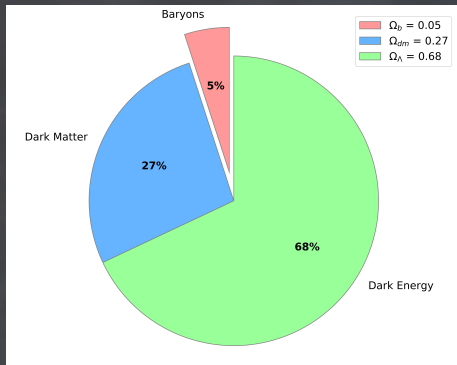
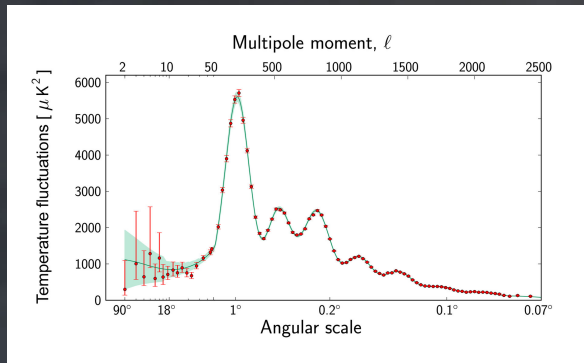
Main collaborators: S. Ettori, E. Pointecouteau, A. Robertson, R. Massey, R. Van der Burg, I. Loubser, ...

Eckert et al. 2022a, A&A 662, 123

Eckert et al. 2022b, A&A 666, 41

November 21, 2022

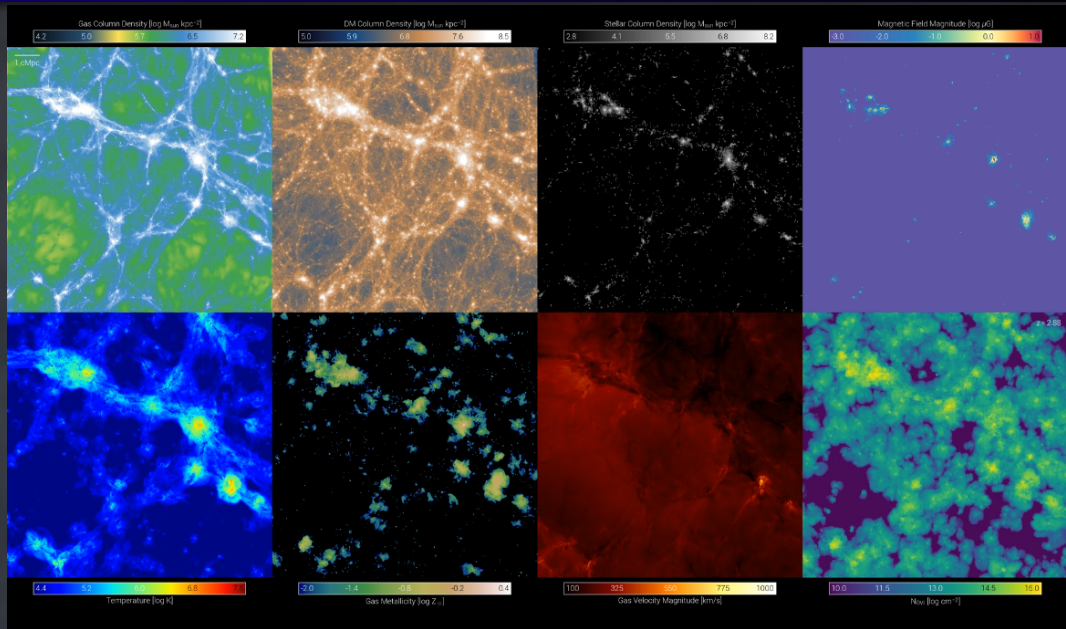
# The dark sector conundrum



Our currently favored cosmological framework describes the Universe's LSS extremely well... but it contains 95% unknown stuff!



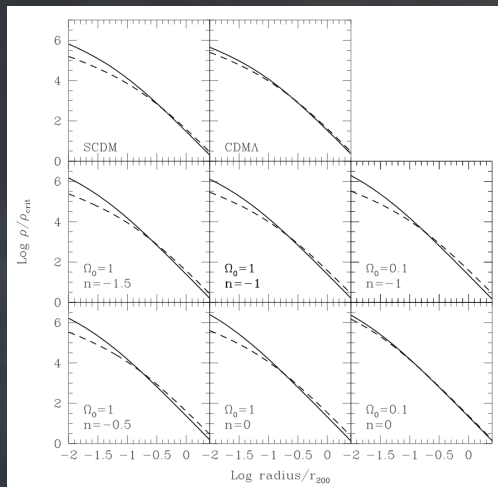
# The formation and evolution of dark matter halos



*Illustris TNG Simulation*

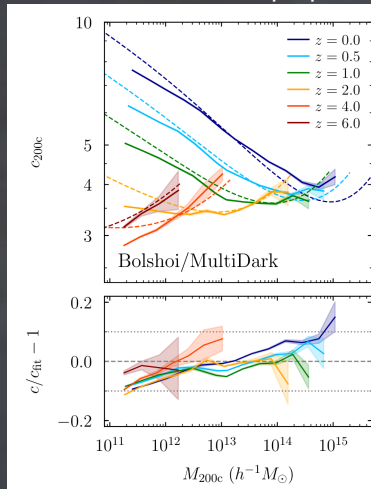
# The mass profiles of collapsed halos in CDM

$\Lambda$ CDM predicts that halos of all scales should share the same structural properties



*Navarro et al. 1997*

$$\rho_{NFW}(r) = \frac{\rho_s}{(r/r_s)(1+r/r_s)^2}$$

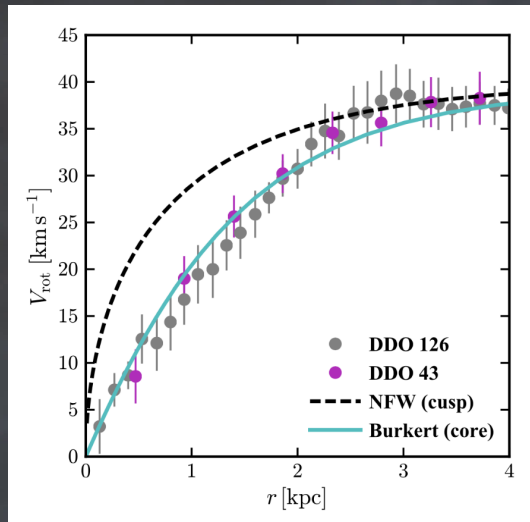


*Diemer & Joyce 2018*

$$c_{200} = \frac{r_s}{R_{200}}$$

# The core-cusp problem

- The NFW model predicts  $\rho(r) \propto r^{-1}$  in the central regions (*cusps*)
- In dwarf galaxies we often observe flat slopes of the gravitational field (*cores*) inconsistent with  $\Lambda$ CDM predictions
- Baryonic effects in dwarf galaxies are poorly understood; important to check this is in other mass ranges

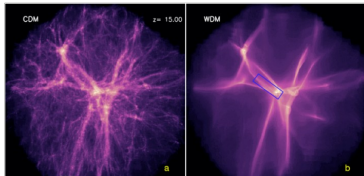


*Bullock & Boylan-Kolchin 2017*

# Alternatives to Cold Dark Matter

Warm Dark Matter

$m_\chi \sim 1\text{-}100\text{ keV}$

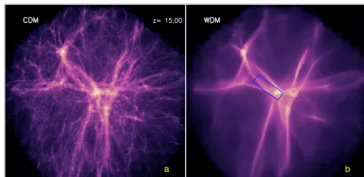


*Moustakas et al. 2009*

# Alternatives to Cold Dark Matter

## Warm Dark Matter

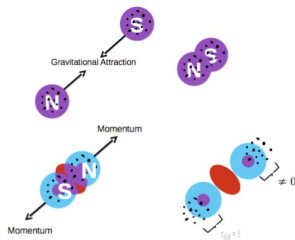
$$m_\chi \sim 1\text{-}100 \text{ keV}$$



*Moustakas et al. 2009*

## Self-Interacting Dark Matter

$$\sigma_{\text{DM-DM}} > 0$$

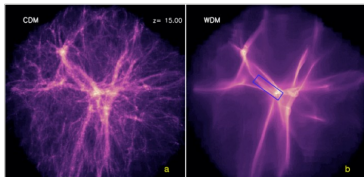


*Wittman et al. 2018*

# Alternatives to Cold Dark Matter

## Warm Dark Matter

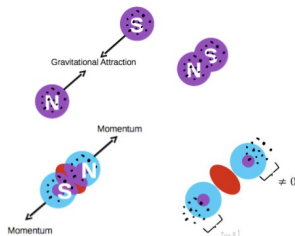
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*Moustakas et al. 2009*

## Self-Interacting Dark Matter

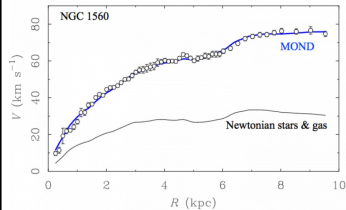
$$\sigma_{\text{DM-DM}} > 0$$



*Wittman et al. 2018*

## Modification of gravity

$$F_g \neq F_{\text{Newton}}$$

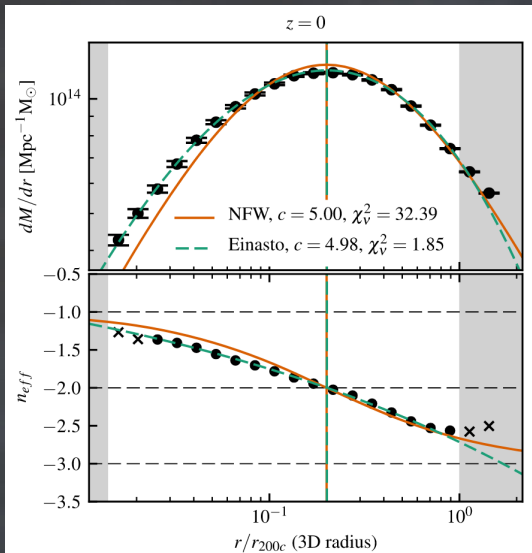


*Begelman et al. 1991*

# The Einasto profile

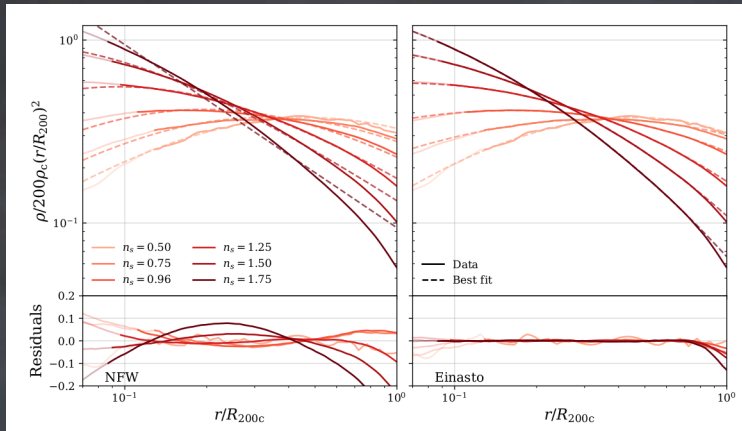
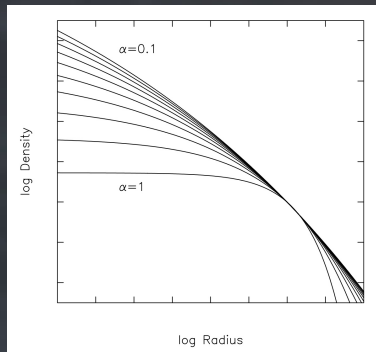
A more general form of DM profiles is the Einasto profile,

$$\rho(r) = \rho_{-2} \exp \left[ -\frac{2}{\alpha} \left( \left( \frac{r}{r_{-2}} \right)^\alpha - 1 \right) \right]$$



*Child et al. 2018*

# The Einasto profile



*Brown et al. 2020*

The Einasto index  $\alpha$  depends on the slope of the primordial matter power spectrum  $n_s$



# Galaxy clusters as the largest concentrations of dark matter

Given their masses galaxy clusters are “closed boxes” for dark matter and baryons alike



*MACS 0416, Jauzac, DE, et al. 2015*

Galaxy clusters can contain up to  $10^{15} M_{\odot}$  of dark matter. They are the best place to search for deviations from  $\Lambda$ CDM!

# Cluster mass profiles from hydrostatic equilibrium

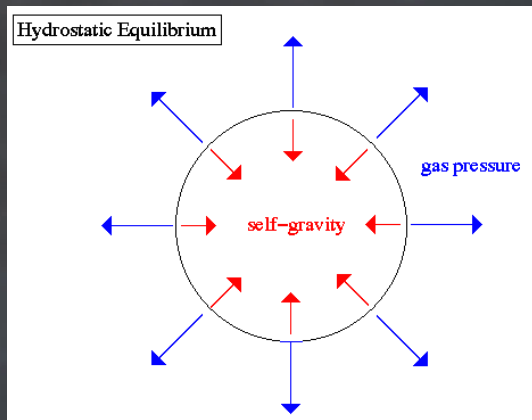
- The dynamics of the hot gaseous atmosphere follows the Euler equation,

$$\frac{\partial \mathbf{v}}{\partial t} + (\mathbf{v} \cdot \nabla) \mathbf{v} = -\frac{1}{\rho} \nabla P - \nabla \Phi$$

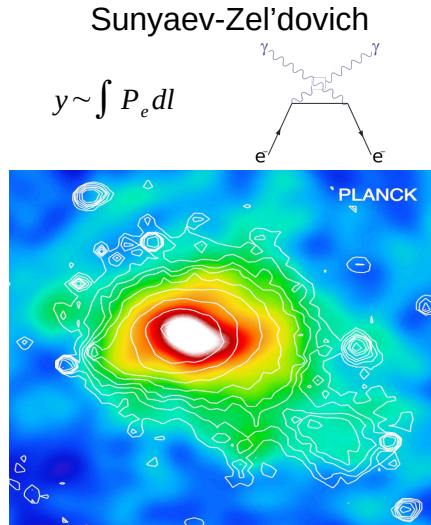
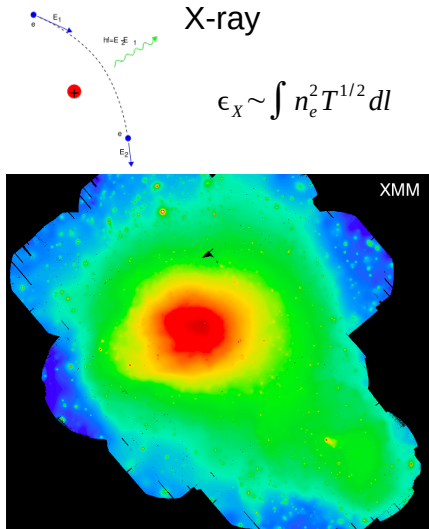
- After relaxation the velocity field is small and the halo is spherically symmetric,

$$\frac{dP}{dr} \approx -\rho \frac{d\Phi}{dr}$$

- If we can measure  $P$ ,  $\rho$  then we can recover  $\Phi$



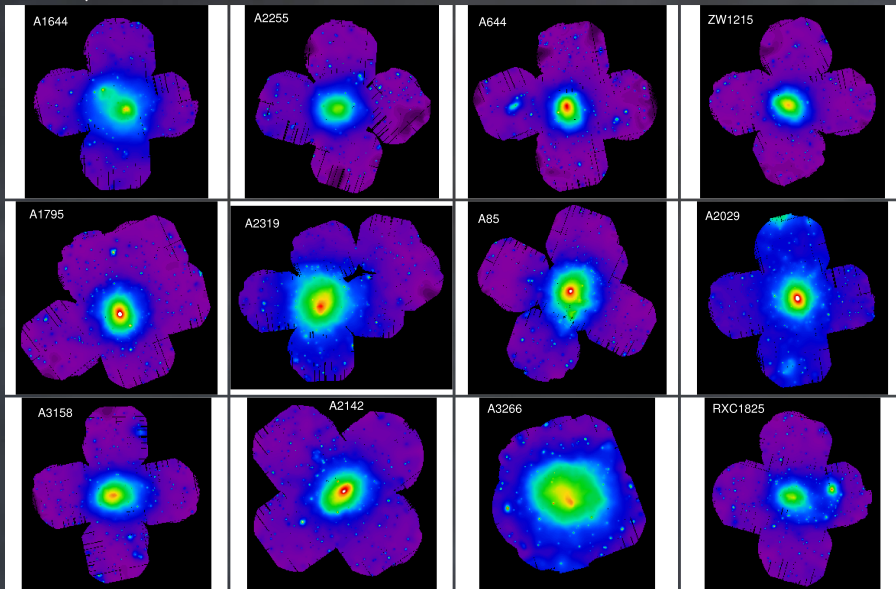
# Joint X-ray/Sunyaev-Zeldovich observations of galaxy clusters



$$kT = P_{SZ}/n_X, K = P_{SZ} n_X^{-5/3}, \frac{dP_{SZ}}{dr} = -\rho_X \frac{GM(<r)}{r^2}$$

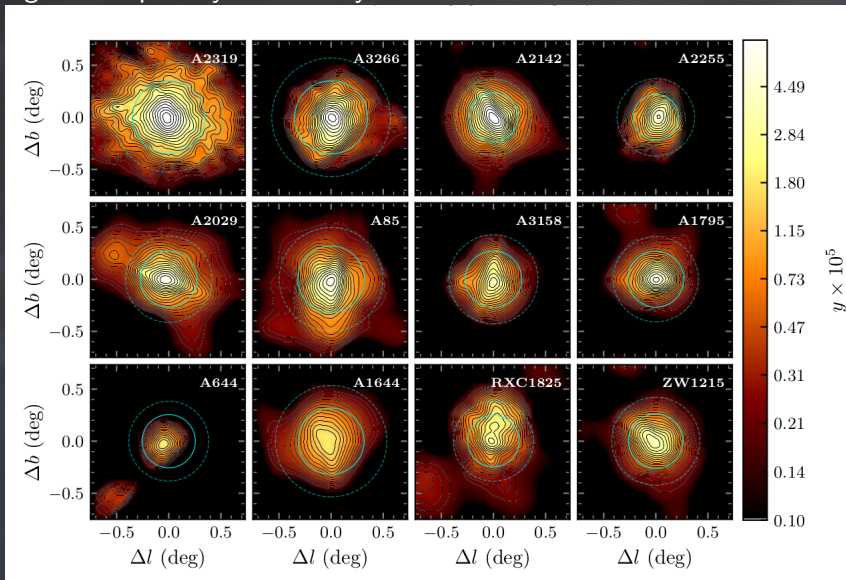
# The X-COP project

X-COP (PI: Eckert) is a very large program on XMM to follow up Planck clusters with the highest S/N



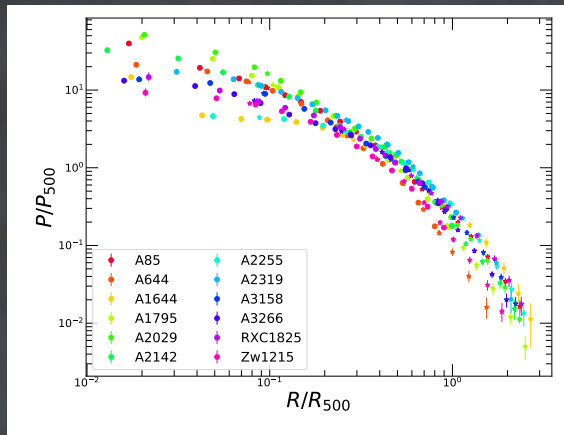
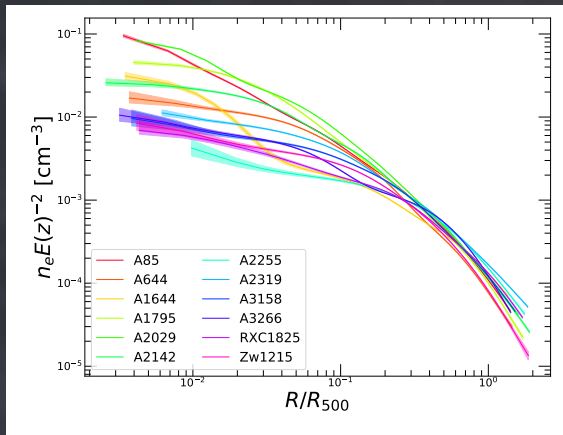
# SZ observations with Planck

All our targets are spatially resolved by *Planck*



Baldi, ..., DE, ..., 2019

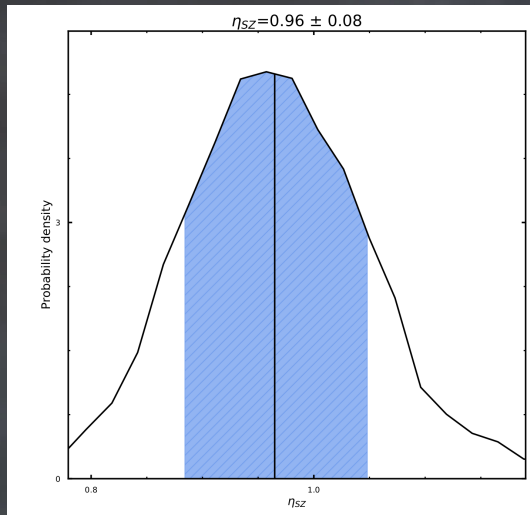
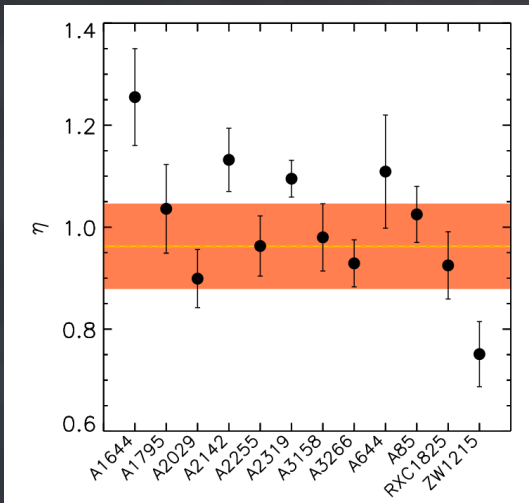
# X-ray and SZ profiles



*Ghirardini, DE et al. 2019*

Our profiles extend to  $1.8R_{500}$  ( $n$ ),  $2.3R_{500}$  ( $P$ ), and  $0.9R_{500}$  ( $T$ )

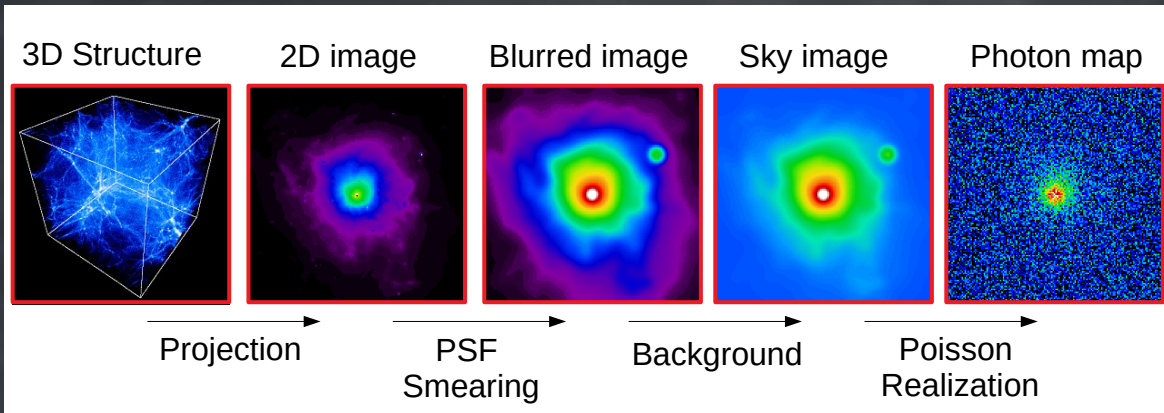
# Consistency between X-ray and SZ data



We measure on average  $\eta_{SZ} = \frac{P_{SZ}}{k_B T_X n_e} = 0.96 \pm 0.08$

# Mass Reconstruction using Bayesian Forward Modelling

In practice we have access to *projected* and *PSF-blurred* quantities

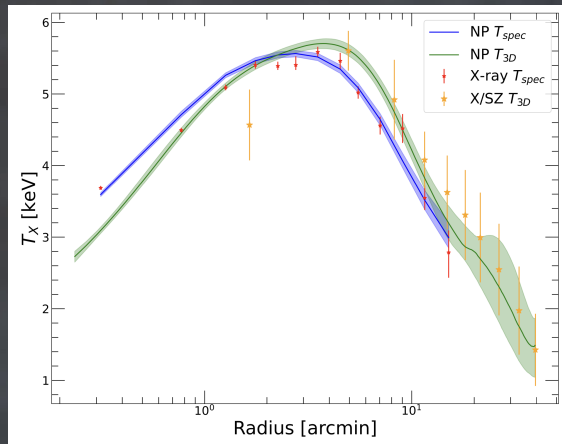
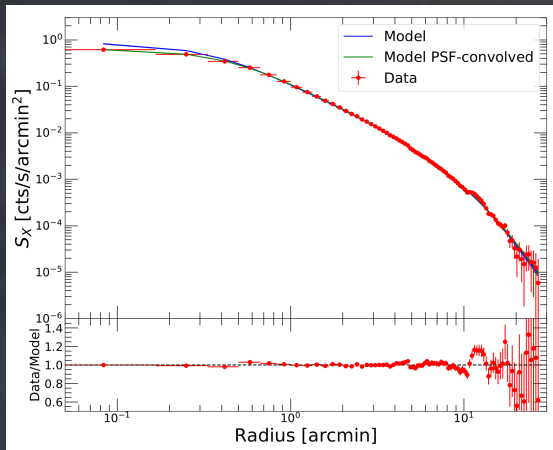


*Eckert et al. 2020*

We decompose the 3D profile as a linear combination of basis functions and forward fit the model to the observed counts

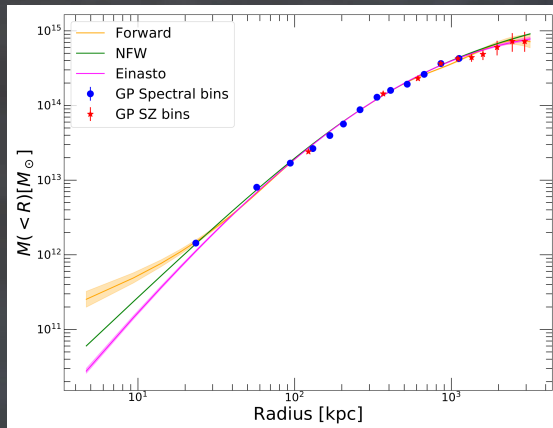
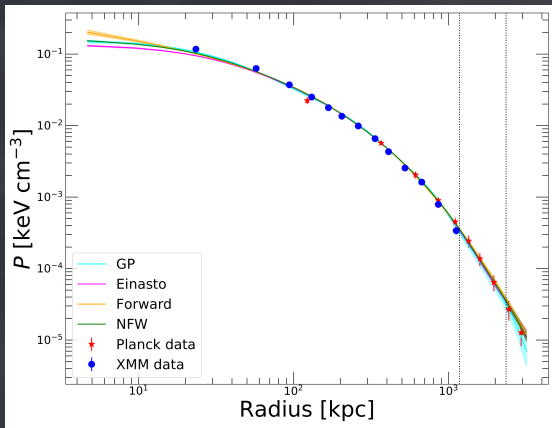


# Example mass reconstruction: A1795



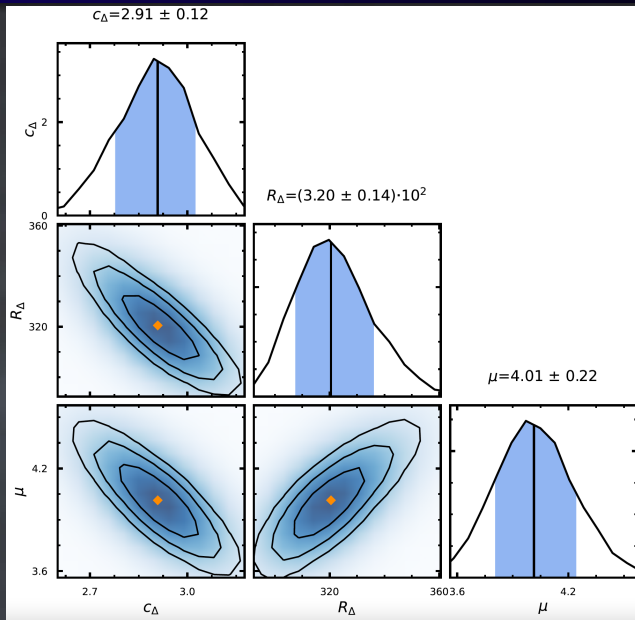
*Eckert et al. 2022a*

# Example mass reconstruction: A1795



*Eckert et al. 2022a*

# Example mass reconstruction: A1795



*Eckert et al. 2022a*

# Public code and documentation

All the code is public! Check out the Python packages `pyproffit` (surface brightness, density, imaging) and `hydromass` (deprojection, mass modeling)

hydromass

latest

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## Fitting a mass model

Since the sound crossing time in a galaxy cluster is much smaller than the cluster formation time, the gas in these systems is roughly in equilibrium between the gravitational force and the thermal pressure gradient. Therefore, the hydrostatic equilibrium equation can be used to get an estimate of the total gravitating mass profile,

$$\frac{dP_{gas}}{dr} = -\rho_{gas} \frac{GM(<r)}{r^2}$$

If a parametric model  $M(<r) = f(r|\theta)$  respective to a set of parameters  $\theta$  can be defined for the total mass, the hydrostatic equilibrium equation and the gas density profile can be integrated to predict the 3D pressure profile,

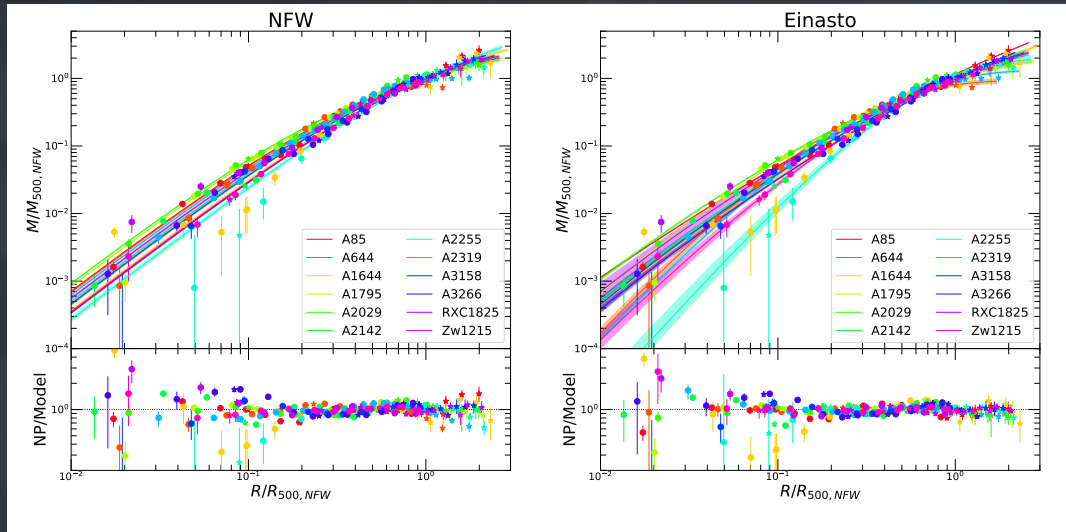
$$P_{3D}(r) = P_0 + \int_r^{r_0} \rho_{gas} \frac{Gf(r'|\theta)}{r'^2} dr'$$

The model pressure can then be projected and convolved with instrumental effects to predict the X-ray spectroscopic temperature profile and the SZ pressure profile.

This tutorial explains how to use `hydromass` and `pyproffit` to fit a mass model to X-ray data from a galaxy cluster under the assumption that the gas is in hydrostatic equilibrium. The chosen example is applied to XMM-Newton observations of the massive galaxy cluster MACS 0451 at  $z=0.54$ , which were published in [Tam et al. \(2020\)](#) and was found to be in excellent agreement with the gravitational lensing data.

<https://hydromass.readthedocs.io>   <https://pyproffit.readthedocs.io>

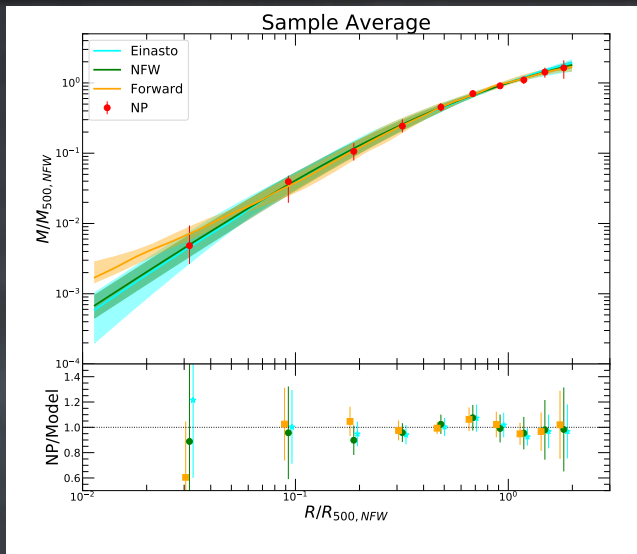
# Einasto vs NFW reconstruction



Eckert et al. 2022a

There is *more variety* in the DM profiles than can be captured with NFW only

# NFW closely traces the average mass profiles

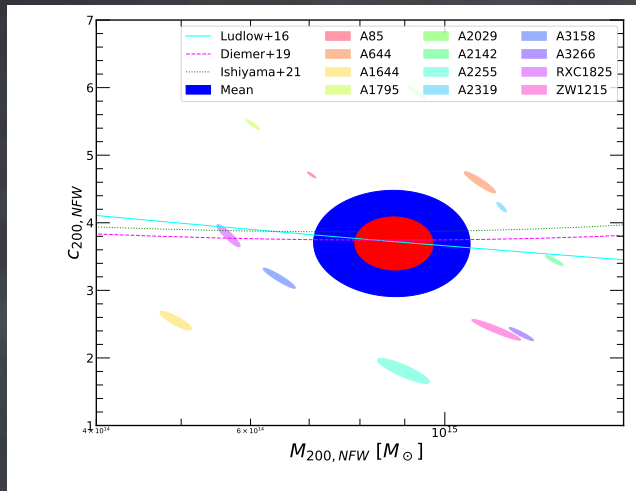


*Eckert et al. 2022a*

The median profiles look closely like NFW, differences less than 10% at all radii

# The mass-concentration relation

In  $\Lambda$ CDM the relation between halo mass and NFW concentration should follow a well known relation

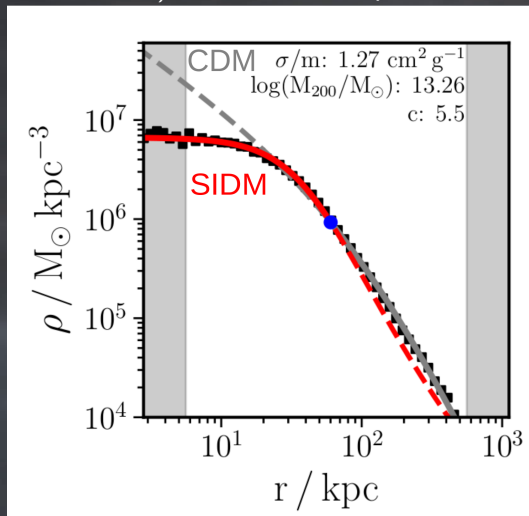


*Eckert et al. 2022a*

Our measurements exactly match the predictions of the  $\Lambda$ CDM paradigm

# Mass profiles in self-interacting DM

DM self-interaction ( $\sigma_{DM-DM} > 0$ ) modifies the shape of DM halos

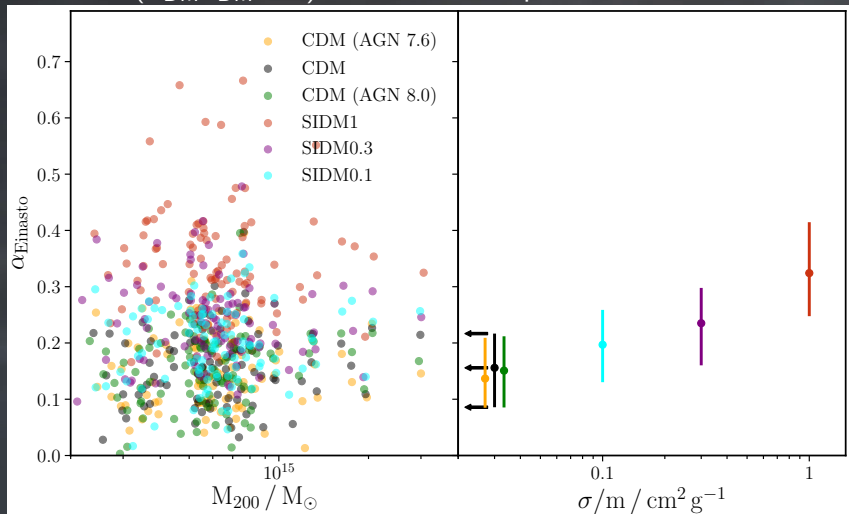


*Robertson et al. 2020*



# Mass profiles in self-interacting DM

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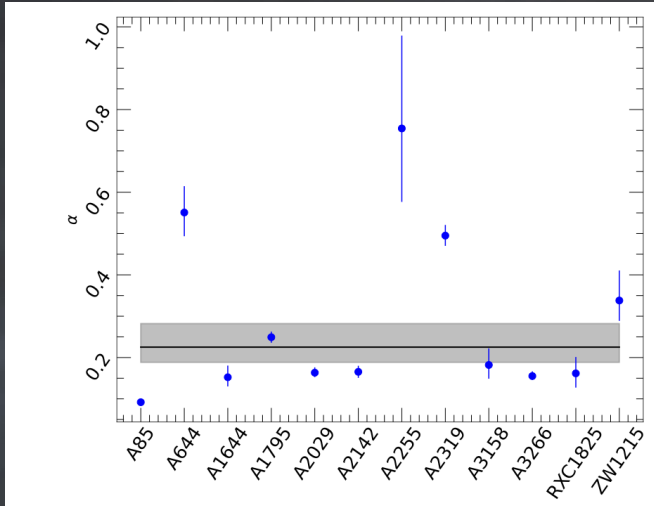


*Robertson et al. 2020*

The Einasto index  $\alpha$  is sensitive to  $\sigma_{DM-DM}$

# Einasto index of X-COP clusters

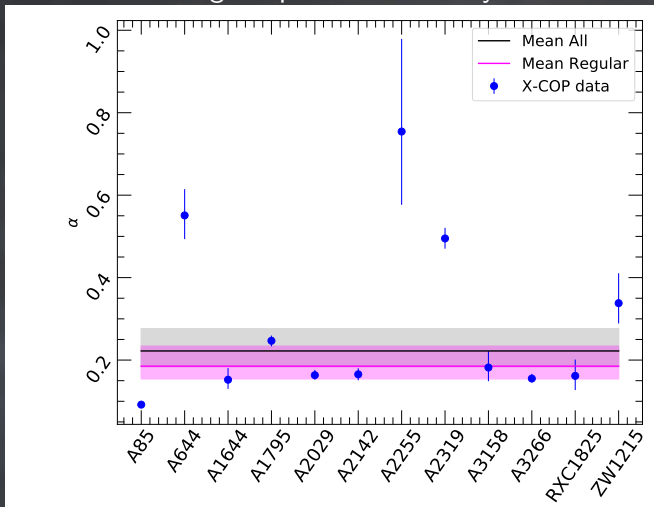
We were able to measure  $\alpha$  with good precision for all systems



*Eckert et al. 2022b*

# Einasto index of X-COP clusters

We were able to measure  $\alpha$  with good precision for all systems

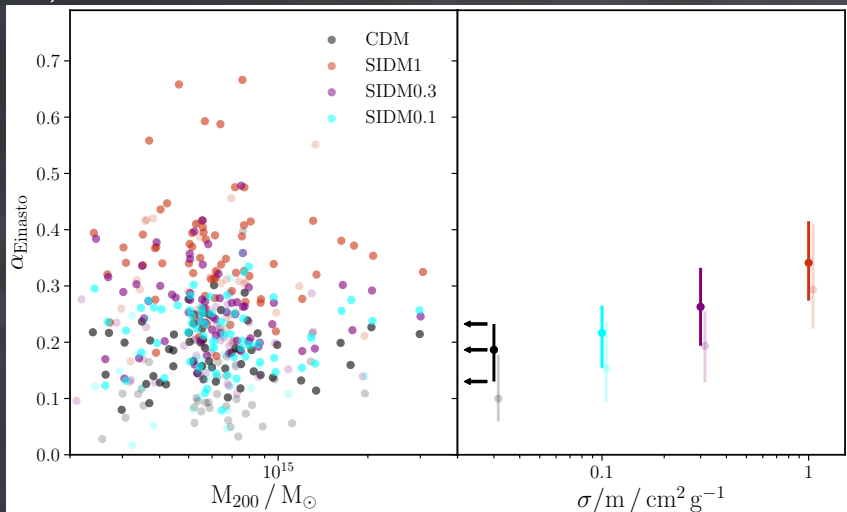


*Eckert et al. 2022b*

To minimize systematics (mis-centering, HSE bias, deviations from spherical symmetry...) we select only the regular X-ray clusters,  $w < 0.02$

# Comparison with numerical simulations

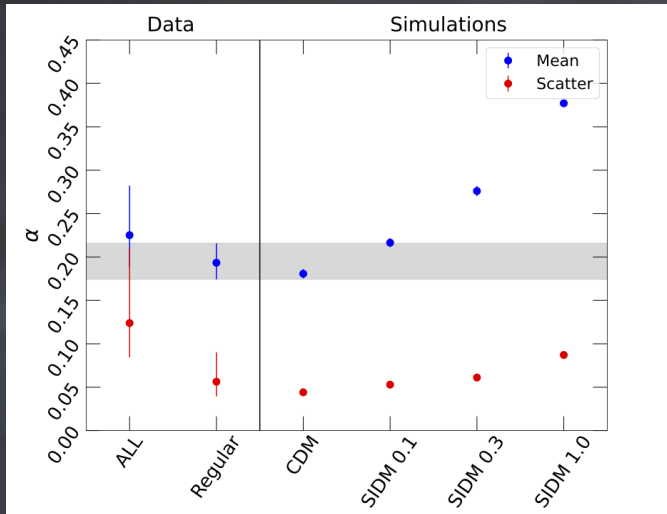
For an appropriate comparison we select only *relaxed* systems in numerical simulations ( $X_{\text{off}} < 0.05$ )



Eckert et al. 2022b

# Comparison with numerical simulations

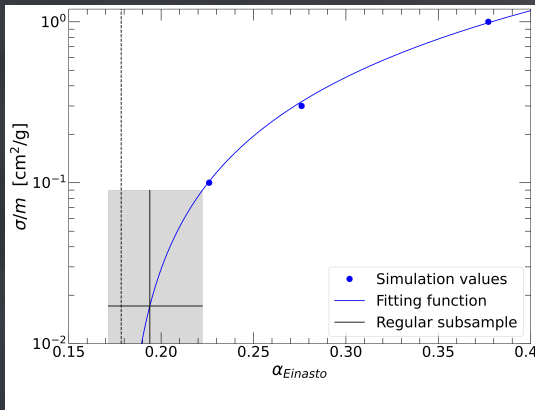
For an appropriate comparison we select only *relaxed* systems in numerical simulations ( $X_{\text{off}} < 0.05$ )



Eckert et al. 2022b

# Constraints on $\sigma_{DM-DM}$

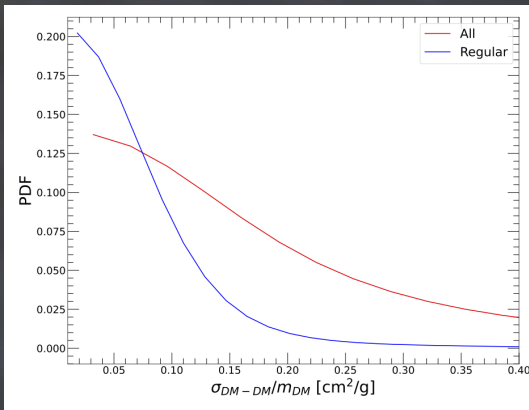
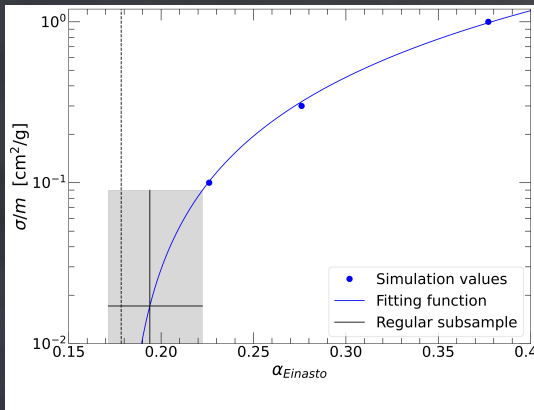
For every value of  $\alpha$  we can associate a value of  $\sigma_{DM-DM}$  and draw a posterior PDF



*Eckert et al. 2022b*

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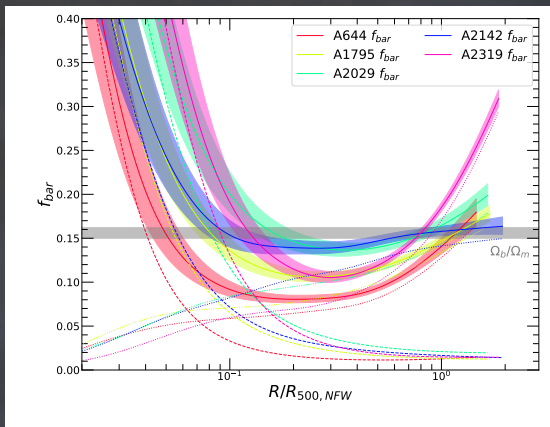
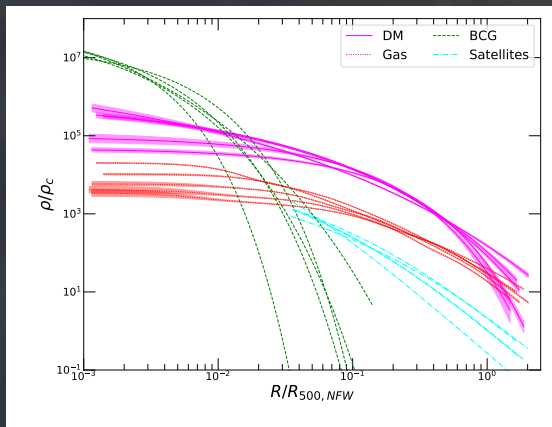


*Eckert et al. 2022b*

Using the regular sample we set an upper limit  $\sigma_{DM-DM} < 0.13$  cm<sup>2</sup>/g (90% c.l.)

# DM vs baryonic components

For a subset of systems we directly measured all the relevant baryonic components: gas, BCG, and satellites

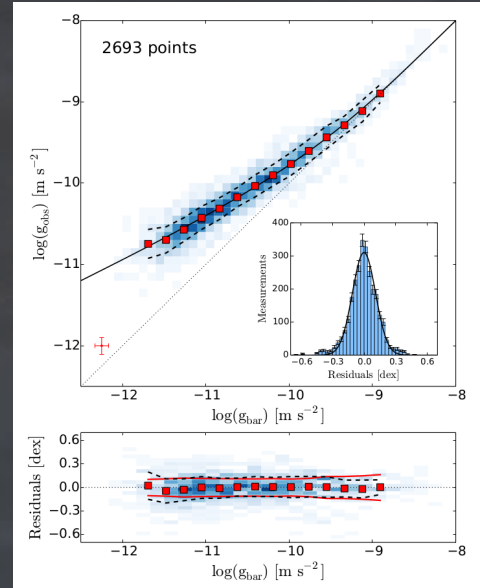


*Eckert et al. 2022a*



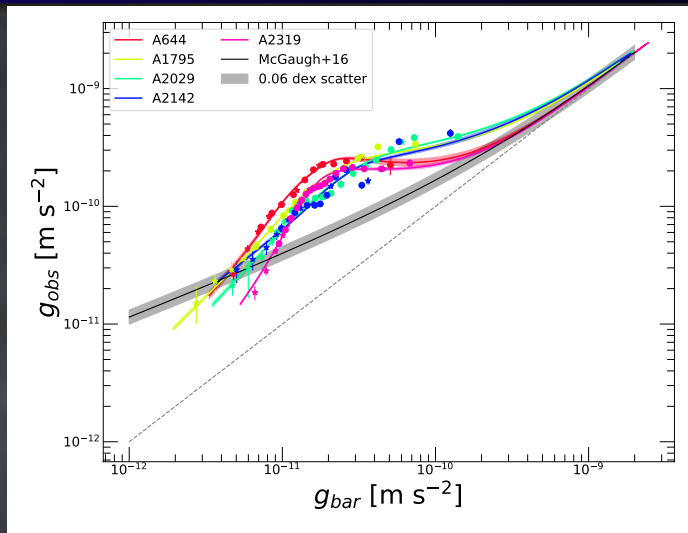
# A universal radial acceleration relation?

- Similar calculations were made for galaxy rotation curves, i.e. comparing the observed gravitational force with that expected from baryons only
- When plotted in terms of gravitational force, it looks like the scale where deviation from baryonic expectations occurs doesn't depend on galaxy mass or type (McGaugh et al. 2016)



McGaugh et al. 2016

# What about galaxy clusters?

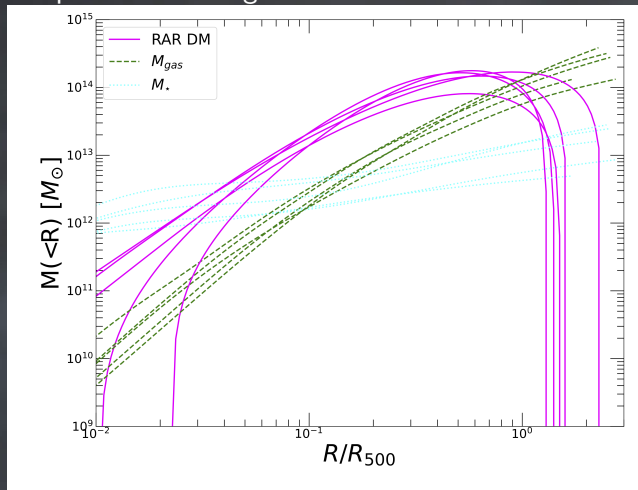


Eckert et al. 2022a

The relation between baryonic and total acceleration *is not universal*, and thus it does not derive from a fundamental property of gravity

# A missing mass component in MOND?

Angus et al. (2010) postulate that a missing mass component (e.g. sterile neutrino) in clusters could make up for the missing acceleration



Eckert et al. 2022a

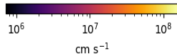
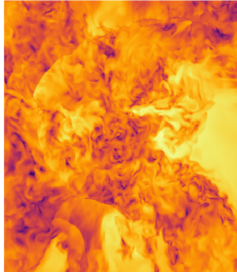
The missing mass should have an *unphysically decreasing* shape on large scales

# Beyond hydrostatic equilibrium

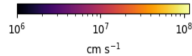
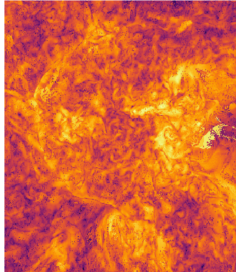
In practice the velocity field in clusters cannot be completely neglected

$$\frac{\partial \mathbf{v}}{\partial t} + (\mathbf{v} \cdot \nabla) \mathbf{v} = -\frac{1}{\rho} \nabla P - \nabla \Phi$$

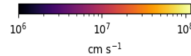
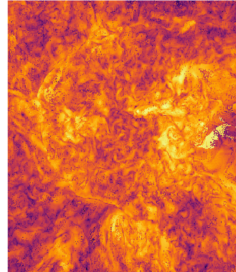
Velocity field



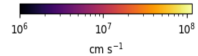
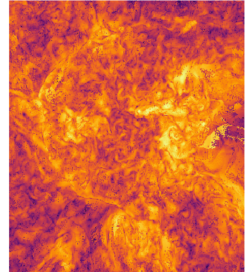
Turbulent velocity field,  
tolerance:  $f = 0.77$



Turbulent velocity field,  
tolerance:  $f = 2/3$



Turbulent velocity field,  
tolerance: 1%

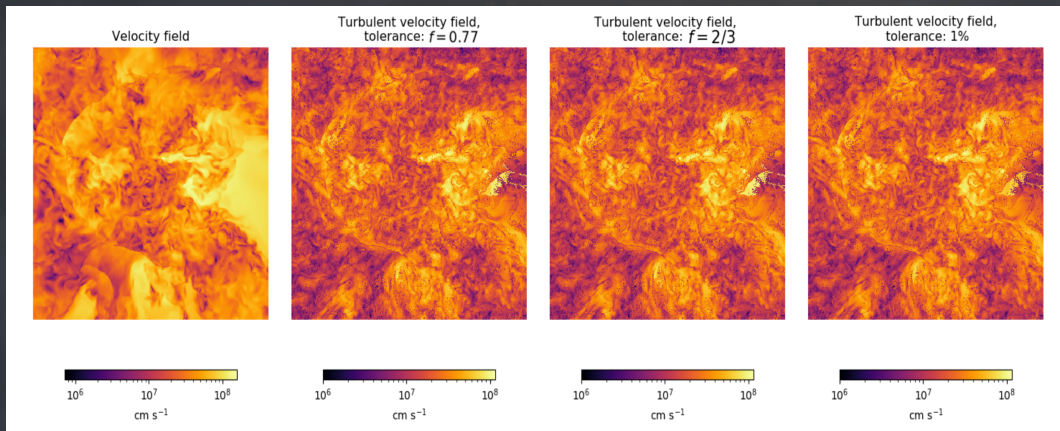


*Angelinelli et al. 2020*

# Beyond hydrostatic equilibrium

In practice the velocity field in clusters cannot be completely neglected

$$\frac{\partial \mathbf{v}}{\partial t} + (\mathbf{v} \cdot \nabla) \mathbf{v} = -\frac{1}{\rho} \nabla P - \nabla \Phi$$

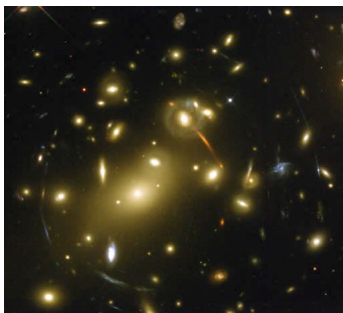


*Angelinelli et al. 2020*

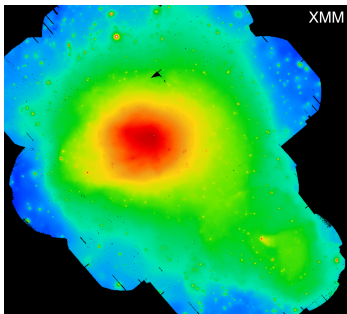
Random gas motions (a.k.a. turbulence) act as an *extra* pressure term

# Accounting for non-thermal pressure with weak gravitational lensing

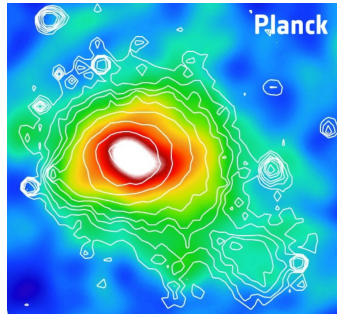
Lensing



X-ray



SZ



$$\Sigma_{mat} \propto \int_{\parallel} \rho_{mat} dl$$

$$\epsilon_X \propto \int_{\parallel} n_e^2 dl$$

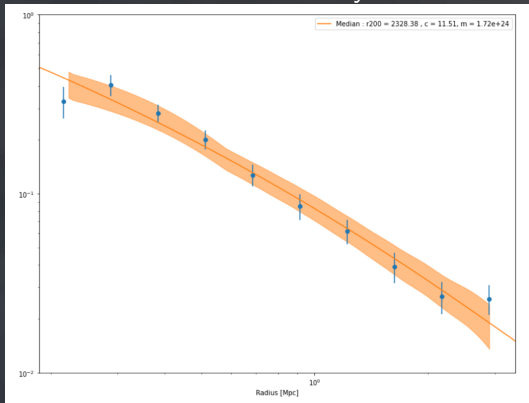
$$T_X \propto \frac{\int_{\parallel} w T dl}{\int_{\parallel} w dl}$$

$$y_{SZ} \propto \int_{\parallel} n_e T dl$$

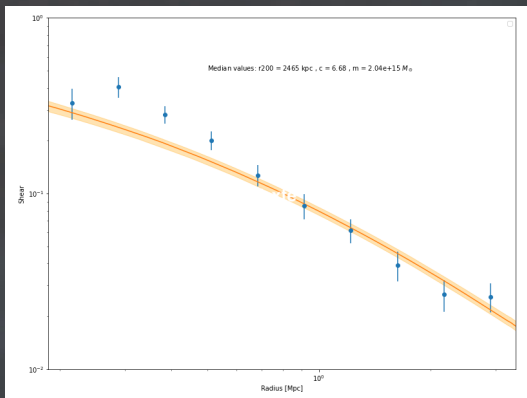
The weak gravitational lensing signal is independent of the hydrostatic assumption; however, strong dependence on l.o.s. structure

# Joint analysis with weak lensing and non-thermal pressure

WL only



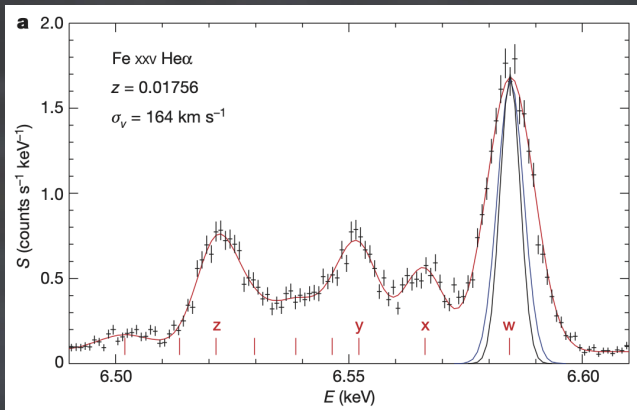
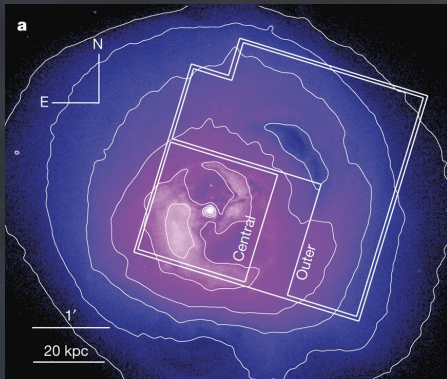
WL+X-ray



A1689, Loris Chappuis's MSc thesis

# Measuring the ICM velocity field with X-ray microcalorimeters

*Hitomi* has given us a short preview of the amazing things we can expect from microcalorimeters

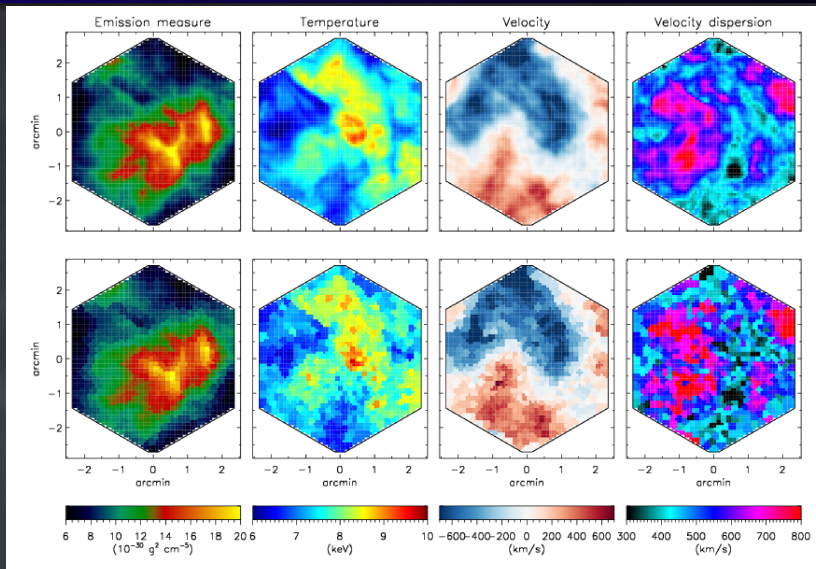


*Perseus cluster, Hitomi Collaboration 16*

A line broadening of  $164 \pm 10 \text{ km/s}$  is detected;  $P_{\text{turb}} \approx 4\% P_{\text{thermal}}$



# Mapping gas motions with Athena/X-IFU

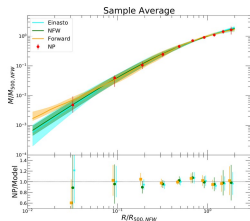


*Simulation of a fiducial cluster at  $z=0.1$ , Roncarelli et al. 2018*

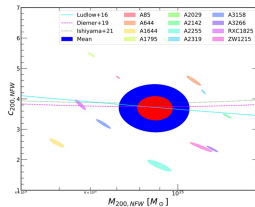
We need the X-IFU to accurately map gas motions and measure accurate DM profiles!

# Take home message

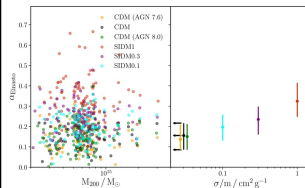
The average mass profiles look closely like an NFW, with deviations smaller than 10 % at all radii



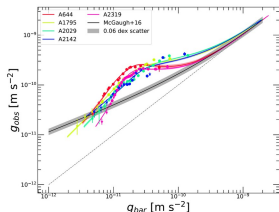
The structural properties of galaxy clusters closely match  $\Lambda$ CDM predictions



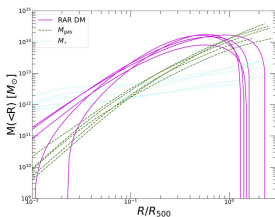
The Einasto index  $\alpha$  is sensitive to the dark matter self-interaction cross section ; we set  $\sigma_{\text{DM-DM}} < 0.13 \text{ cm}^2/\text{g}$  (90 % c.l.)



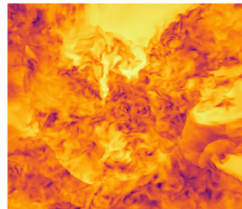
The relation between baryonic and total acceleration is not a fundamental property of gravity



The shape of the measured gravitational field is inconsistent with MOND predictions

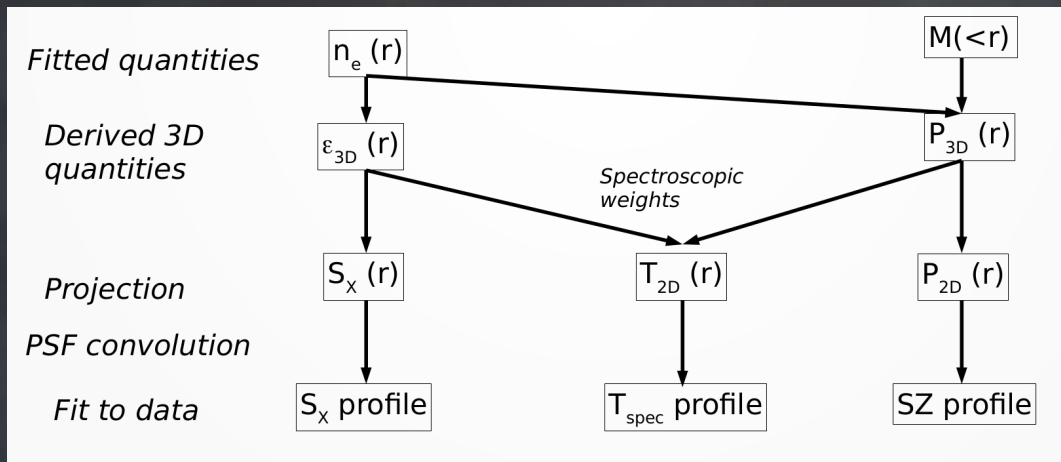


We need Athena/X-IFU to determine the velocity field and accurately measure the gravitational field



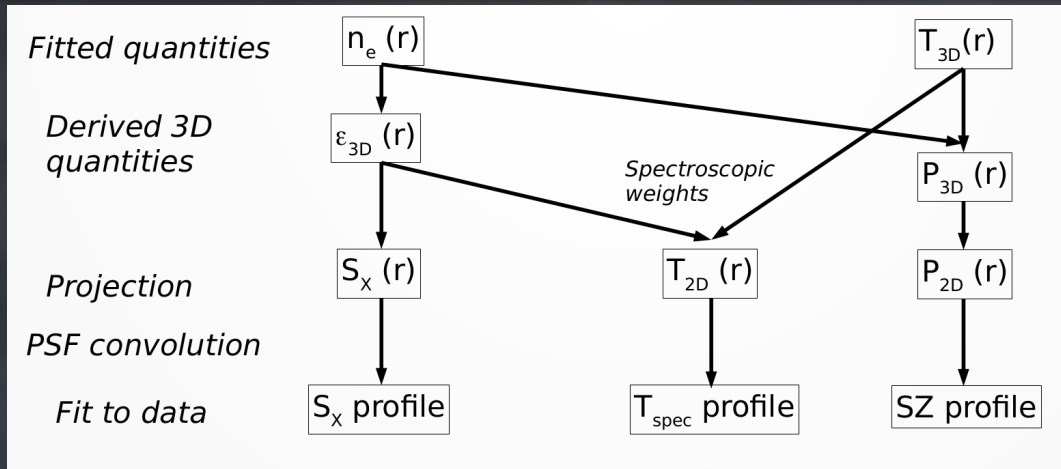
# Backup Slides

# Mass modeling scheme



We assume a functional form for the mass (Einasto, NFW) and forward-model it to the data, jointly fitting X-ray and SZ observables

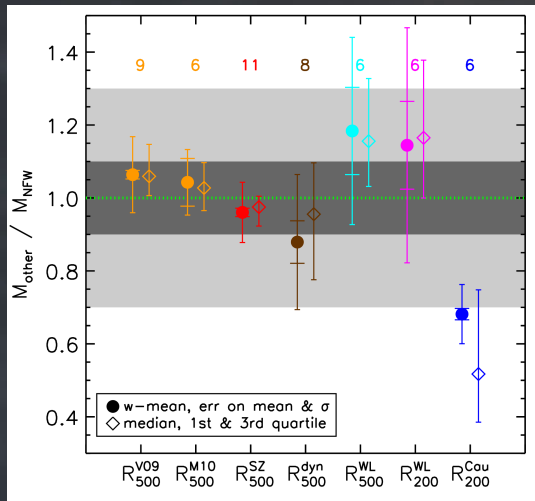
# Non-parametric lognormal mixture reconstruction



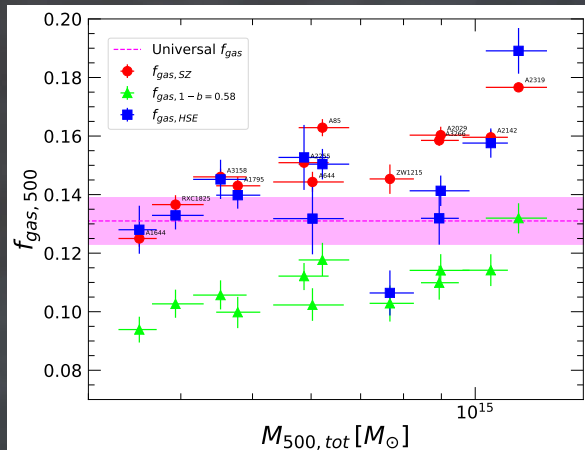
As a comparison point we apply a *non-parametric* method by describing the 3D temperature profile as a linear combination of Gaussians

$$\log T_{3D}(r) = \sum G_i \mathcal{N}(\mu_i, \sigma_i^2)$$

# HSE bias in X-COP clusters



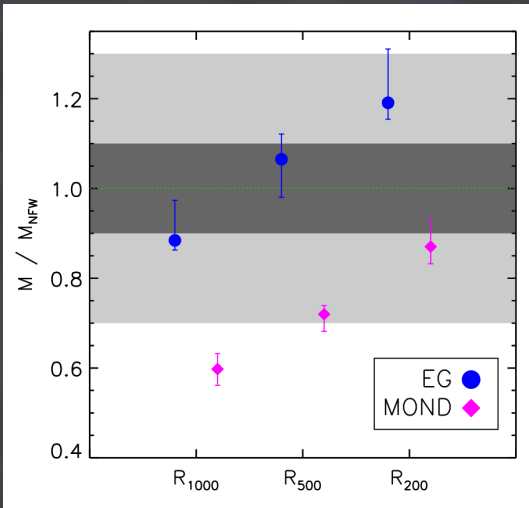
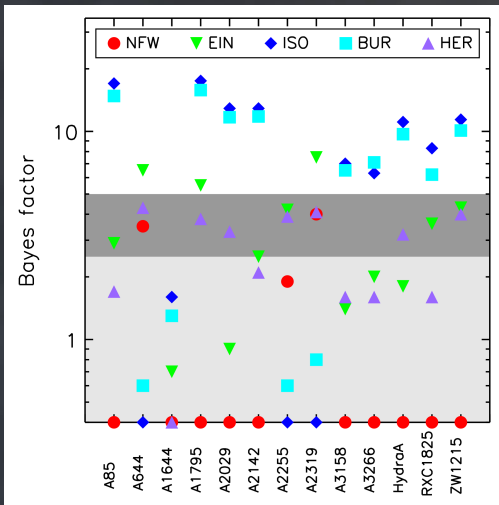
Ettori et al. 2019



Eckert et al. 2019

# Mass profile comparison

In Ettori et al. 2019 we found that NFW is generally a better fit to the X-COP data than competing models

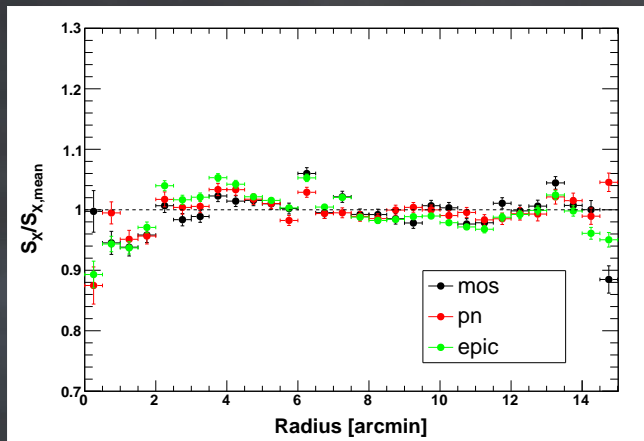


*Ettori, DE, et al. 2019*

Here the Einasto index was fixed to  $\alpha = 0.2$

# Beating systematics in background subtraction

We analyzed a set of  $\sim 500$  blank-sky XMM pointings and estimated the reproducibility of the background

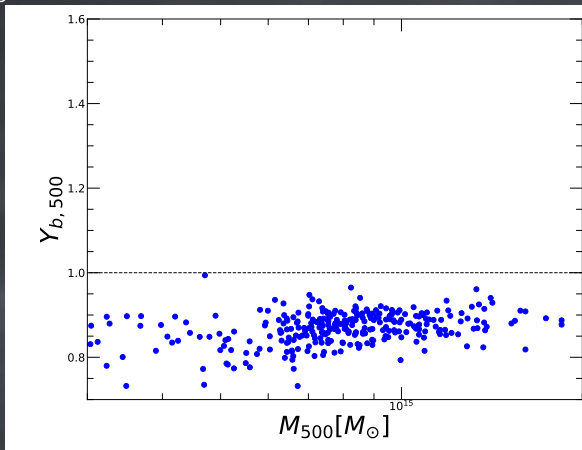


When modeling all known XMM background components we reach a precision of 3% on background subtraction



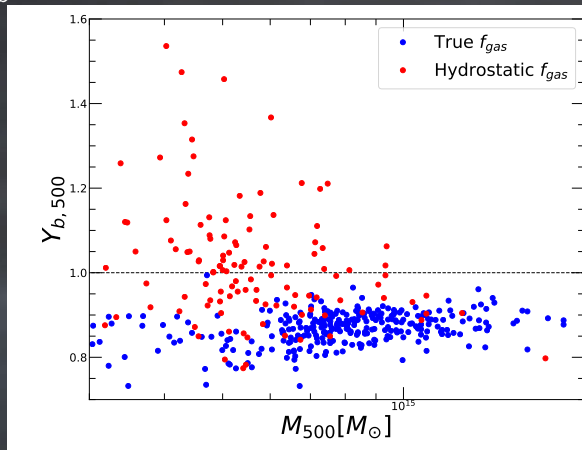
# Universal gas fraction

We used a large set of  $\sim 300$  simulated clusters (Rasia et al. in prep.) to determine the baryon depletion  $Y_b$



# Universal gas fraction

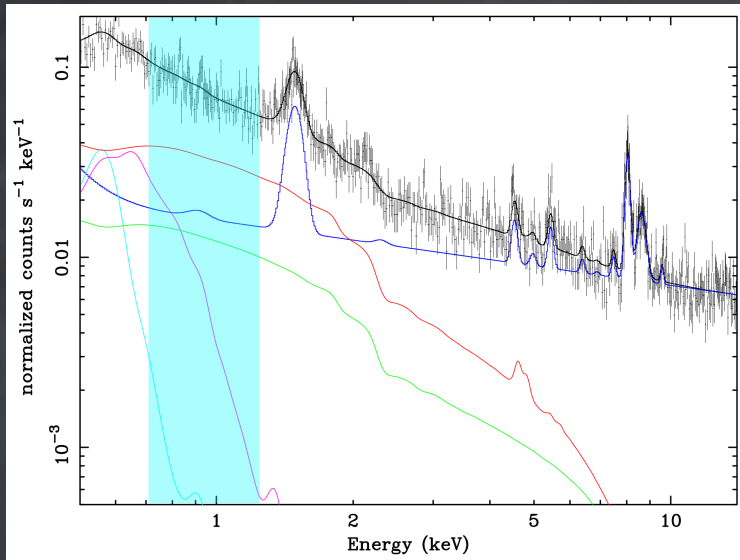
We used a large set of  $\sim 300$  simulated clusters (Rasia et al. in prep.) to determine the baryon depletion  $Y_b$



- The value of  $Y_{bar}$  is nearly independent of the adopted baryonic physics (Planelles et al. 2014)
- Considering the (well-measured) stellar fraction, we set  $f_{gas} = Y_b \frac{\Omega_b}{\Omega_m} - f_\star$

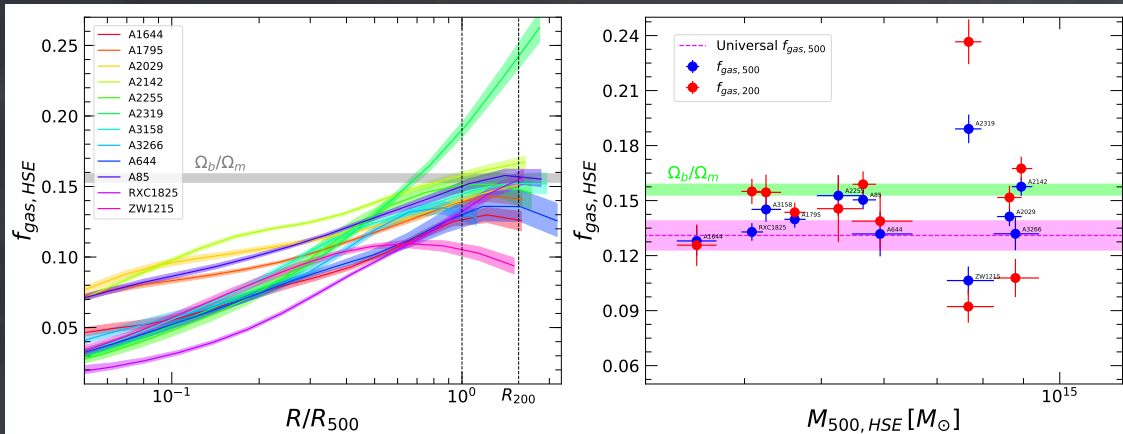
# The X-COP strategy

XMM has a large FOV and collecting area... but also a high and variable background



In the [0.7-1.2] keV band the signal-to-background ratio is maximized

# Testing hydrostatic equilibrium with $f_{gas}$



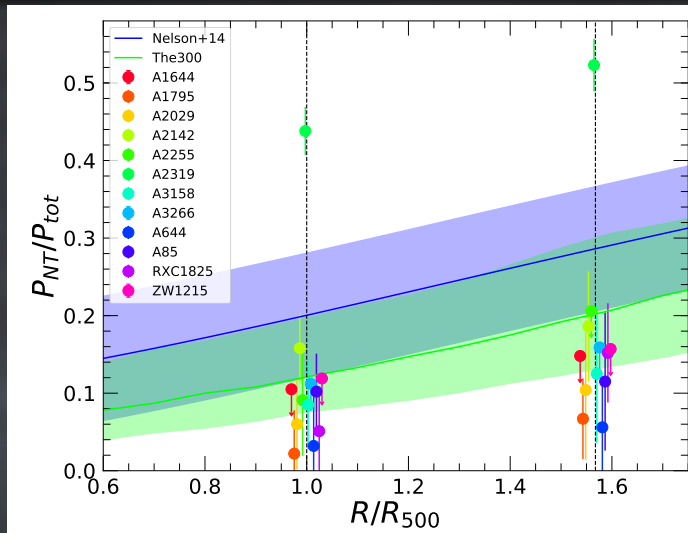
*Eckert et al. 2019*

Median [percentiles] for the full sample:

- $f_{gas,500} = 0.141 [0.131, 0.154]$

- $f_{gas,200} = 0.149 [0.121, 0.161]$

# Non-thermal pressure support vs simulations

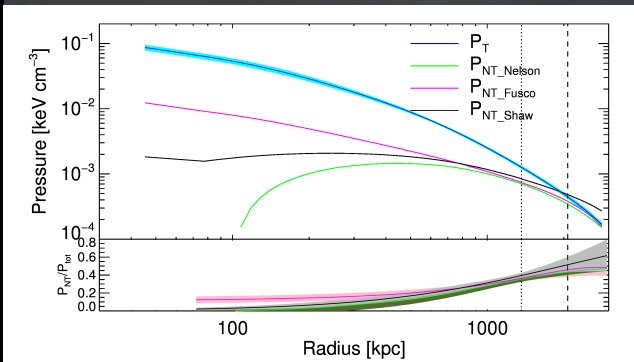
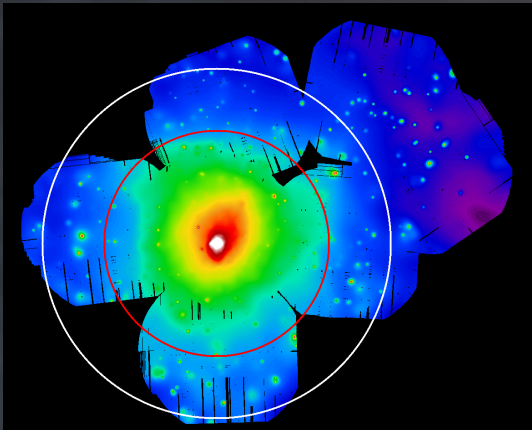


*Eckert et al. 2019*

With one exception (A2319) the level of NT pressure is *lower* than predicted  
Median  $P_{NT,500} = 6\%$ ,  $P_{NT,200} = 10\%$

# The case of A2319

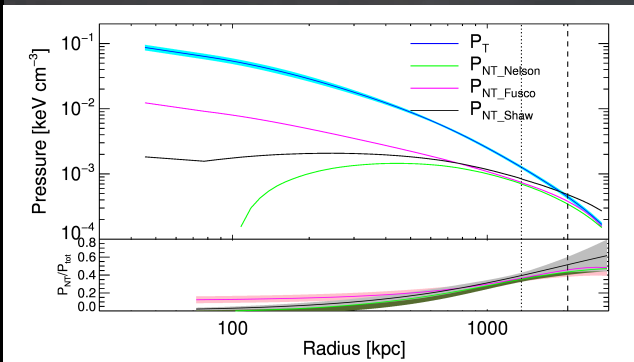
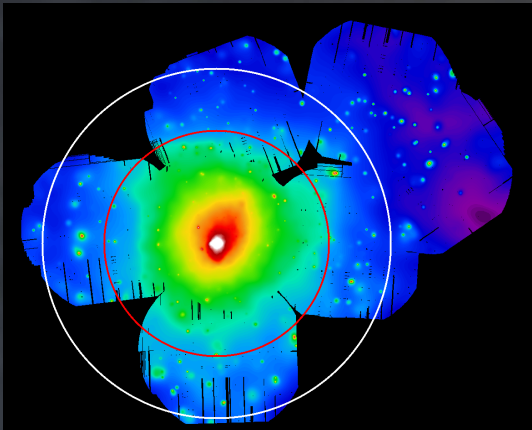
A2319 is a head-on merger with 3:1 mass ratio



*Ghirardini, Ettori, DE et al. 2018*

# The case of A2319

A2319 is a head-on merger with 3:1 mass ratio

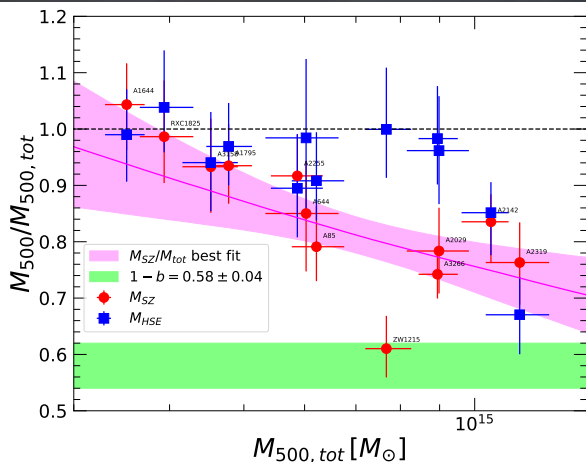
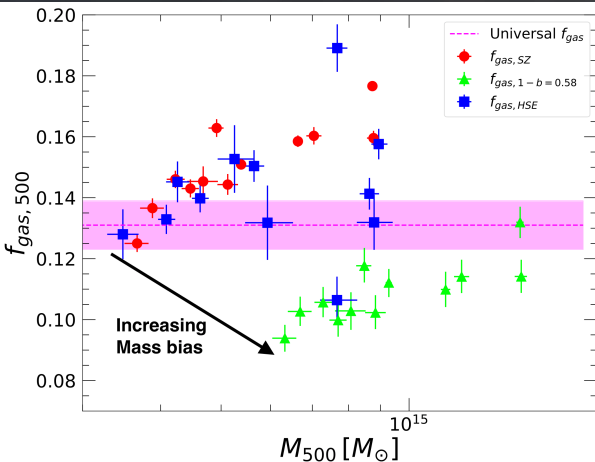


*Ghirardini, Ettori, DE et al. 2018*

A2319 is probably in a transient phase of high NT pressure ( $\sim 40\%$ )

# Non-thermal pressure and hydrostatic bias

We compared our masses corrected for NT pressure with hydrostatic masses



Eckert et al. 2019

- On average we measure  $M_{\text{HSE}}/M_{\text{tot}} = 0.94 \pm 0.04$
- *Planck* masses are slightly biased low,  $M_{\text{SZ}}/M_{\text{tot}} = 0.85 \pm 0.05$
- $1-b = 0.58 \pm 0.04$  would imply a very low  $f_{\text{gas}} = 10.5\%$